

Electron Spin Qubits

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- Review of quantum dots (mostly GaAs/AlGaAs), with many references:
[Hanson, Kouwenhoven, Petta, Tarucha, Vandersypen, Rev. Mod. Phys. **79**, 1217 \(2007\).](#)
- Overview of older silicon spin qubit work:
[Morton, McCamey, Eriksson, Lyon, Nature, **479**, 345 \(2011\).](#)

Outline

- Background on Si and electrons
- Spin resonance measurements of spin coherence in Si
- GaAs quantum dot spin experiments
- Si quantum dot spin experiments
- Si donor spin experiments
- Other schemes (electrons on helium, ...)

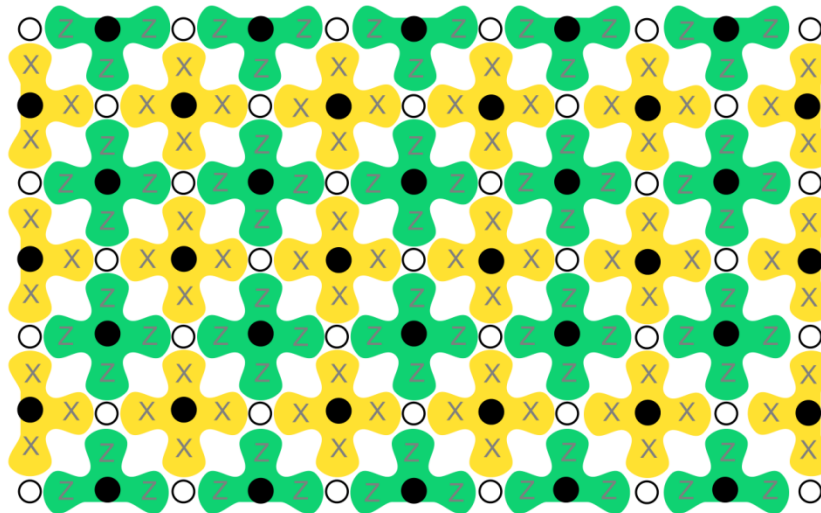
Why Electron Spins?

$\sim 10^9$ Qubits

for full-scale Quantum Computer

- Need small qubits
- Need fast qubits
- Recent Ion Trap proposal (shuttle ions)
 - $100 \times 100 \text{ m}^2$ [Lekitsch, Sci. Adv. **3**, e1601540 (2017).]
= 2.5 acres

Surface Code (Error Correction)



- Every cycle
 1. CNOT gates between the black dots and 4 neighbor white dots colored yellow
 2. Measure state of black dot
 3. Repeat 1 & 2 for green colored regions
- Turn off these operations in regions to define logical qubits
- Move (braid) these logical qubits to perform logical gates

Electron spins as quantum bits

- Natural 2-level system (for $S = 1/2$)
- Spins interact weakly (magnetic dipole)
 - ⇒ long coherence (in principle)
 - But, weak interaction
 - ⇒ difficult to manipulate spin
 - ⇒ difficult to measure spin
 - ⇒ difficult to make 2-qubit gates

Energies and transitions

- Zeeman Hamiltonian

- $H = g\mu_B \mathbf{B} \cdot \mathbf{S} = E_Z$

- Often $g \sim 2$, and $S = 1/2$

- $\Rightarrow E_Z$

- $\sim 10 \text{ GHz at } B=0.35\text{T}$

- $\sim 0.5\text{K}$

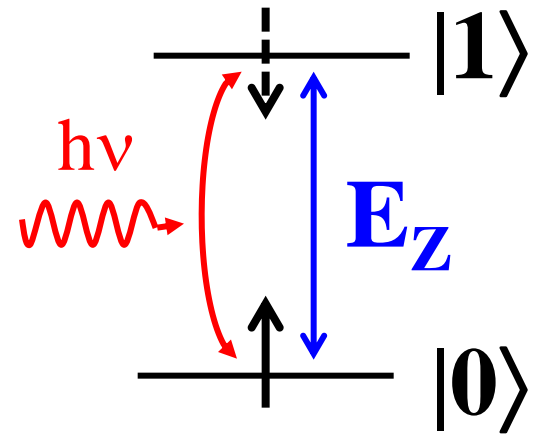
- \Rightarrow Drive spins with microwaves

- Typically 5 – 50 GHz

- Driven by magnetic field of microwaves (weak)

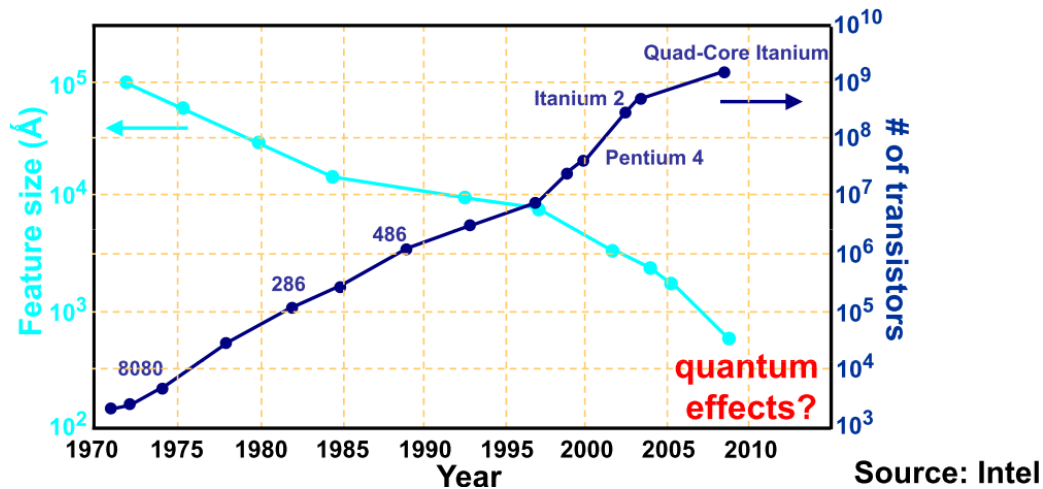
- \Rightarrow Can initialize by cooling to mK

- \blacktriangleright Conversions: 10 GHz \sim 450 mK \sim 41 μeV



Electron spins in semiconductors

- Why semiconductors?
 - Electrons readily moved and controlled in semiconductors
 - Huge industry exists which can manufacture chips with $> 10^{11}$ devices

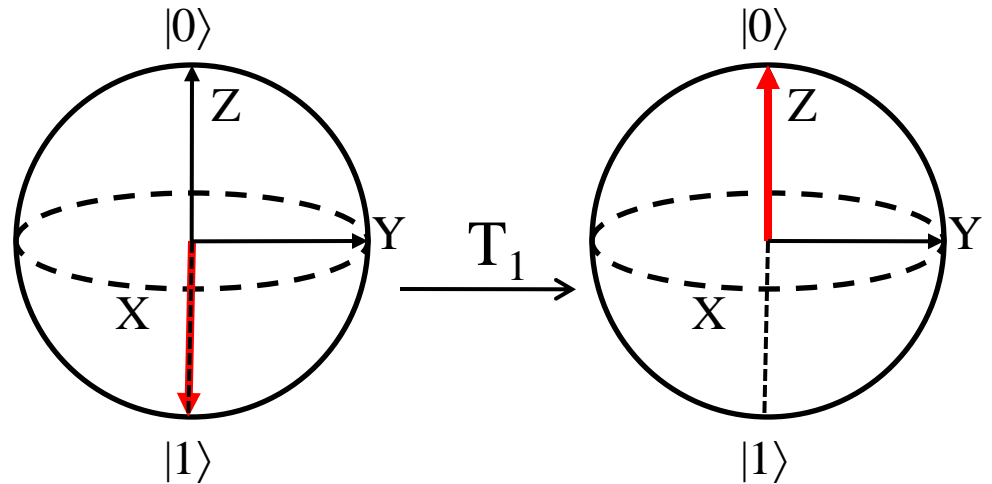


- Data from 1950's showed long spin lifetimes (T_1)
- Semiconductors can be extremely pure
 - So, maybe long spin coherence (T_2)

Decoherence on the Bloch Sphere

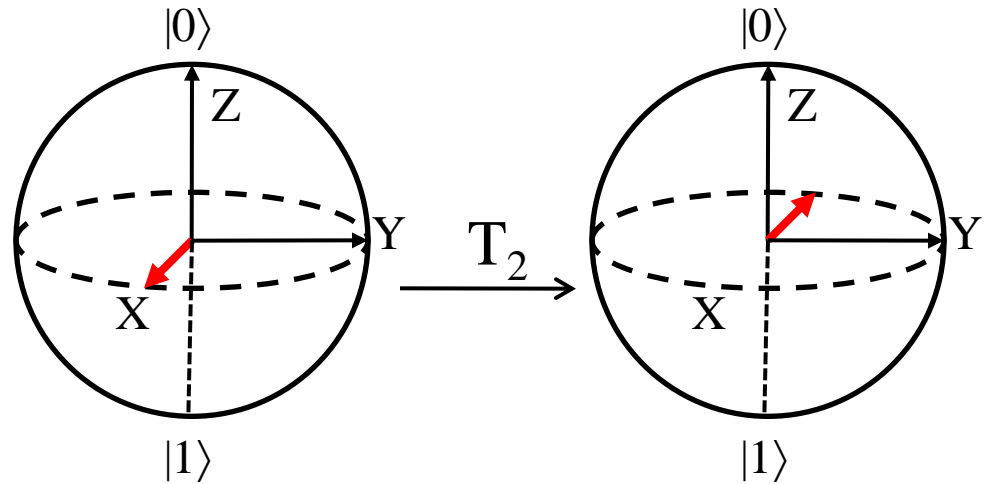
- $T_1 =$ bit flip time

$$|1\rangle \xrightarrow{T_1} |0\rangle$$



- $T_2 =$ phase flip time

$$\frac{|0\rangle + |1\rangle}{\sqrt{2}} \xrightarrow{T_2} \frac{|0\rangle - |1\rangle}{\sqrt{2}}$$



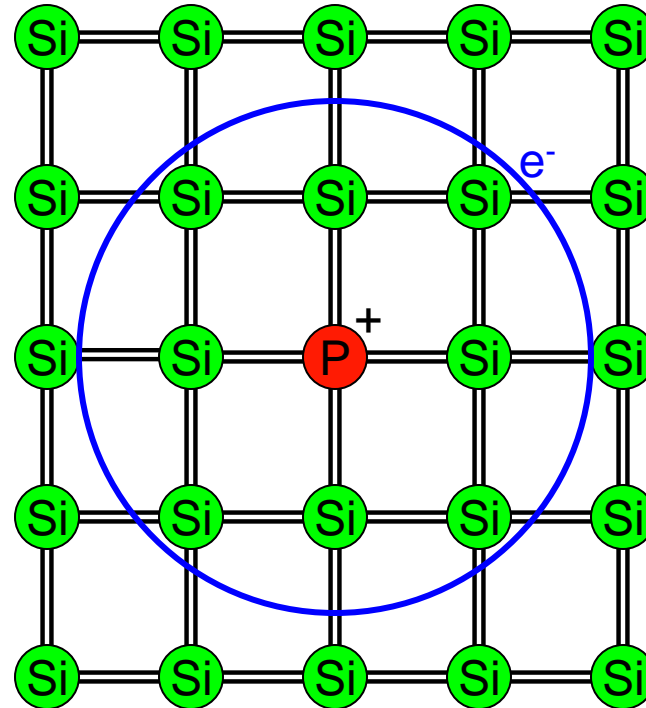
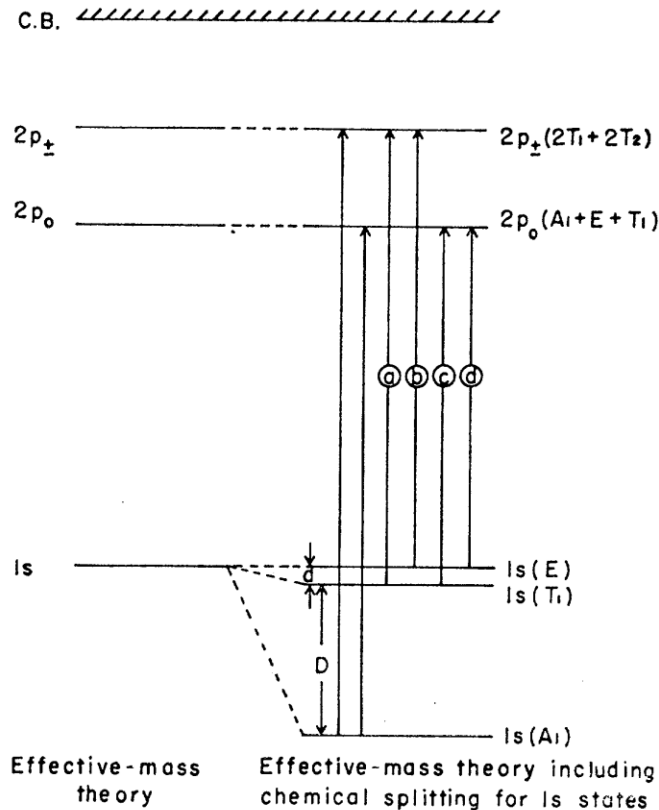
What do we know about electron
spin coherence in Si?

(in ~2000 assumed maximum coherence ~ 1 ms)

Pulsed electron spin resonance (ESR = EPR)

- Ensemble technique (measure $\sim 10^8 - 10^{13}$) spins at once – a **spatial** ensemble
 - Need many spins for enough signal
 - Often will not do **time** ensemble
 - Some sort of ensemble required for coherence
- Often simpler sample preparation than devices (sometimes just cutting to the right size)

Donor impurities in silicon



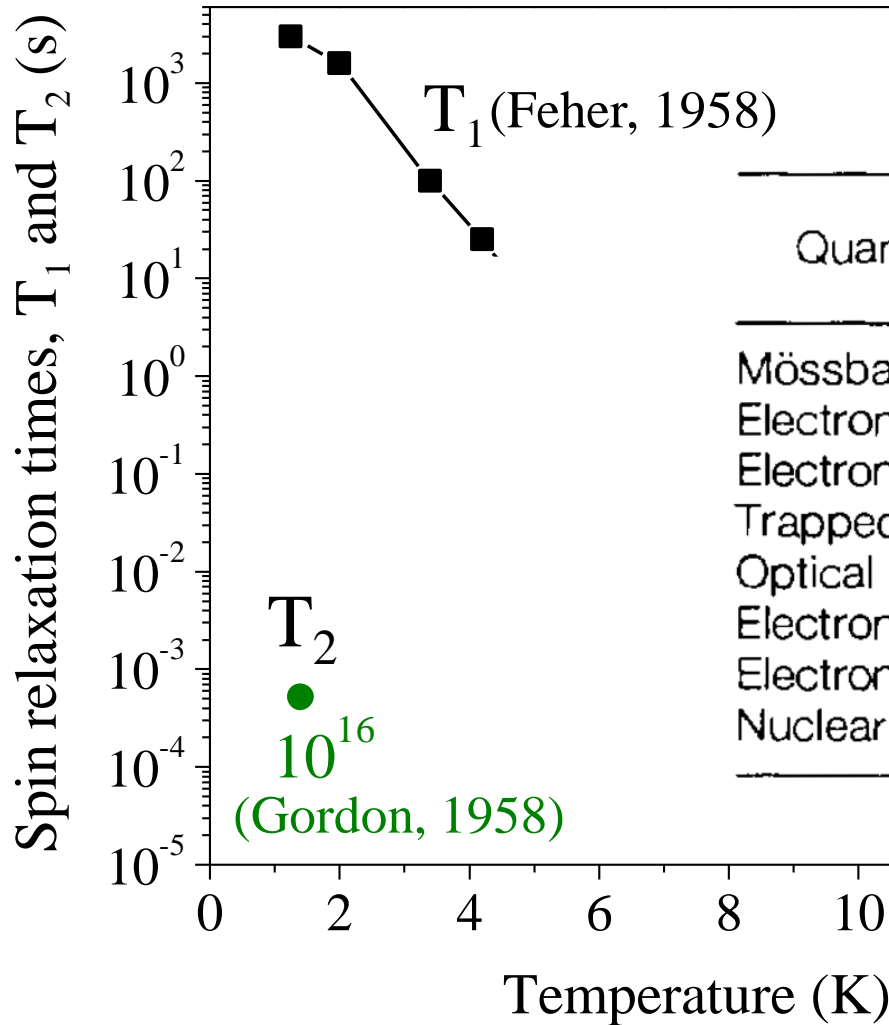
Ionization energy (phosphorus) ~ 50 meV

Impurity Bohr radius ~ 2 nm

Lowest excited state ~ 10 meV (not hydrogenic)

Nuclear spin (phosphorus) $= 1/2$

Spin qubits

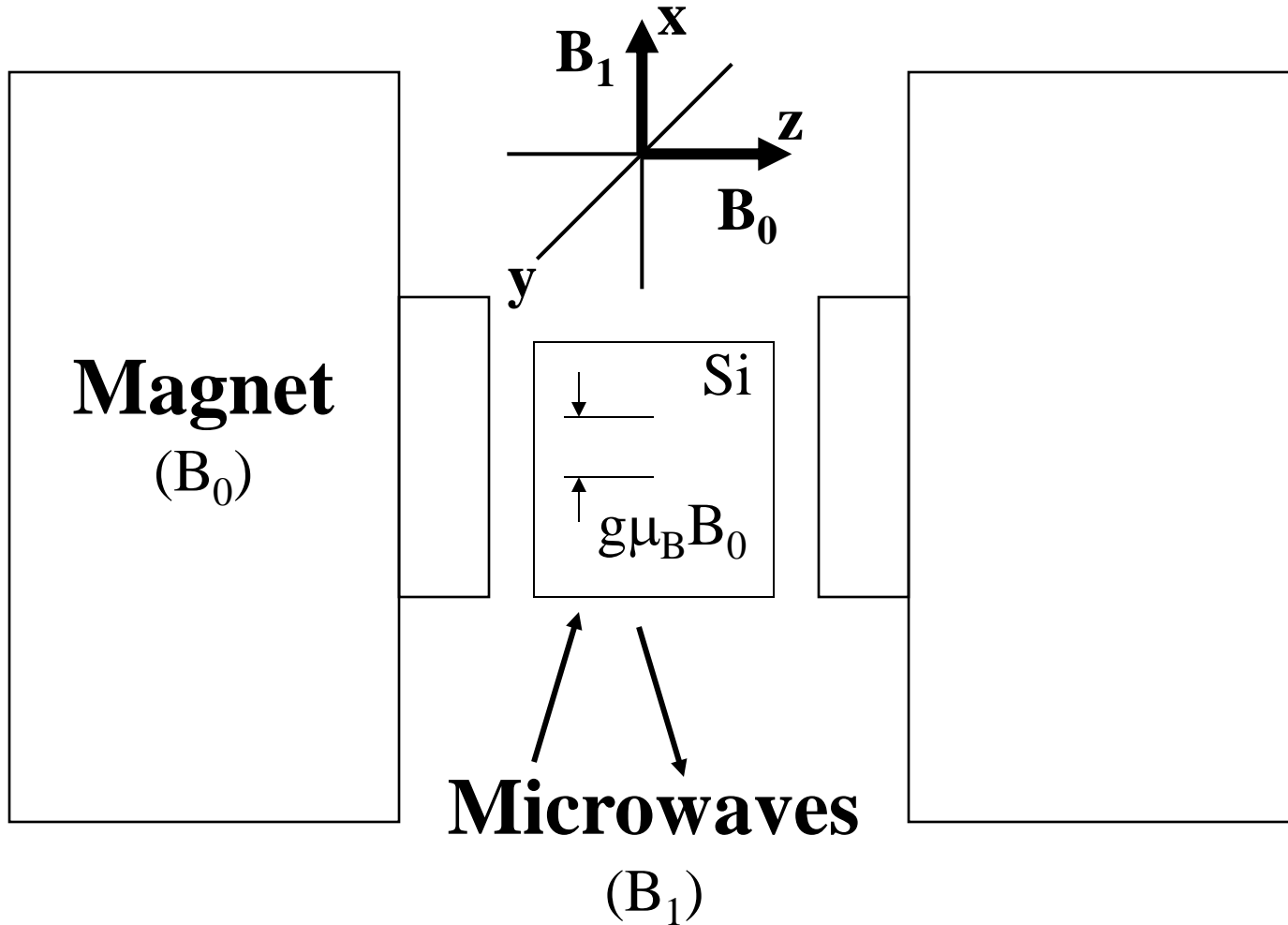


Quantum system	t_{switch} (s)	t_{ϕ} (s)	Ratio
Mössbauer nucleus	10^{-19}	10^{-10}	10^9
Electrons: GaAs	10^{-13}	10^{-10}	10^3
Electrons: Au	10^{-14}	10^{-8}	10^6
Trapped ions: In	10^{-14}	10^{-1}	10^{13}
Optical microcavity	10^{-14}	10^{-5}	10^9
Electron spin	10^{-7}	10^{-3}	10^4
Electron quantum dot	10^{-6}	10^{-3}	10^3
Nuclear spin	10^{-3}	10^4	10^7

DiVincenzo, Science **270**, 255 (1995)

Electron Spin Resonance (ESR)

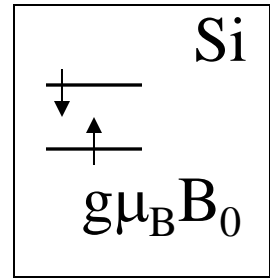
– the Laboratory Frame



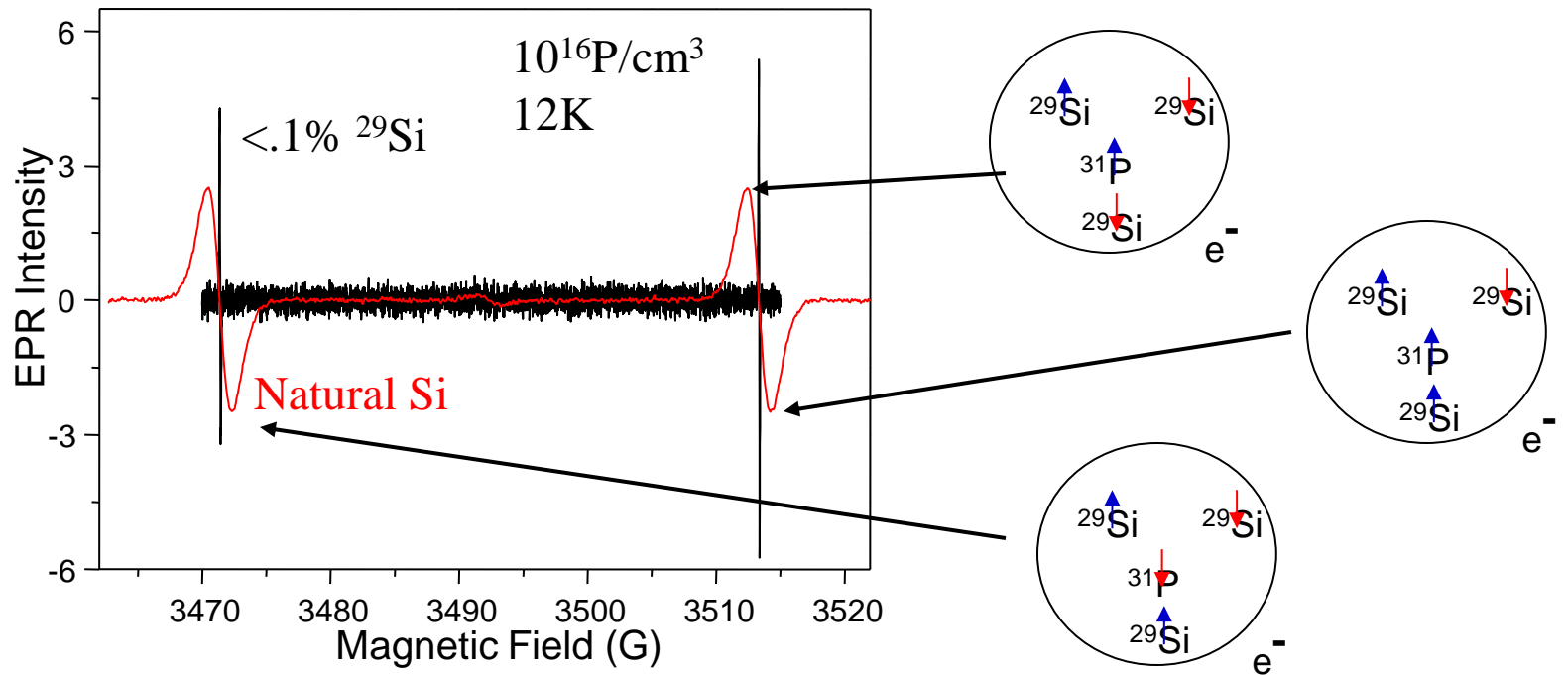
Adjust magnetic field (B_0) so that $g\mu_B B_0 \sim h\nu$ and measure microwave absorption and emission.

Electron Spin Resonance (ESR)

- Put spins into magnetic field, B_0

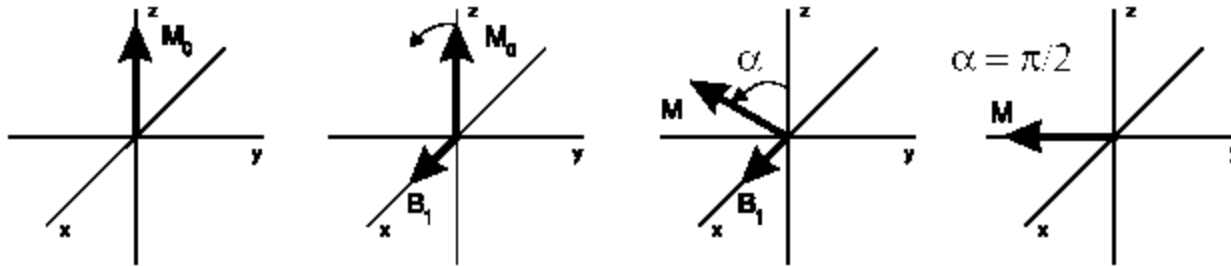


↔ Microwaves
at $h\nu = g\mu_B B_0$

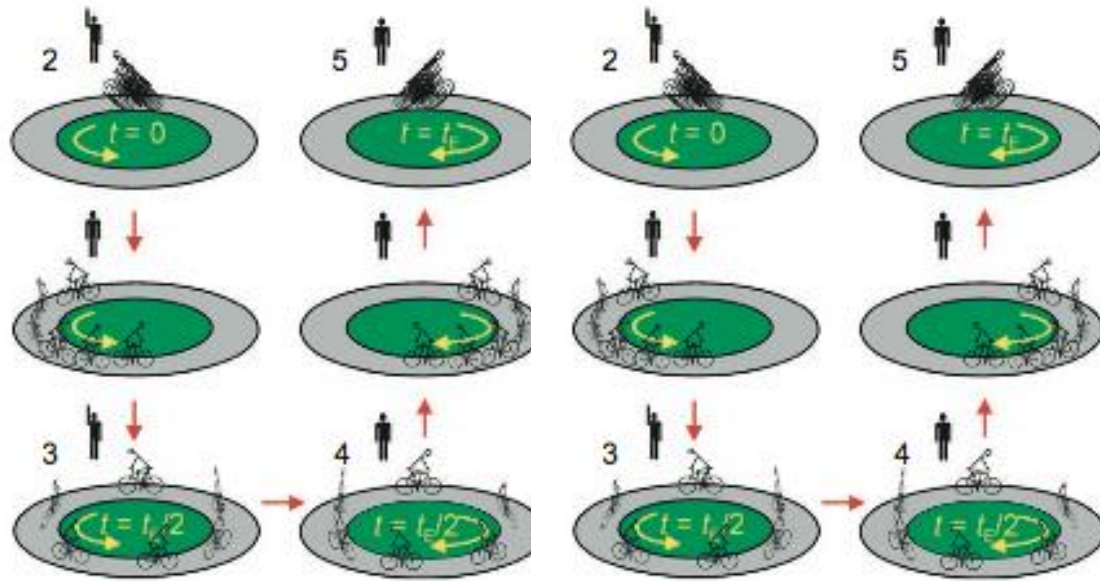


The Rotating Frame and a $\pi/2$ Pulse

- The electrons' magnetic moment is precessing about B_0 at the Larmor frequency ($\sim 10\text{GHz}$)
- Reference frame rotating at $g\mu_B B_0 \Rightarrow$ spins nearly stationary
- In rotating frame a $\pi/2$ -pulse (B_1) rotates the magnetization 90° around the x or y axis.
 - The B_1 pulse must “rotate” at the Larmor frequency



Spin echo (Hahn echo)



identities happen
 relax (thermalize)
 lose phase information



Microwave pulses

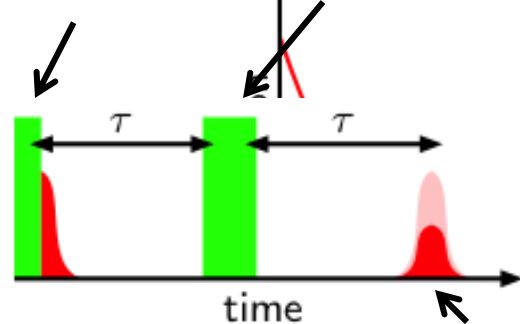
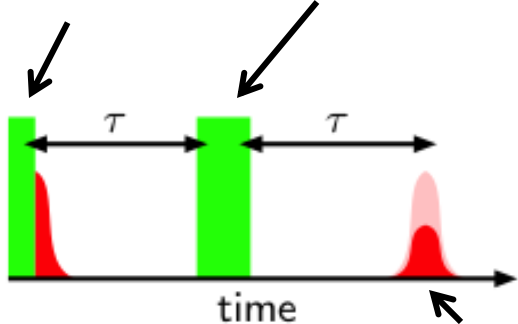
Microwave pulses

$\pi/2$ pulse
 = "start"

π pulse
 = "reverse"

$\pi/2$ pulse
 = "start"

π pulse
 = "reverse"



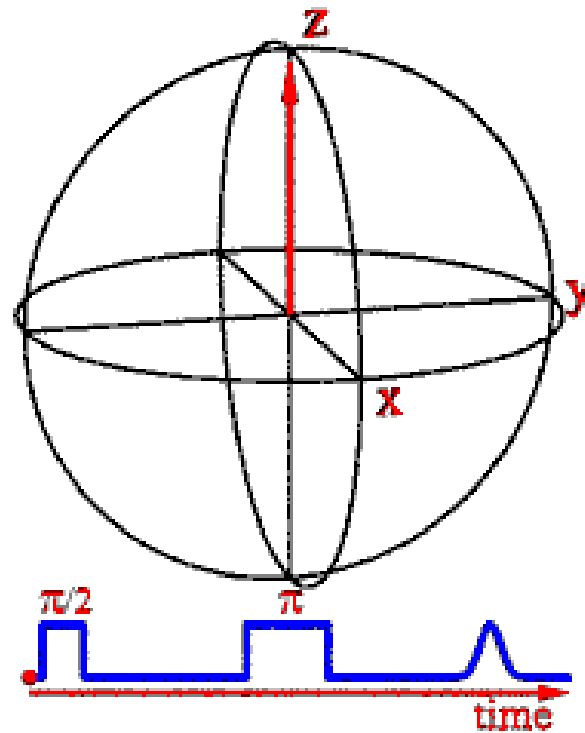
T_1

$e^{-2\tau/T_2}$

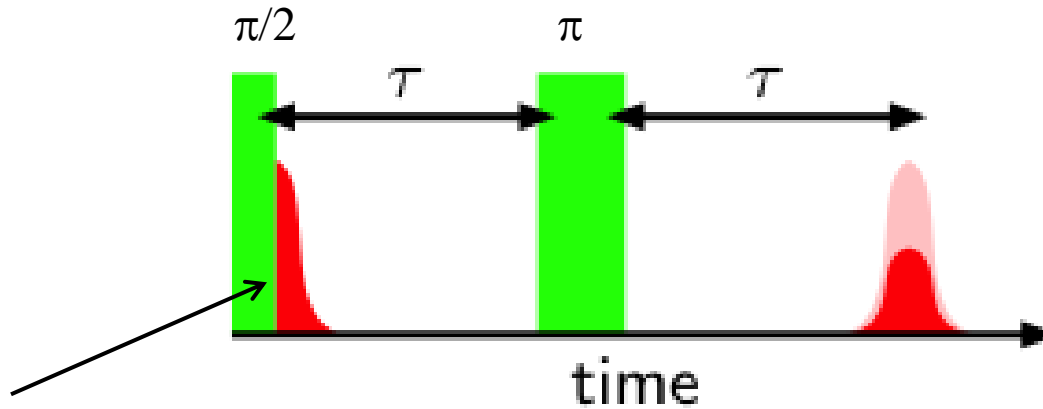
Echo = emission
 of microwaves

Echo = emission
 of microwaves

Spin Echo Animation

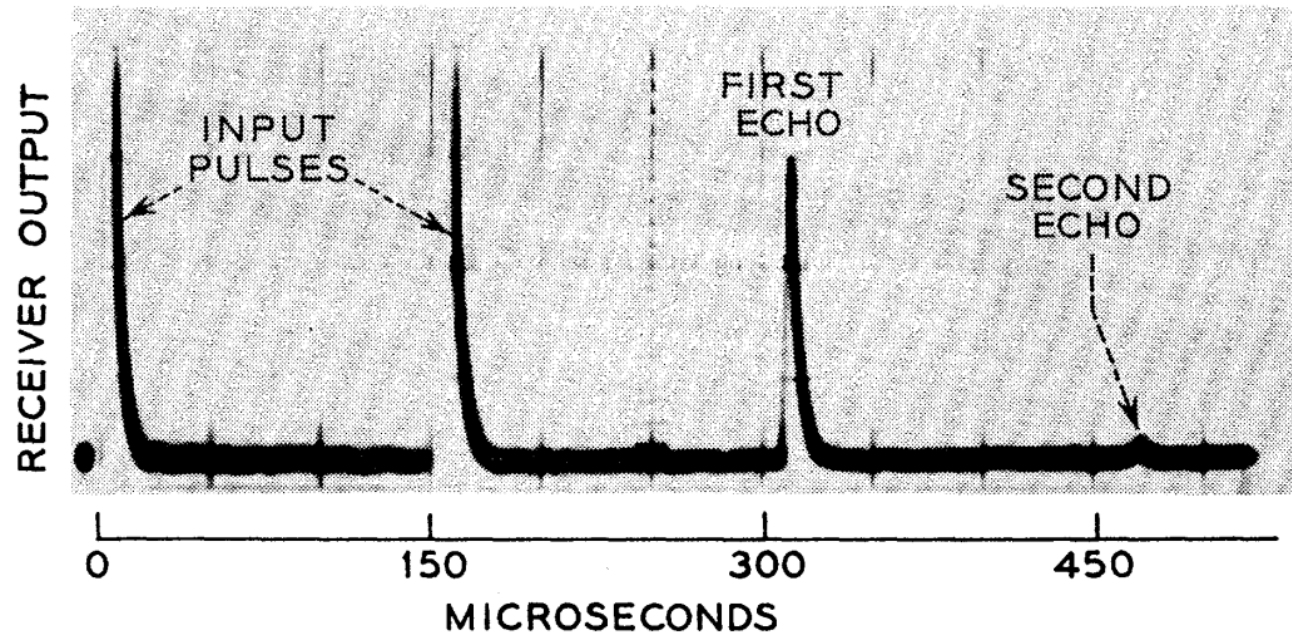


Magnetic Resonance Jargon



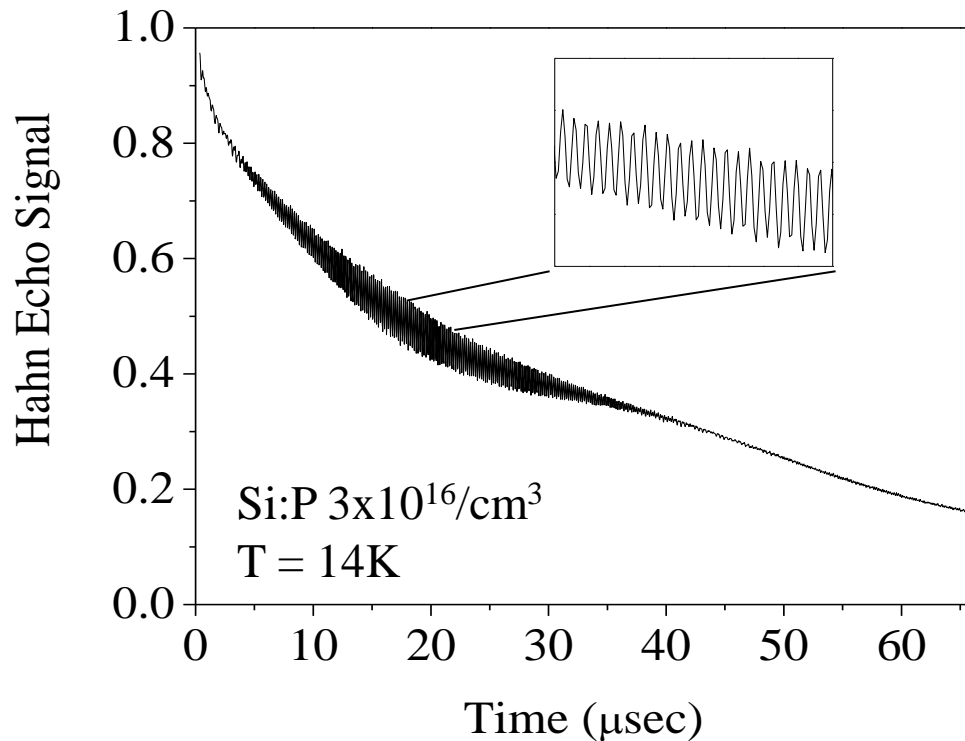
- FID = Free Induction Decay = initial emission
- T_2^* = “Dephasing Time” = time for different spins to go out of phase with one another in FID
- “Refocusing pulse” = the π -pulse
- T_2 = decay time of the echo = “coherence time” = “spin-spin relaxation time”
- T_1 = “Relaxation time” = “Spin flip time” = “spin-lattice relaxation time”

First Microwave Spin Echo Experiment Si:P

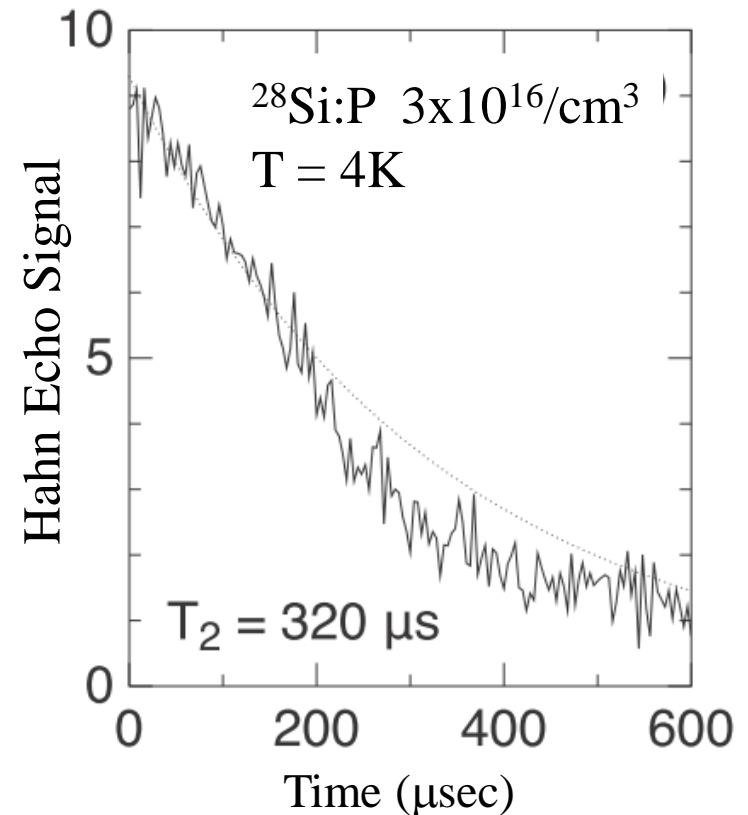


- Gordon & Bowers, Phys. Rev. Lett. **1**, 369 (1958)
- Measured $T_2 \sim 520 \mu\text{s}$ with $^{28}\text{Si:P}$
 - Longest electron spin T_2 until ~ 2003 (?)

Electron Spin Echoes from Donors in Silicon



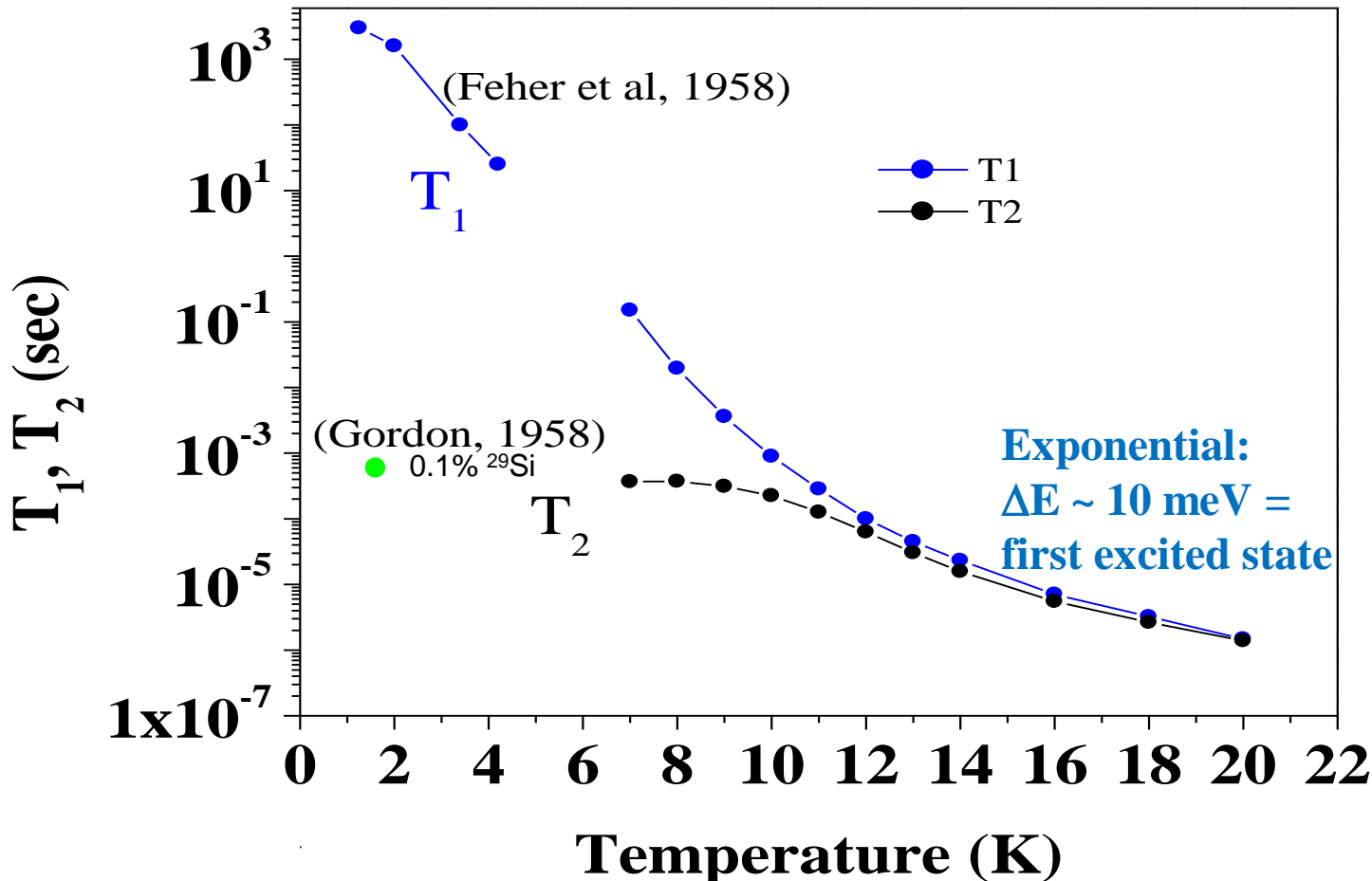
Natural silicon



Isotopically enriched silicon

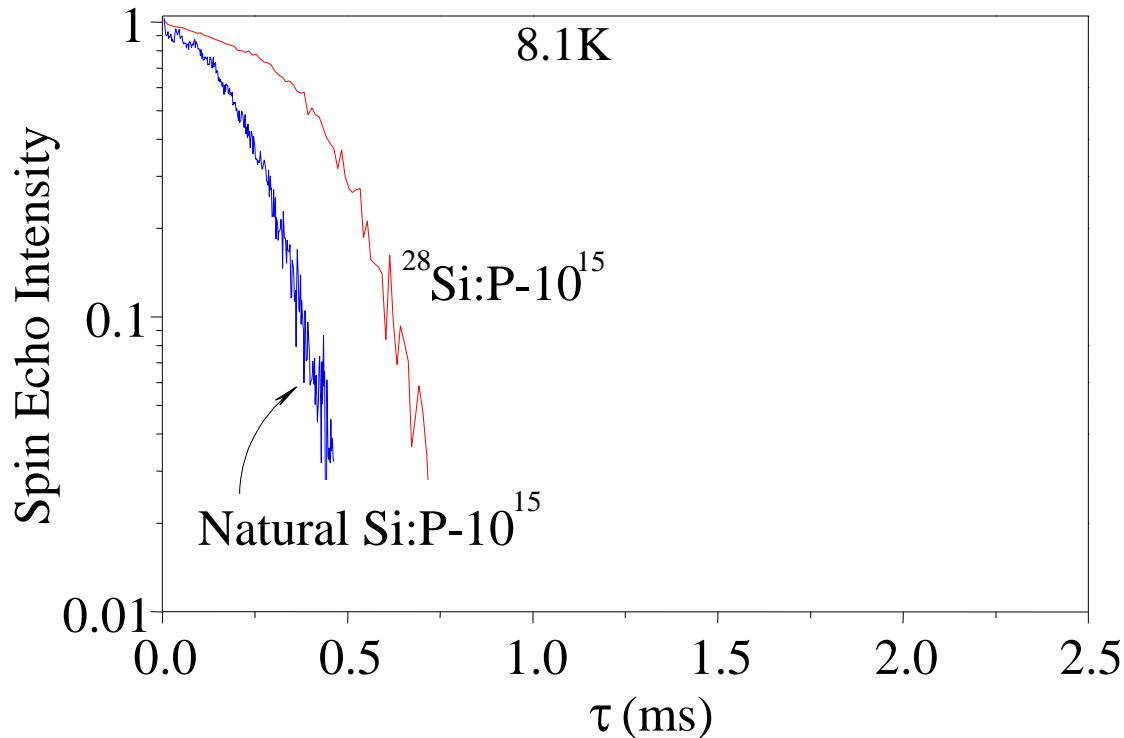
Donor electron spin qubits

- Doping $\sim 10^{16}/\text{cm}^3$
- Isotopically purified $^{28}\text{Si}:\text{P}$ (800ppm ^{29}Si)



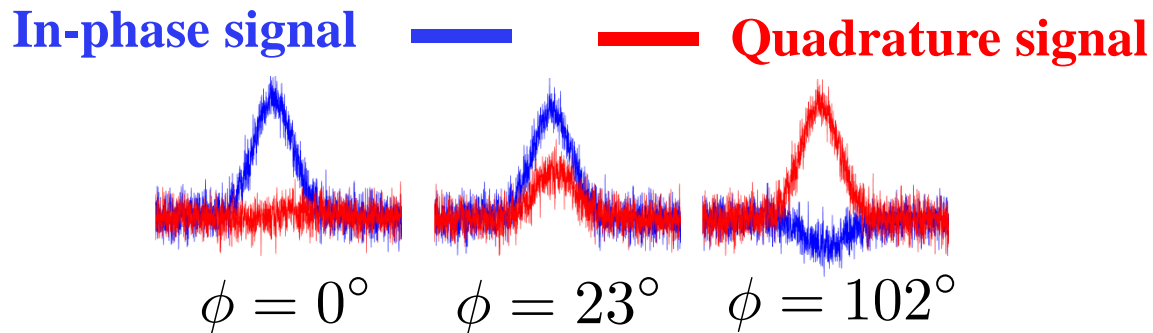
Gordon & Bowers measured $T_2 \sim 520 \mu\text{s}$ with $^{28}\text{Si:P}$

- Now measured it with fancier (= more expensive) equipment and get a similar T_2
- What was limiting T_2 ?



Global Magnetic Field Noise

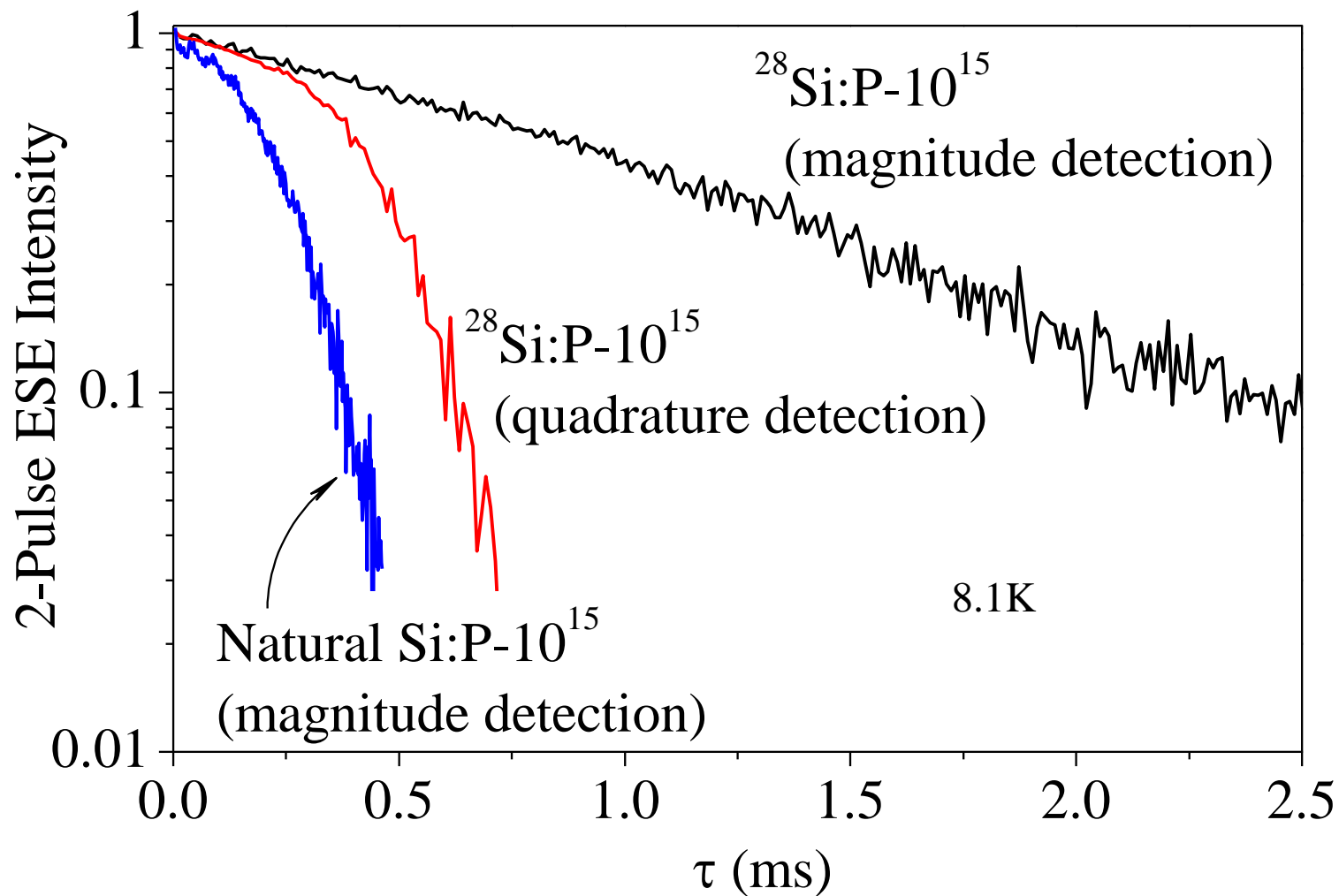
Single-shot Hahn echo, quadrature detection,
3 different 1-shot experiments



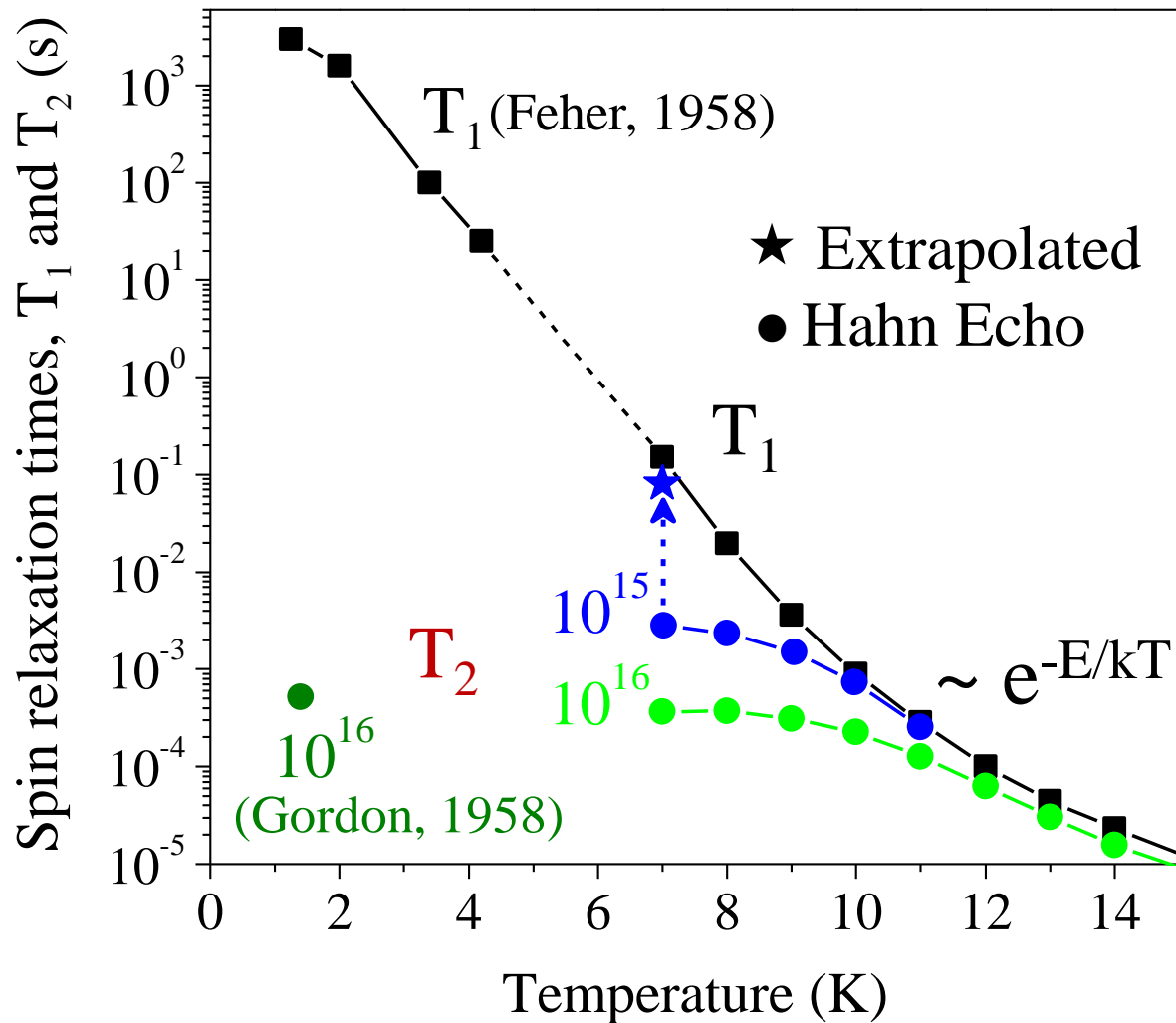
Strong echo signals \Rightarrow Spins stay in phase with one another

Global magnetic field fluctuations \Rightarrow Randomized echo phase

Magnitude Detection

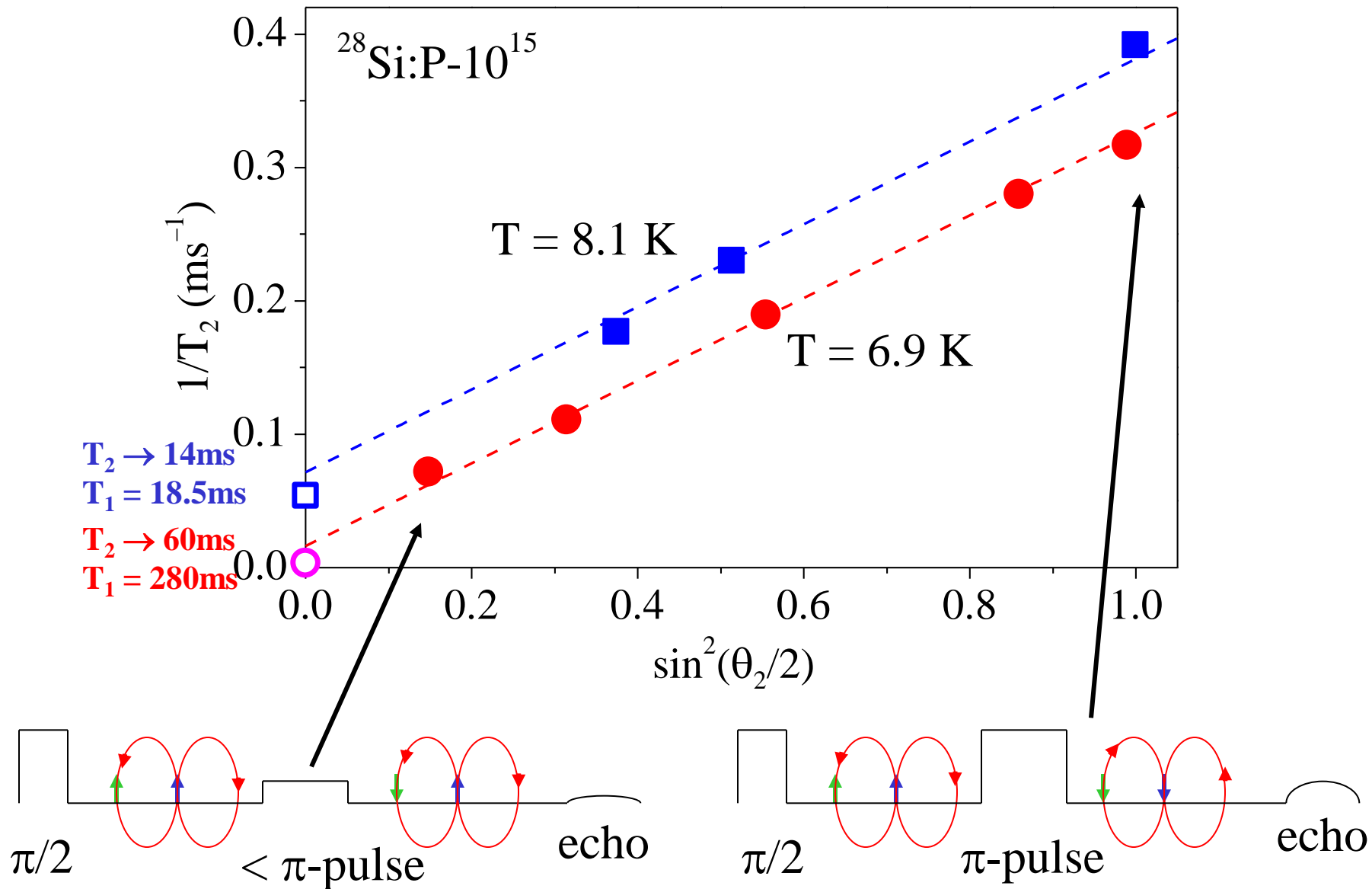


Coherence without Instantaneous Diffusion



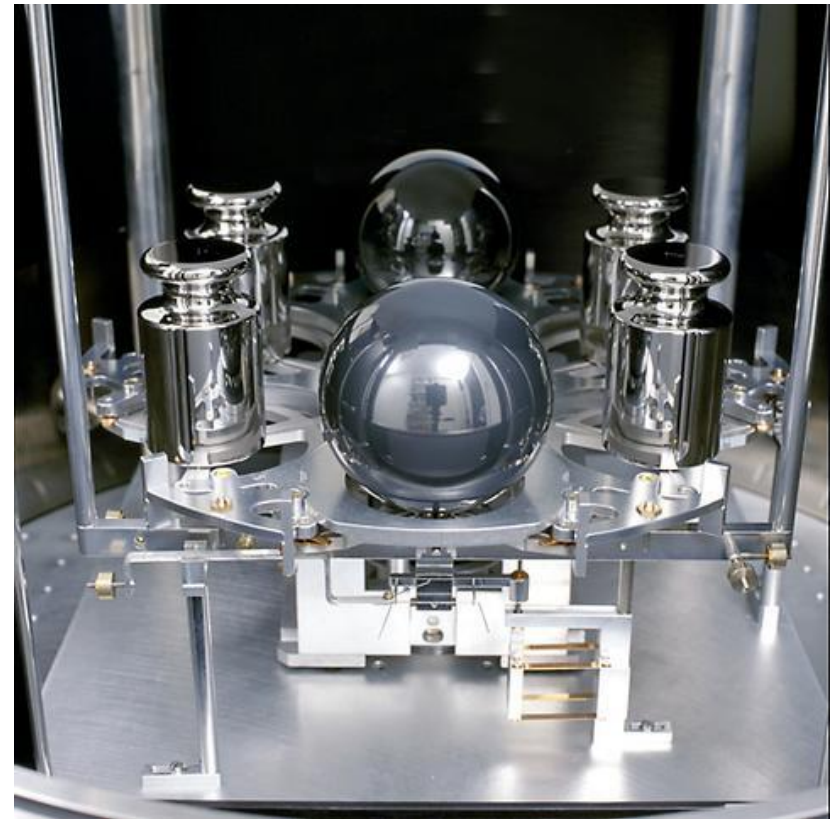
Eliminating Instantaneous Diffusion

Vary power of second pulse \Rightarrow probability to flip spin without flipping neighbors



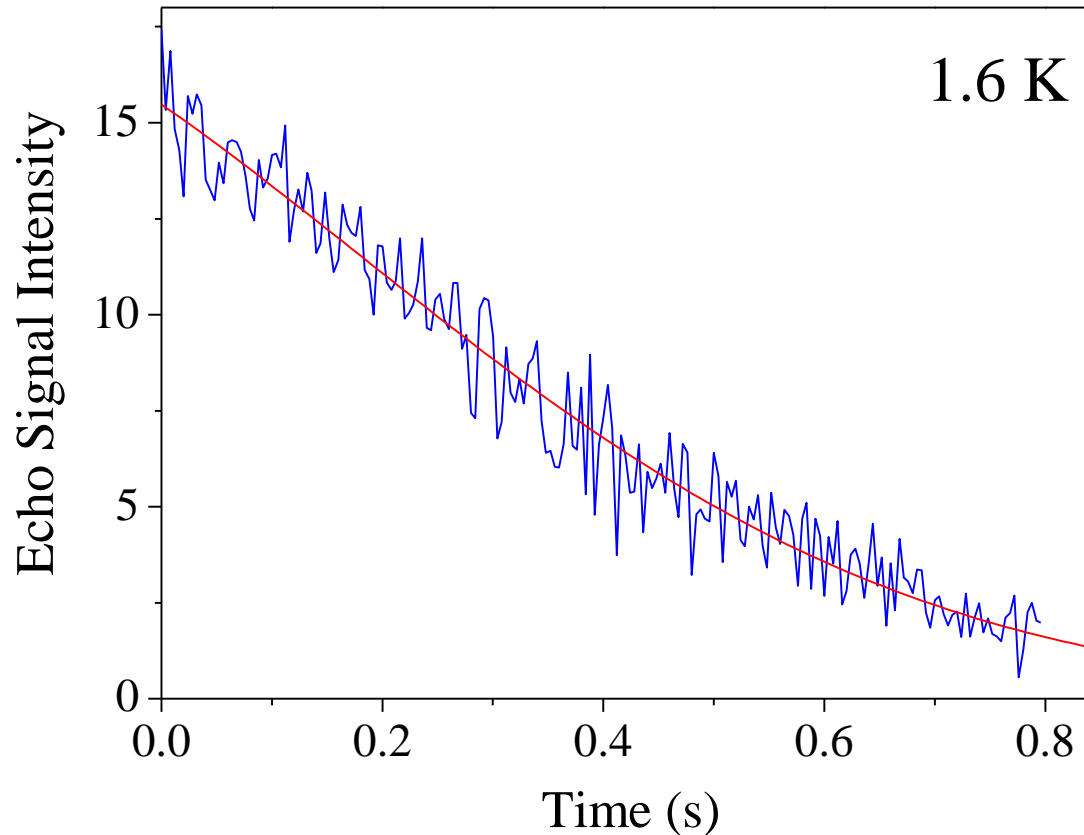
Avogadro Project Silicon

- Very highly enriched ($\sim 50\text{ppm } ^{29}\text{Si}$)
- Very high chemical purity (boron, phosphorus $\sim 10^{12}/\text{cm}^3$)
- Large pieces of bulk Si



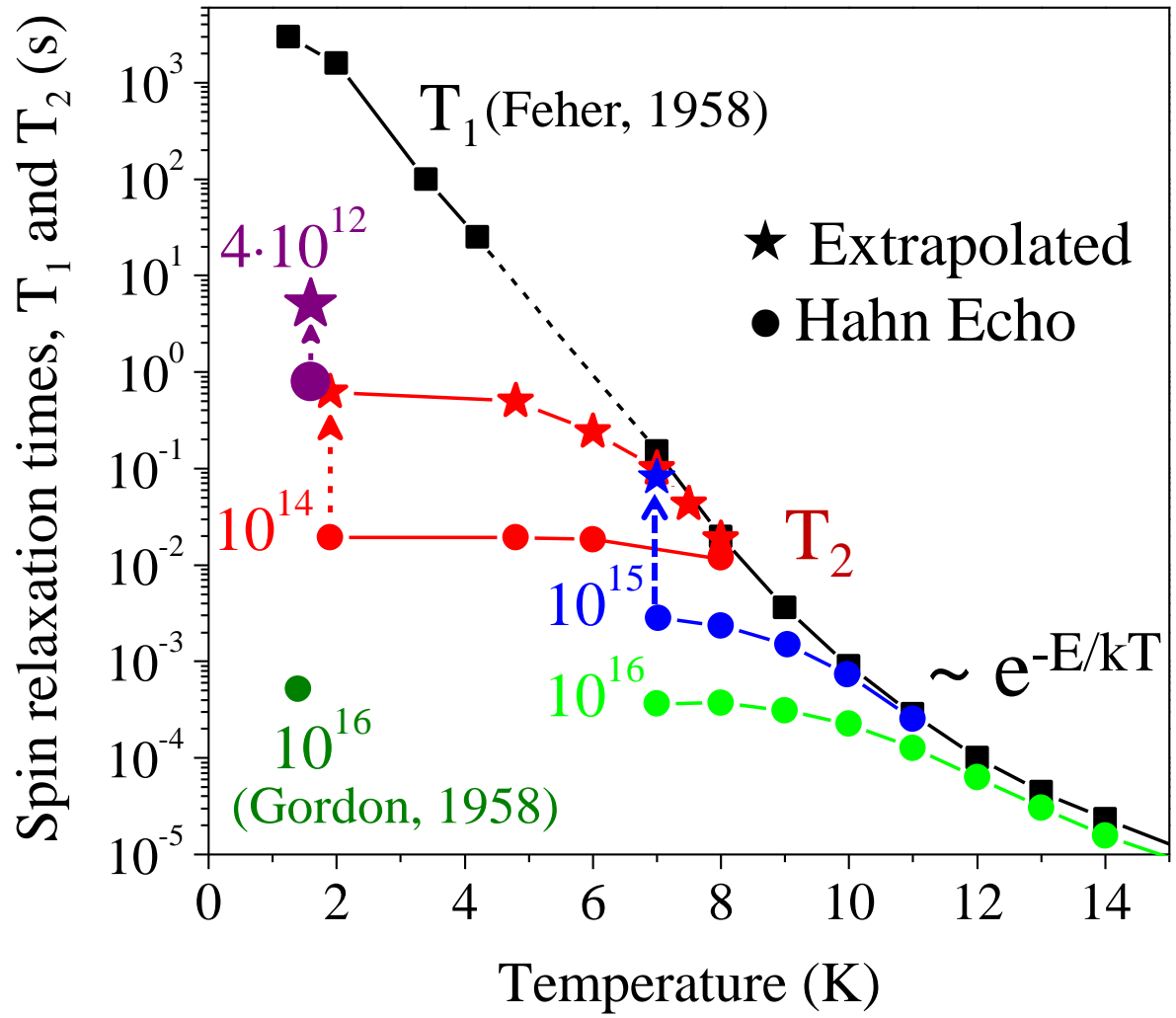
30x More Lightly Doped $^{28}\text{Si}:\text{P}$

$4 \times 10^{12} \text{ P/cm}^3$, $8 \times 10^{12} \text{ B/cm}^3$, 100 ppm ^{29}Si

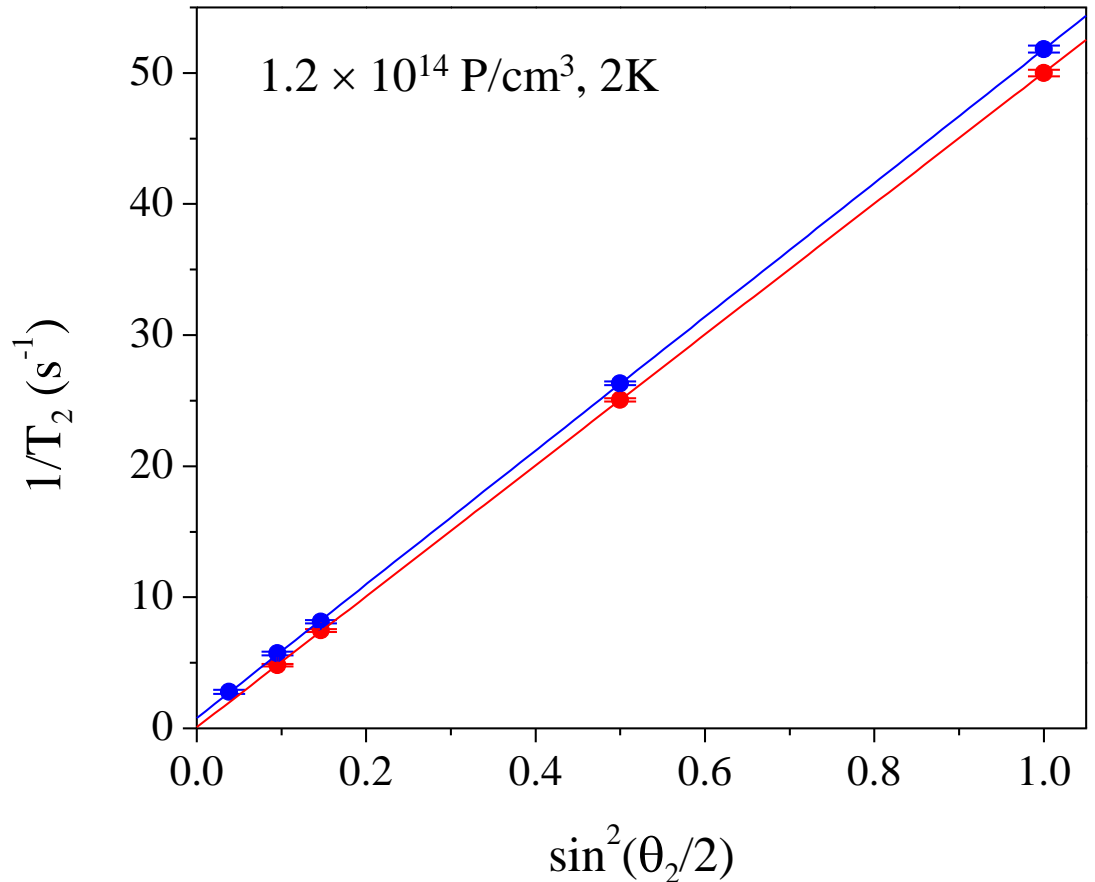
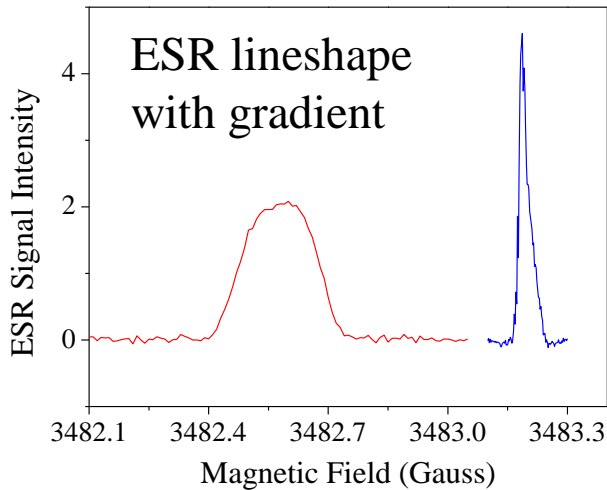
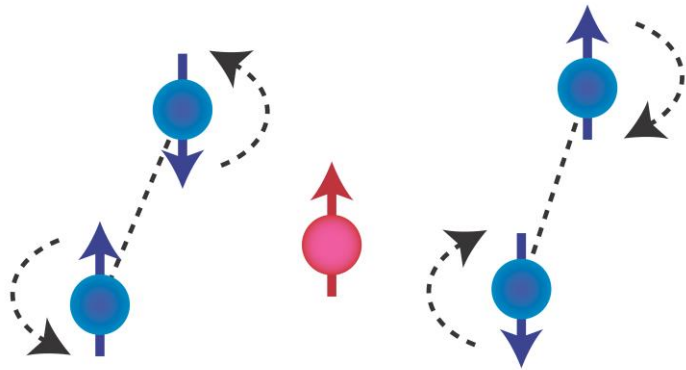


$$Echo \propto e^{-t/T_2} e^{-(t/T_{SD})^n}$$

- $T_{SD} = 0.7 \text{ sec}$; $n = 2$
- $T_2 = 0.8 \text{ sec}$



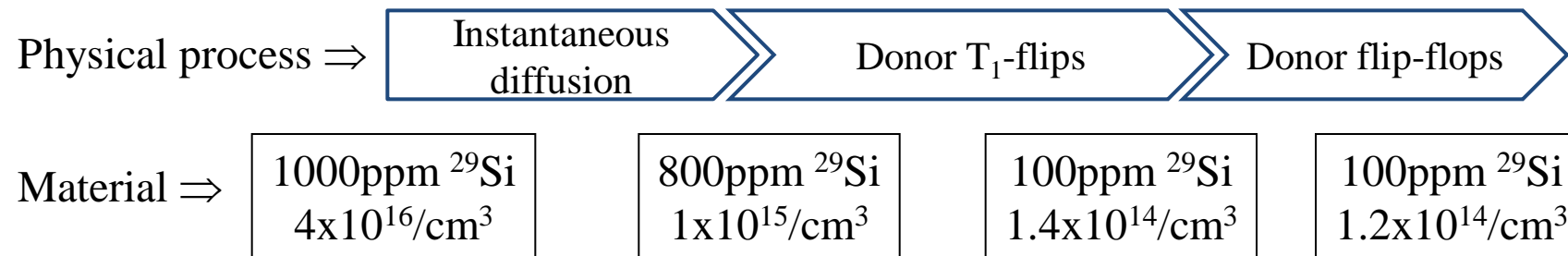
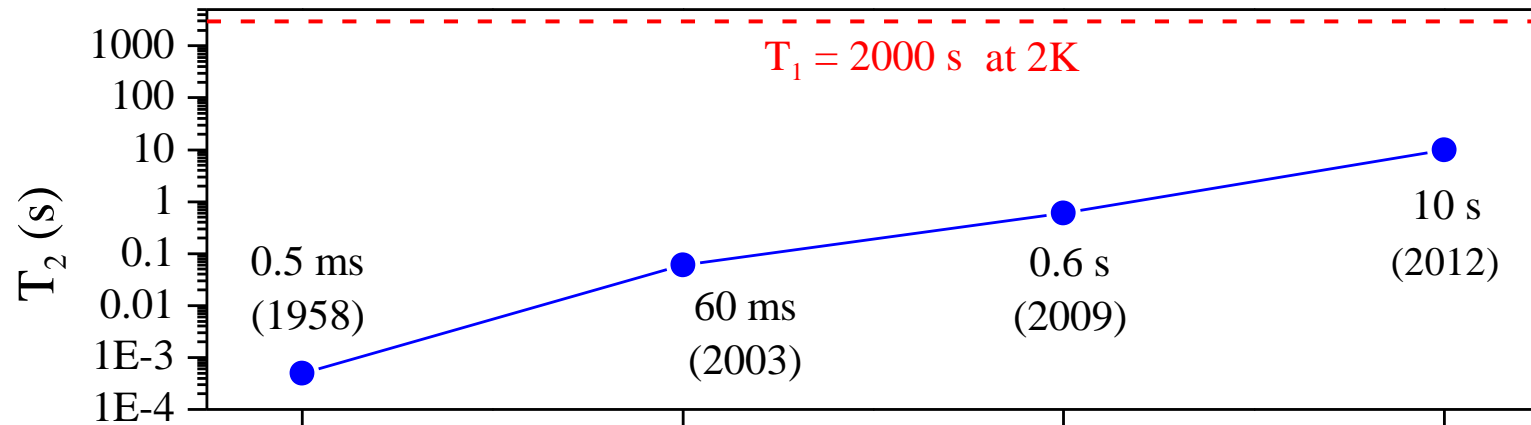
Suppressing Donor Flip-Flops with a Magnetic Field Gradient – take 4



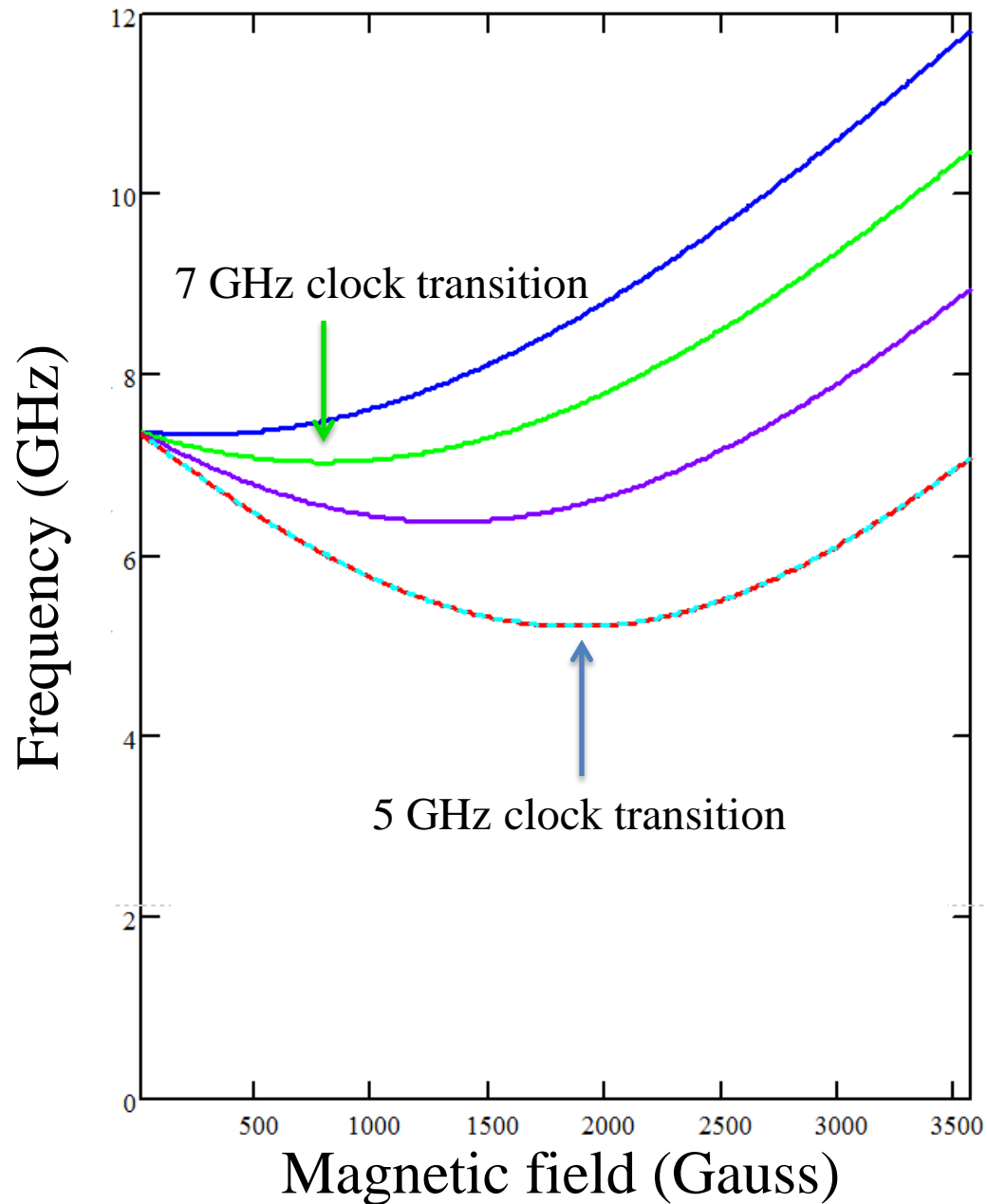
No gradient $\Rightarrow T_2 = 1.3 \pm 0.1$ sec

Gradient (0.3Hz/nm) $\Rightarrow T_2 = 12 \pm 7$ sec

Electron Spin Coherence in Ultra-pure Silicon - Isolated Donor T_2 in ^{28}Si

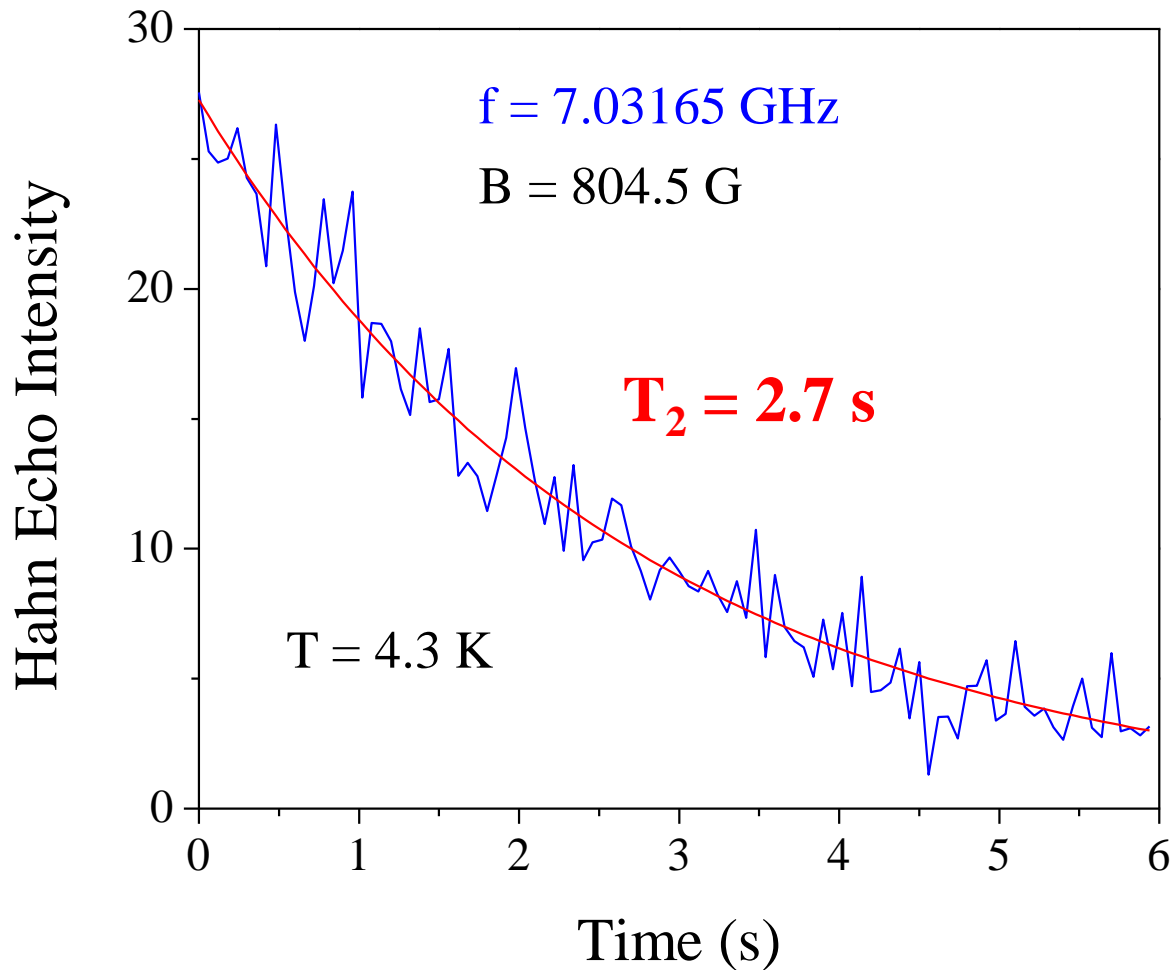


Clock Transitions for Si:Bi



Electron T_2 for ^{28}Si

$4 \cdot 10^{14} \text{ Bi/cm}^3$, 50 ppm ^{29}Si



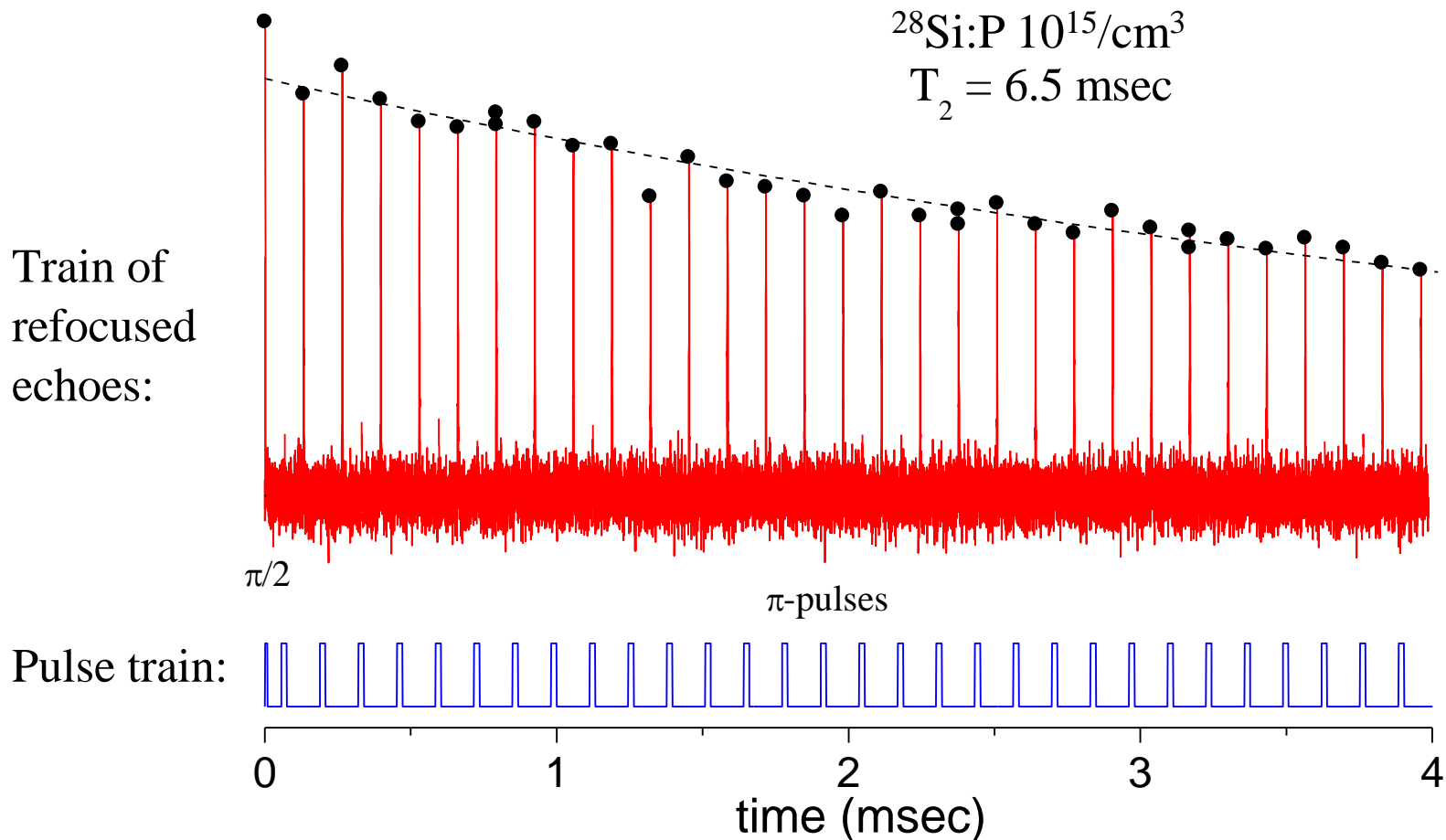
Dynamical Decoupling

- Hahn Echo ($\pi/2 - \tau - \pi - \tau - \text{echo}$) removes static and slow phase decoherence (frequencies $< 1/\tau$)
- So, just repeat
 - Carr-Purcell = $\pi/2 - \tau - \pi - \tau - \pi - \dots - \pi - \tau - \text{echo}$
 - Filters noise, only allowing noise at $\omega \sim 1/\tau$
[Biercuk J.Phys.B. 44,154002 (2011)]
- But, need to worry about pulse errors
 - CP = $\pi_x/2 - \tau - \pi_x - \tau - \pi_x - \dots - \pi_x - \tau - \text{echo}$
 - Pulse errors \Rightarrow echo dies off quickly
 - CPMG = Carr-Purcell-Meiboom-Gill (fix some errors)
= $\pi_x/2 - \tau - \pi_y - \tau - \pi_y - \dots - \pi_y - \tau - \text{echo}$

Carr-Purcell-Meiboom-Gill Sequence

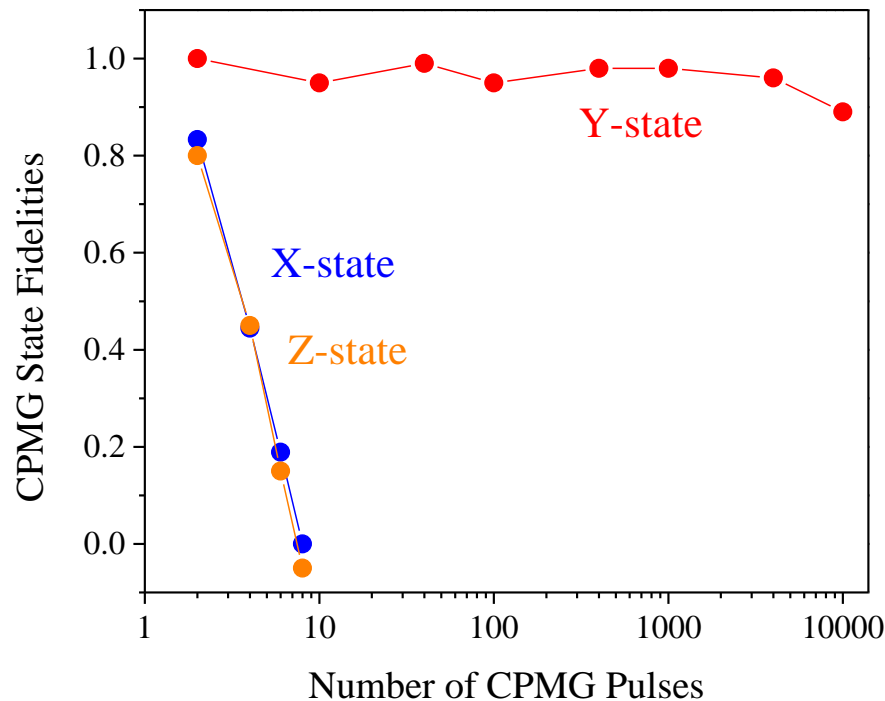
Refocus spins every $130\mu\text{s}$ (train of π -pulses) – decouples B-noise

\Rightarrow retain coherence for > 6 msec



Dynamical Decoupling with CPMG?

- Easy, just decouple noise with CPMG?
 - No, there's no free lunch
- CPMG preserves only one state

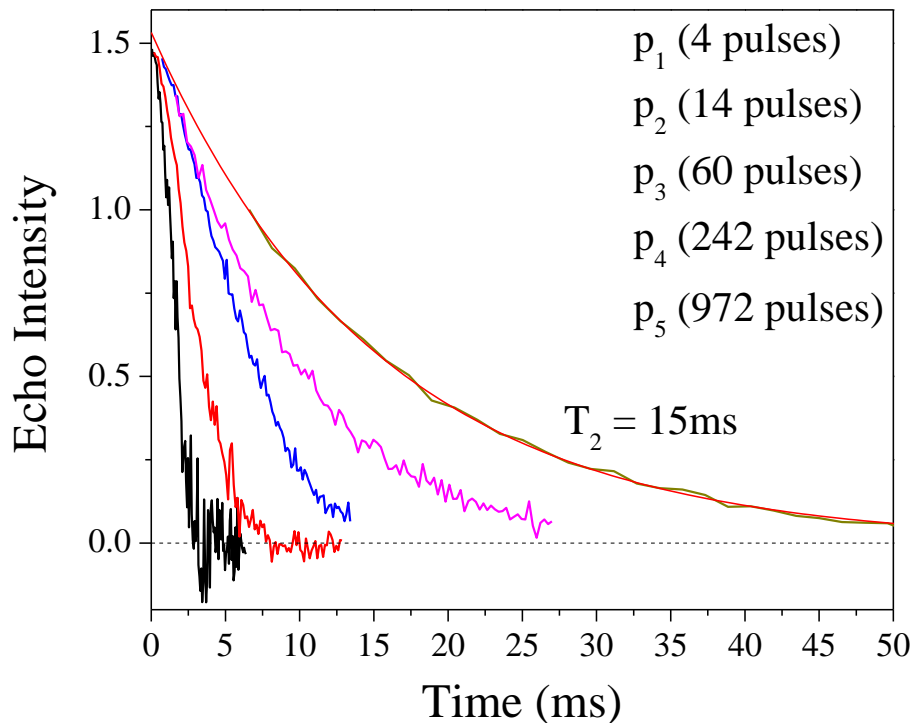


Better Dynamical Decoupling Sequences

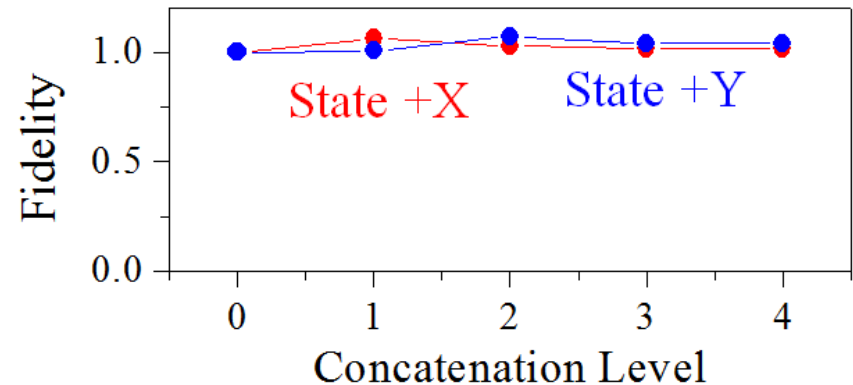
- Sequences made from XYXY are “good” (for spins):
 - Especially “concatenated” versions:

K. Khodjasteh, PRL **95**, 180501 (2005) & Wang, PRB **85**, 085206 (2012)

Concatenated XZXZ pulse sequence



Initial State Sensitivity:
XYXY sequence



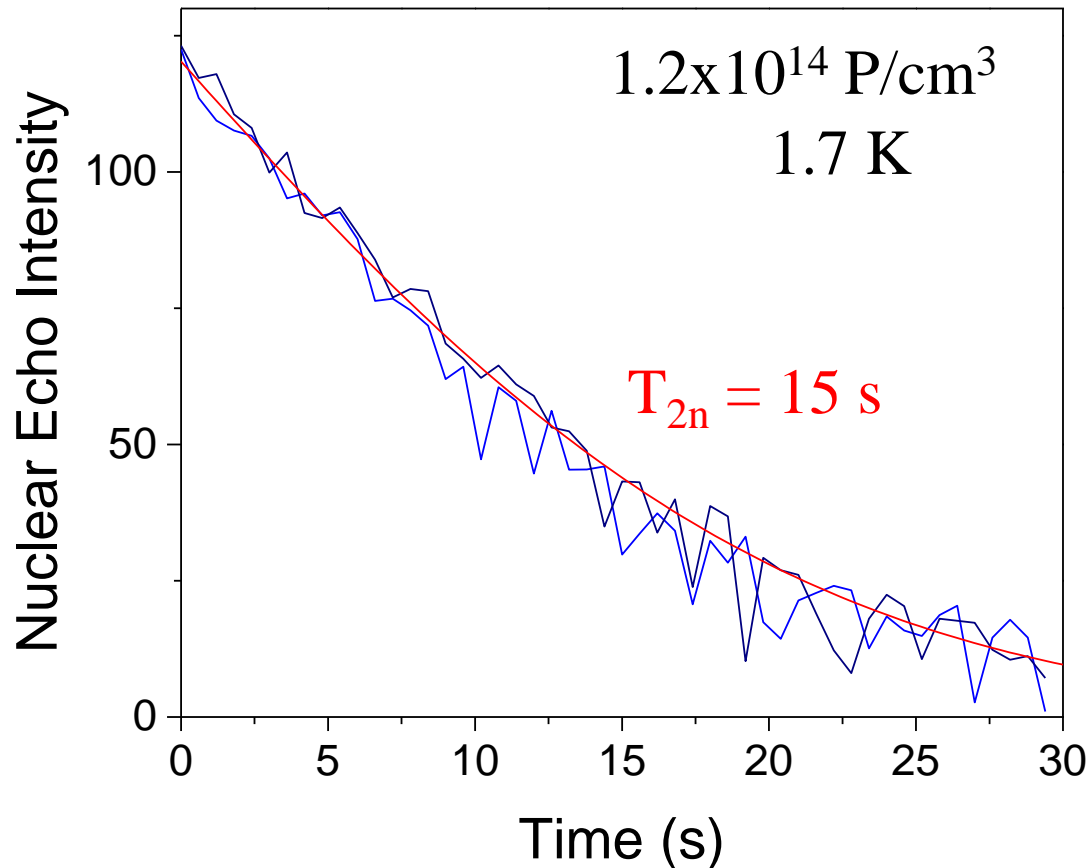
Dynamical Decoupling – Where are we?

- Dynamical decoupling is good for non-Markovian noise
 - Like $1/f$ noise
 - Errors that standard quantum error correction is bad at
- Dynamically makes a decoherence-free subspace
 - If spin is up and down half the time \Rightarrow insensitive to B_0
- Not known, in general, how to interleave DD and gates
 - Gates can be performed between repetitions of sequences
 - Must wait until concatenated sequence is complete
- CPMG is not useful dynamical decoupling for qubits
 - Does not protect general state
 - Pulse errors + dipolar interactions cause odd effects
 - Is useful for extending coherence of single QB's, but unclear what physics is being averaged out

What is the limit for donor electron spin T_2 in Si?

- We don't know
 - Our measurements are still limited by donor-donor interactions and residual ^{29}Si .
 - In most QC architectures, the donor-donor distance would be larger than we have
 - Expect $T_2 \gg 10$ s.
- Do we need it longer?
 - Bigger is better?
 - Many other effects in devices – surfaces and interfaces, gate voltages, ...

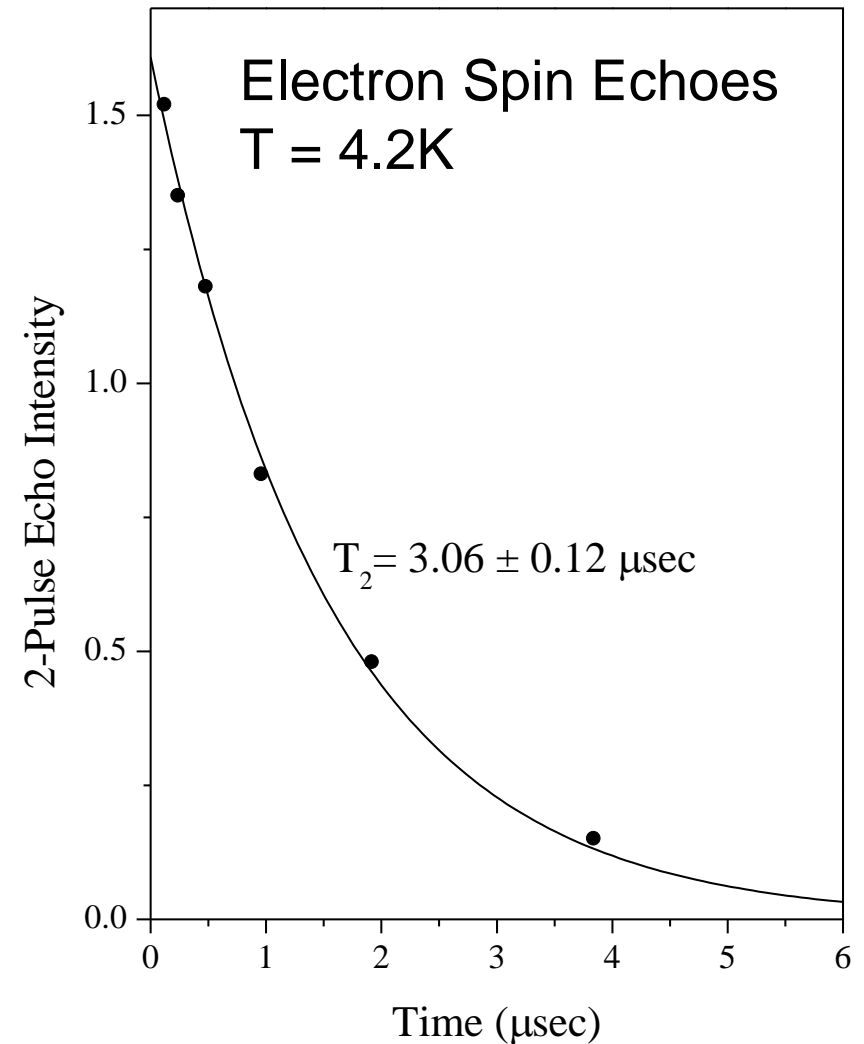
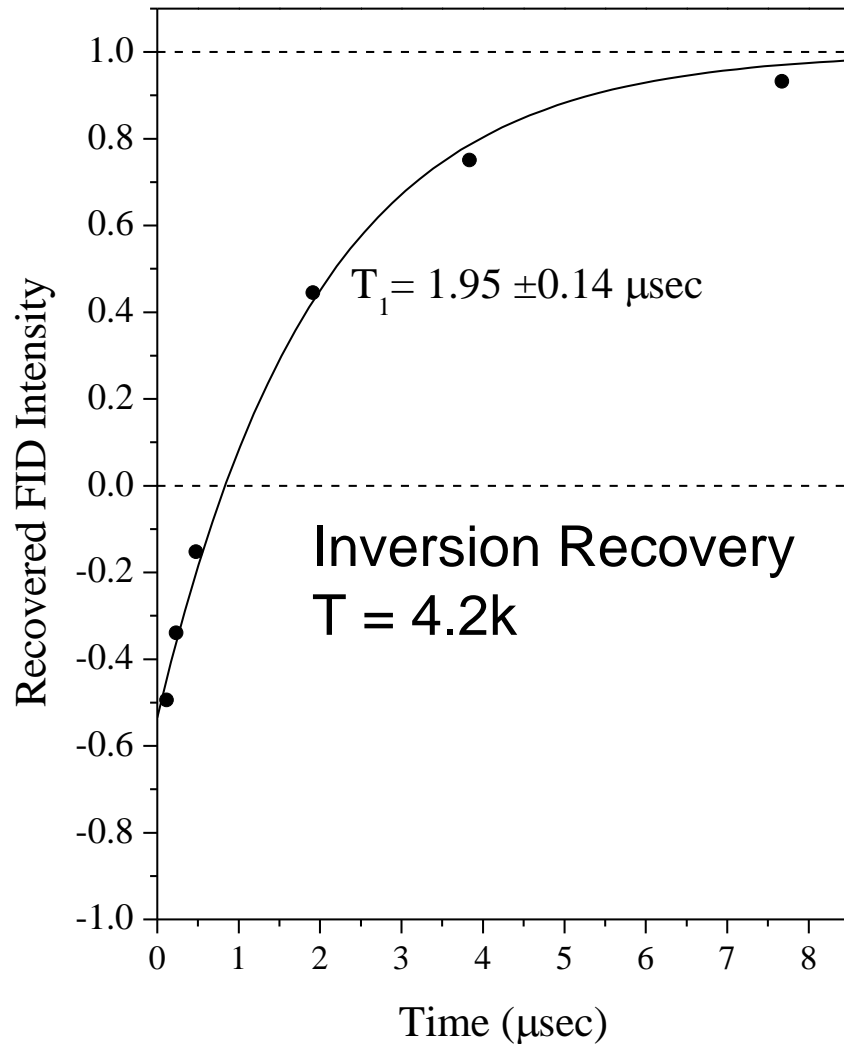
Nuclear T_2 in highly enriched silicon (~ 100 ppm ^{29}Si)



T_{2n} is limited by electron spin flip-flops.

Ionized donor nuclei $\Rightarrow T_{2n} \sim 3$ hr. Useful? Bigger is better?

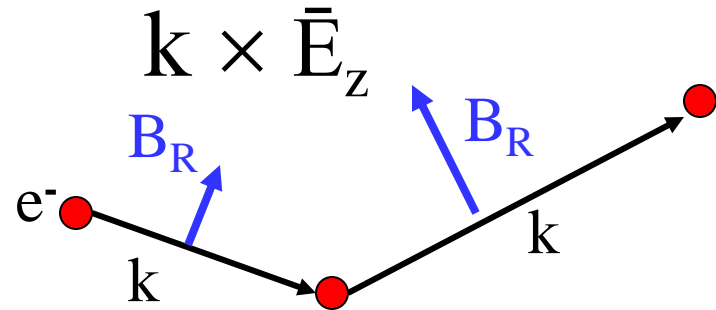
Mobile qubits? Free 2D Electron Spin Relaxation Times in Si/SiGe Heterostructure



Origin of the Spin Relaxation in 2D

- $T_2 > T_1$ requires anisotropic relaxation mechanism
- Abstractly, fluctuating B-fields cause relaxation
- Appears that fluctuating fields arise from Rashba effect (spin-orbit interaction from broken symmetry at interface):

$$H_R = \alpha \underbrace{(\bar{k} \times \bar{E})}_{\mathbf{B}_R} \cdot \hat{S}$$



- Use correlation time, $\tau_c = 10$ psec (from mobility)
 - In-plane fields $(B_x, B_y) = 10$ Gauss
 - Perpendicular $(B_z) = 5$ Gauss

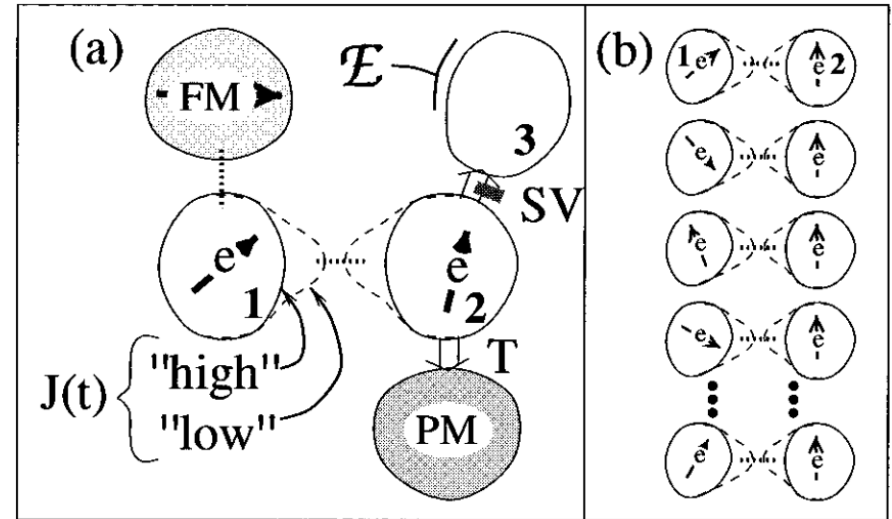
Outline

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- Spin resonance measurements of spin coherence in Si
- GaAs quantum dot spin experiments
- Si quantum dot spin experiments
- Si donor spin experiments
- Other schemes (electrons on helium, ...)

1998: Two proposals

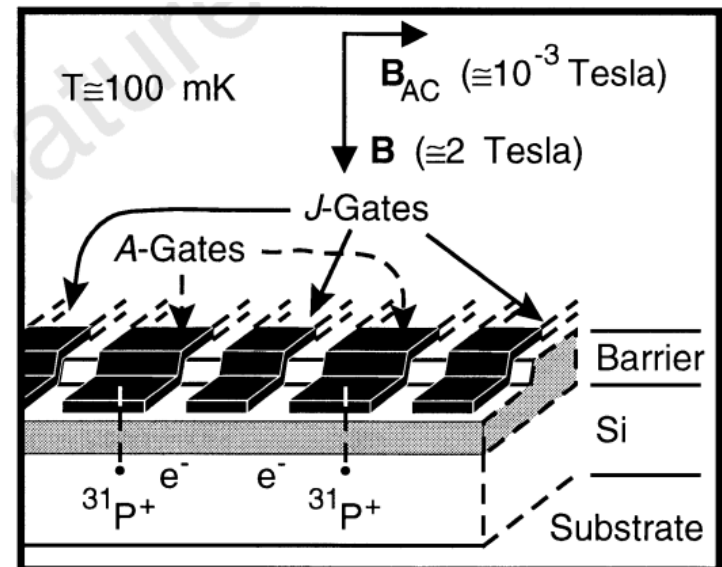
1. Loss & DiVincenzo,
PRA **57**, 120 (1998)

- Quantum dots



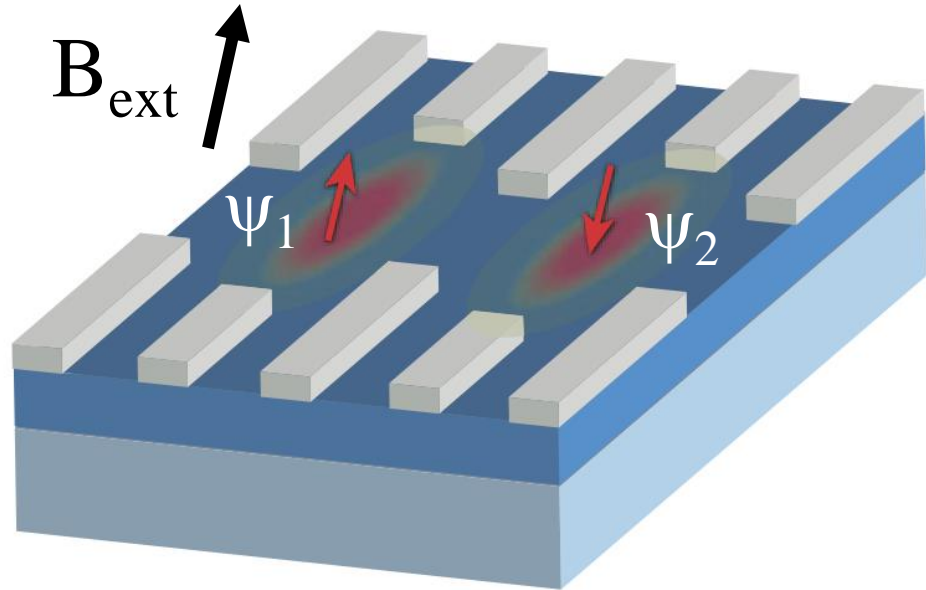
2. Kane, Nature **393**, 133
(1998)

- Donor impurities in Si

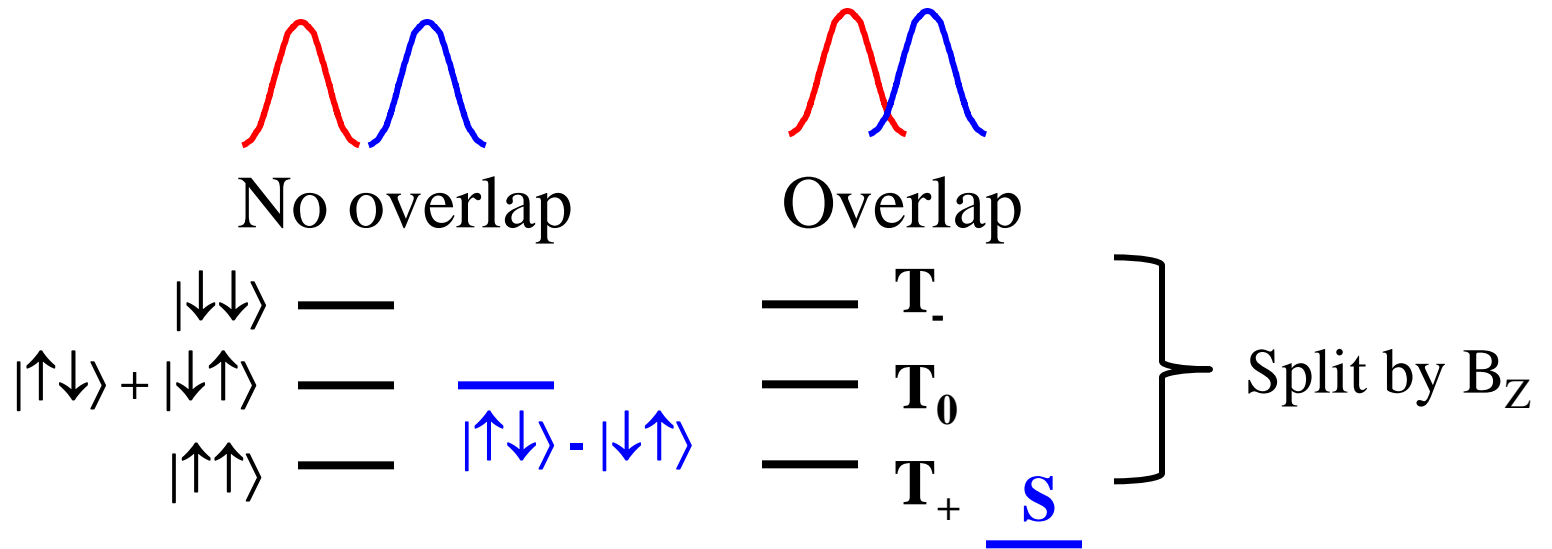


Electrons in quantum dots

- Gates (white) hold electrons (red) in dots
- Electrons assumed to be held at interface between light and dark materials (unspecified)
- Use gate voltages to cause ψ_1 and ψ_2 to overlap \Rightarrow exchange interaction (J)



Exchange gates



- $H_J \sim J\mathbf{S}_1 \cdot \mathbf{S}_2$
- In $B_Z \Rightarrow S_X, S_Y$ mix $|0\rangle$ & $|1\rangle$
 - Mixture oscillates at ω_Z
- $\Rightarrow H_J \sim JS_{1z} \cdot S_{2z}$

Exchange \rightarrow CPHASE

- $H_J \sim JS_{1z} \cdot S_{2z}$

$$\Rightarrow H_J(\alpha) = \begin{pmatrix} e^{-i\alpha} & 0 & 0 & 0 \\ 0 & e^{i\alpha} & 0 & 0 \\ 0 & 0 & e^{i\alpha} & 0 \\ 0 & 0 & 0 & e^{-i\alpha} \end{pmatrix}$$

$$R_{1z}(2\alpha) = \begin{pmatrix} e^{i\alpha} & 0 & 0 & 0 \\ 0 & e^{i\alpha} & 0 & 0 \\ 0 & 0 & e^{-i\alpha} & 0 \\ 0 & 0 & 0 & e^{-i\alpha} \end{pmatrix}$$

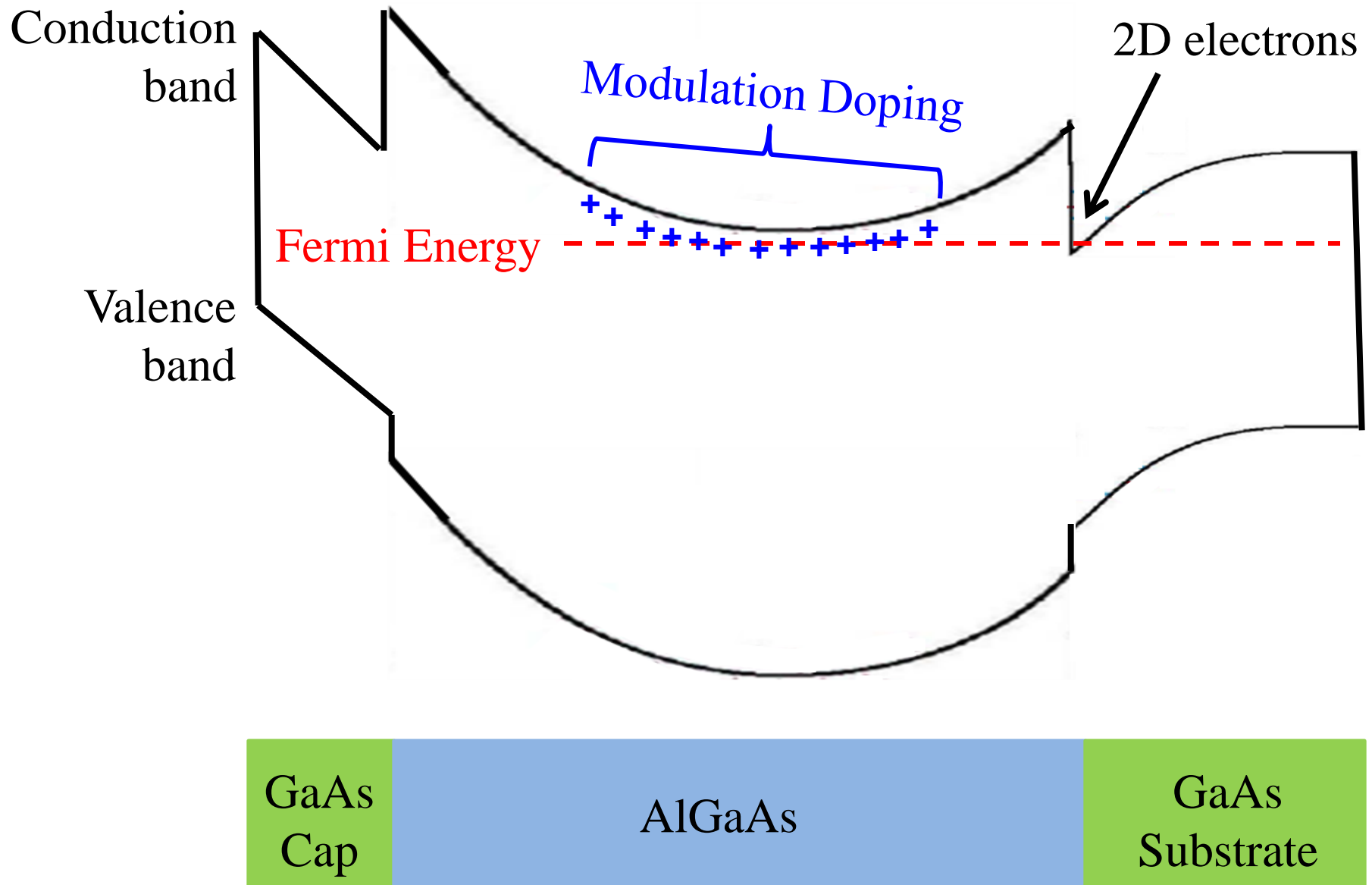
$$R_{2z}(2\alpha) = \begin{pmatrix} e^{i\alpha} & 0 & 0 & 0 \\ 0 & e^{i\alpha} & 0 & 0 \\ 0 & 0 & e^{-i\alpha} & 0 \\ 0 & 0 & 0 & e^{-i\alpha} \end{pmatrix}$$

$$H_J(\pi/4) R_{1z}(\pi/2) R_{2z}(\pi/2) = e^{i\pi/4} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix} = \text{CPHASE}$$

Quantum dot jargon

- Solution-grown **nanocrystal** quantum dots
 - Typically less than 10 nm in size
 - Coated with organic ligands
- **Self-assembled** quantum dots
 - Typically less than 20 nm across, and a few nm thick
 - Formed during growth by Molecular Beam Epitaxy
- **Vertical** quantum dots
 - Few x 100 nm pillars etched into multilayer GaAs/AlGaAs
 - Have been used to study electron spins
- **Lateral** or **gate-defined** quantum dots
 - Typically 100's of nm across
 - Start with 2D electron heterostructure
 - These are the main dots we want to use

GaAs/AlGaAs Heterostructures



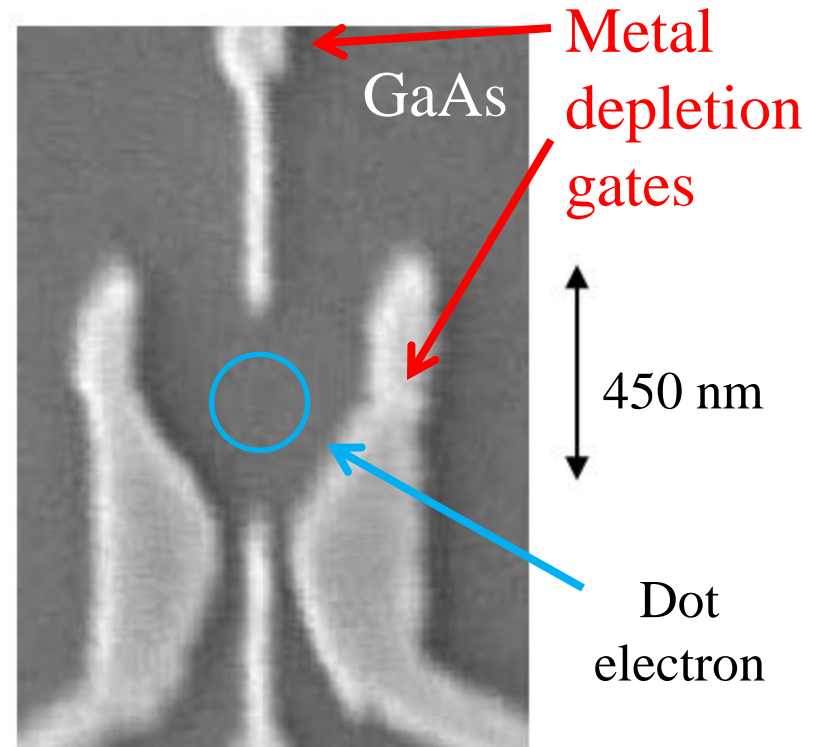
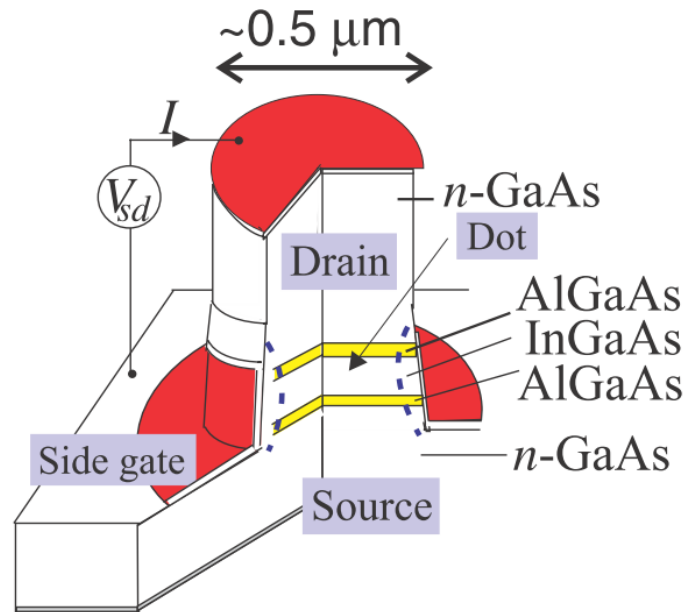
Properties of GaAs/AlGaAs

- Nearly defect-free interfaces
 - Reduce electron density to $\sim 10^{10}/\text{cm}^2$ before charges trap (\Rightarrow 100nm between electrons)
- Single conduction band valley
- Small effective mass ($m^* \sim 0.07 m_0$)
 - Small mass means large energy splitting (for spatial part of ψ), even in a large device
 - Approximately harmonic potential $\Rightarrow \Delta E \sim 1/\sqrt{m^*}$
- Little leakage for Au gates on GaAs cap

- Charge motion in doping layer can cause noise
- No stable isotopes with zero nuclear spin
 - As: 100% ^{75}As ; Ga: 60% ^{69}Ga , 40% ^{71}Ga ; all with $I = 3/2$

Single quantum dot structures

Vertical dot



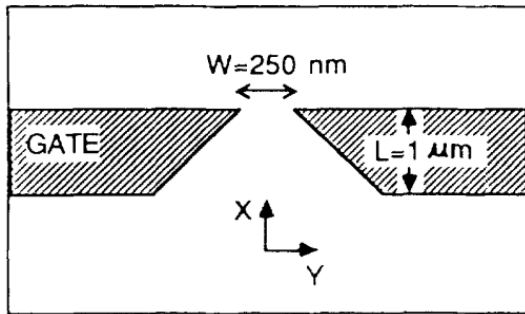
Kouwenhoven, Rep. Prog. Phys. **64**, 701 (2001)

Ciorga, PRB **61**, 16315 (2000)

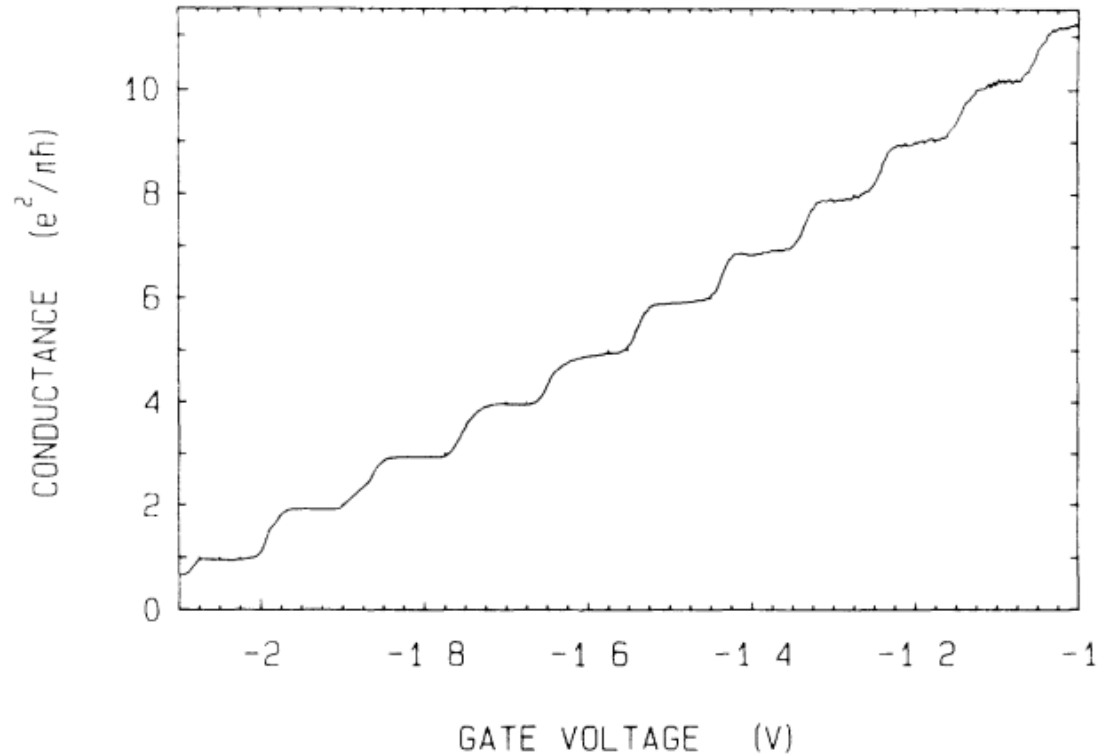
For Both

- Size of dot can be controlled by side gate(s)
- Must pass current through dots to measure

Quantum point contacts (QPC)



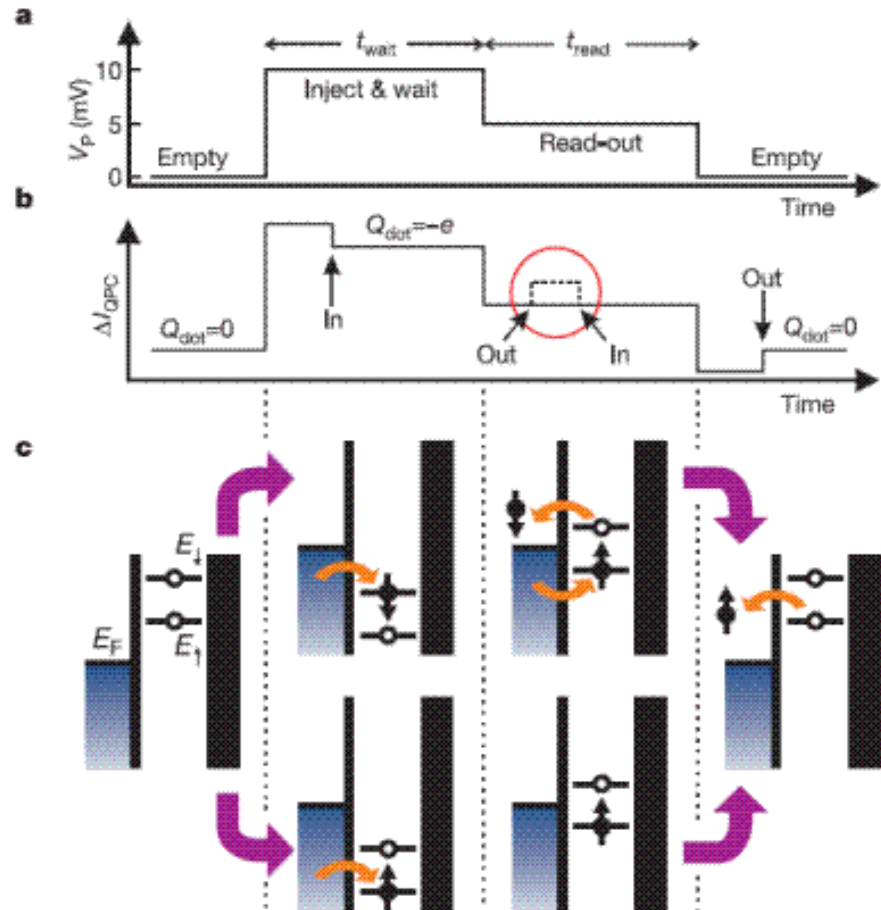
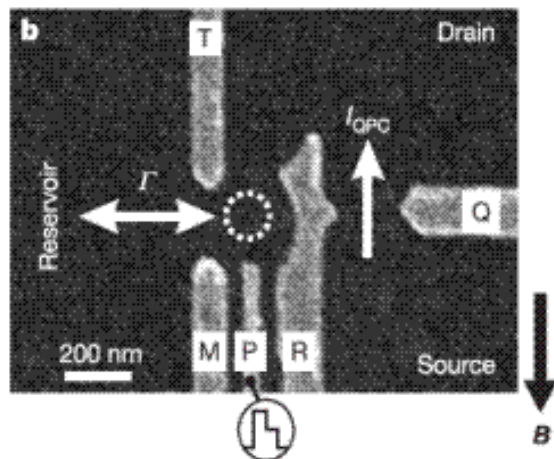
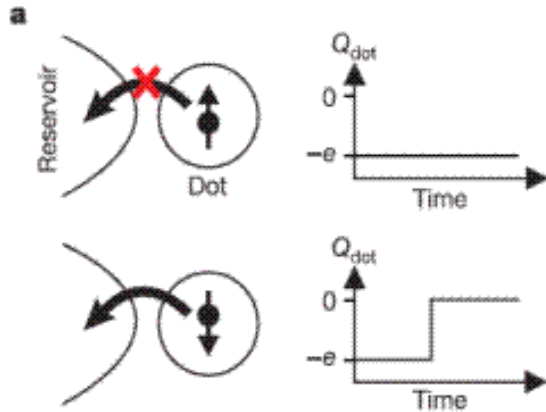
Narrow channel acts as electron waveguide. Step increase in current when new mode becomes available



van Wees, PRL **60**, 848 (1988)

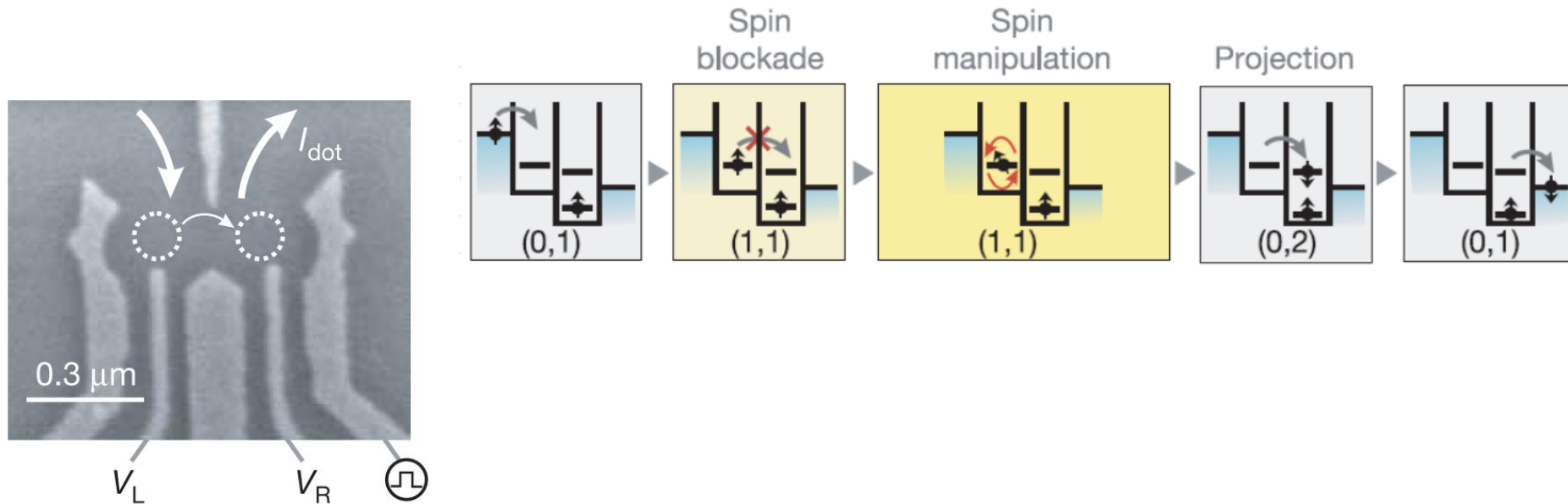
A QPC forms a very high-gain detector of electric fields (or charge). M. Field showed that single electrons can be detected - Field, PRL **70**, 1311 (1993)

Single dot spin measurement



Need large spin splitting ($g\mu_B B \gg kT_e$)

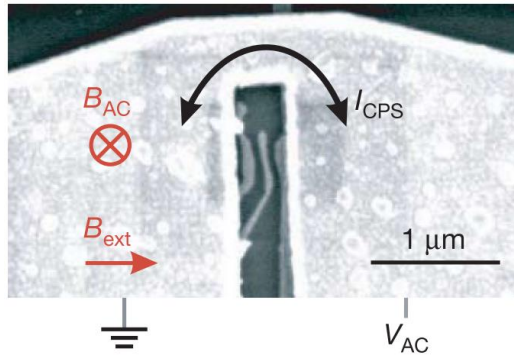
Spin blockade in double quantum dot



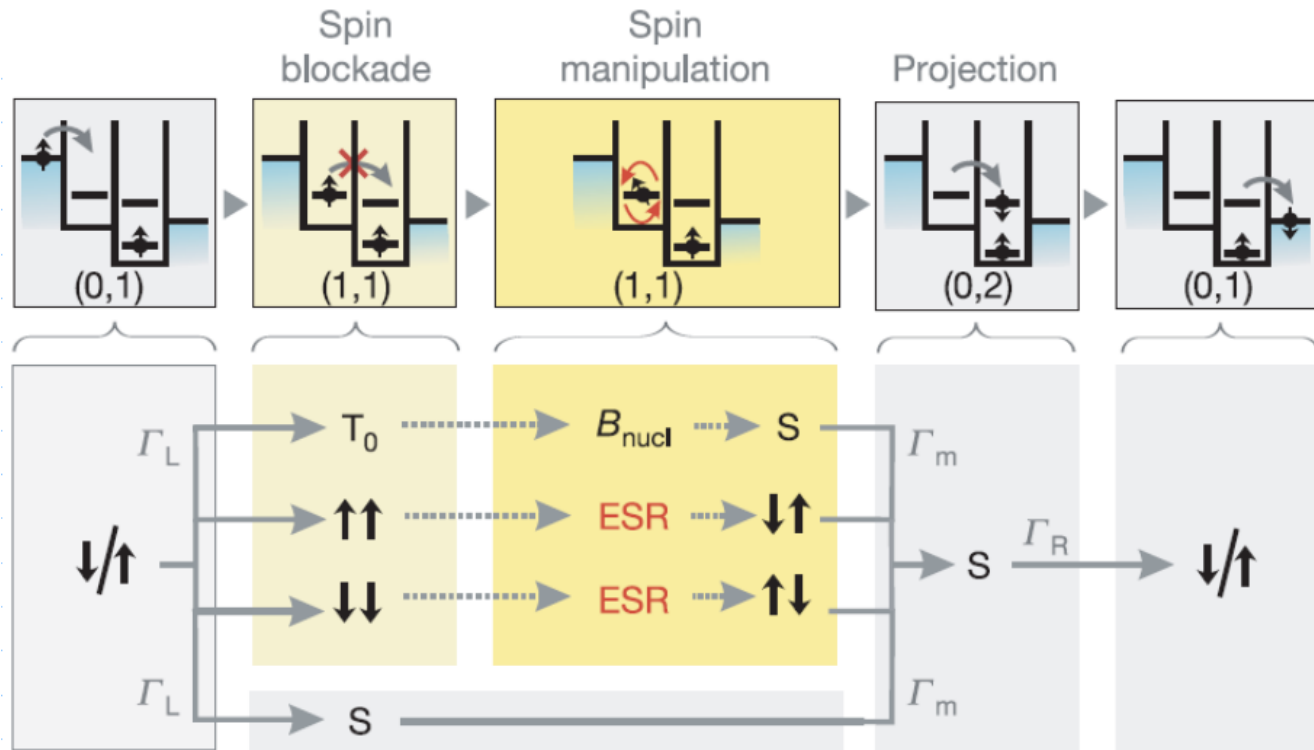
Singlet-Triplet splitting can be $\gg kT$, meaning electron can only move from left to right dot if the two form a singlet

Koppens, et al. Nature **442**, 766 (2006)

Single spin electron spin resonance (ESR)



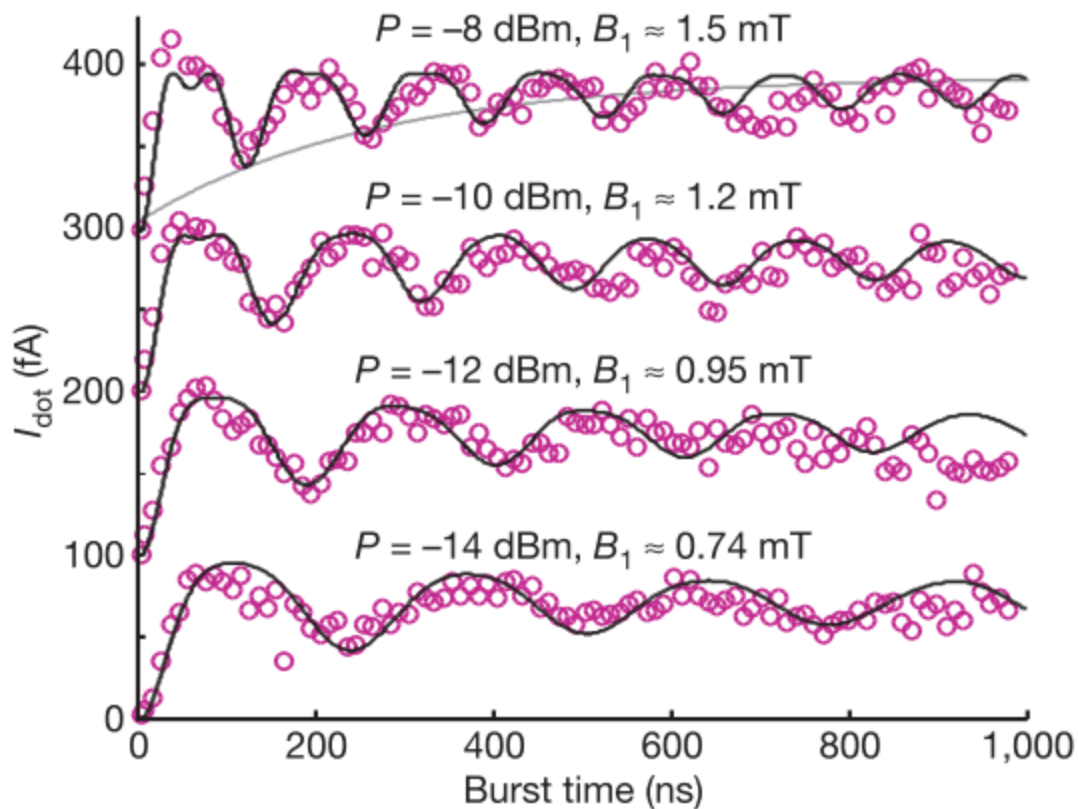
Quantum dot covered with large co-planar strip microwave guide. Shorting waveguide gives maximum B and minimum E at the dots.



Rotating a spin with the microwaves can lift the blockade by converting triplets into singlets (middle two lines)

Koppens, et *al.* Nature **442**, 766 (2006)

Single spin coherence

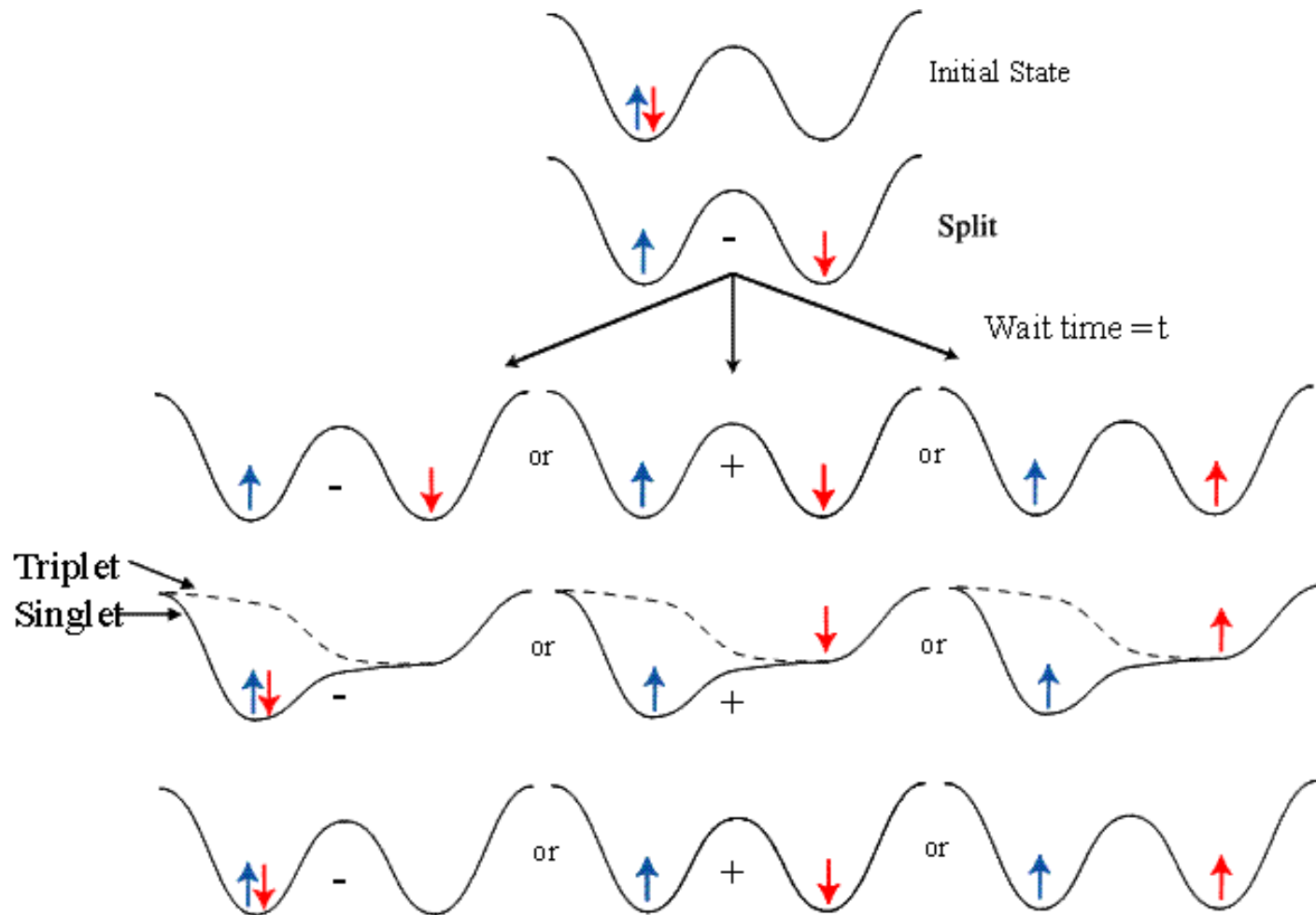


Current increases, as triplet probability increases, then decreases as spin rotates past the optimal point to form singlets. Oscillations decay non-exponentially, but conclude $T_2 \sim 500 \text{ ns}$.

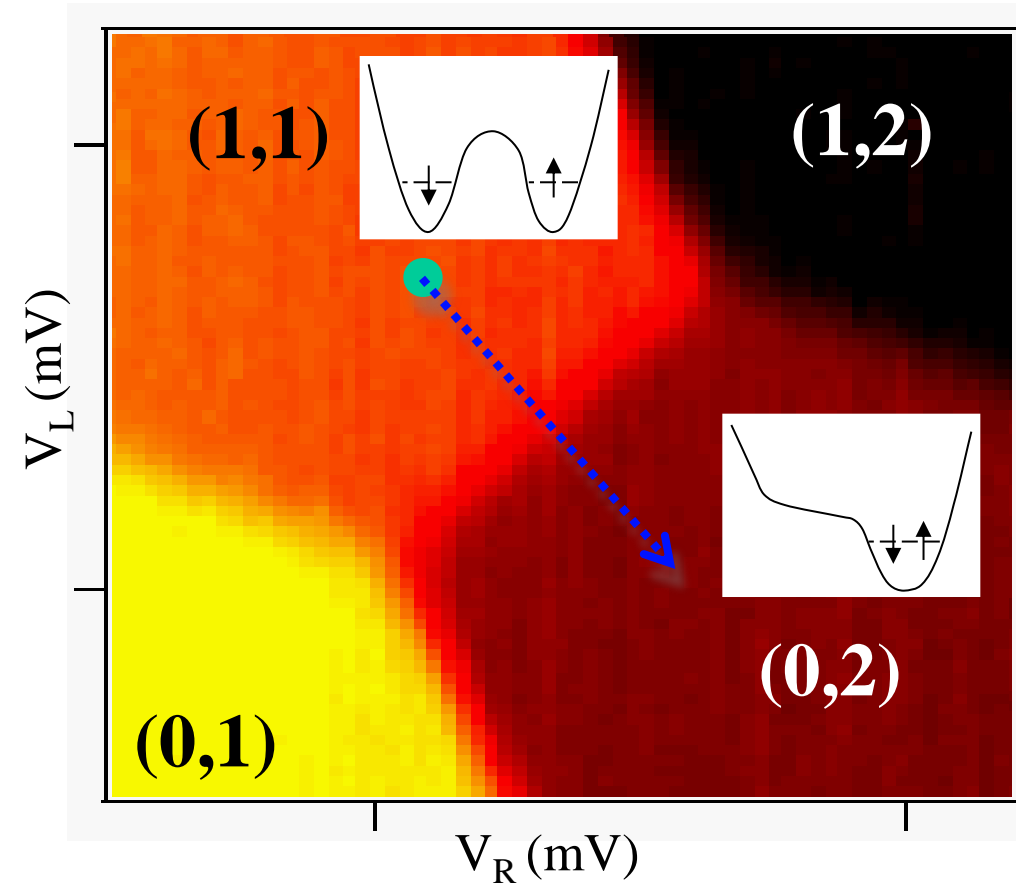
Koppens, et al. Nature **442**, 766 (2006)

Double Dot Spin “Coherence”

nonlocal, since two electrons are in different dots

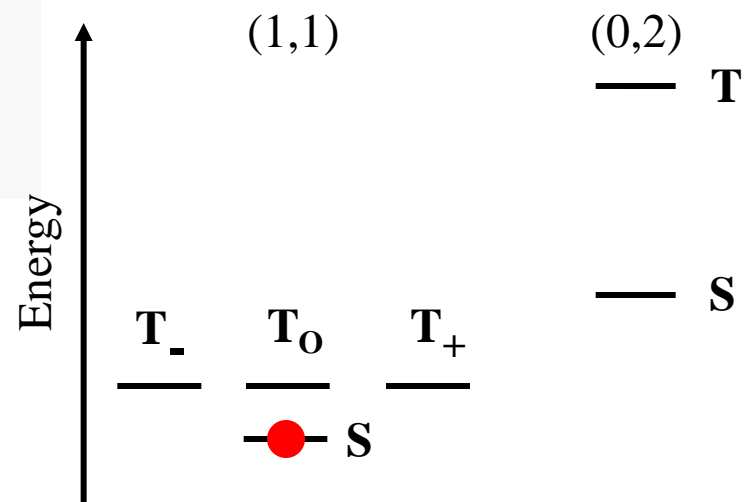
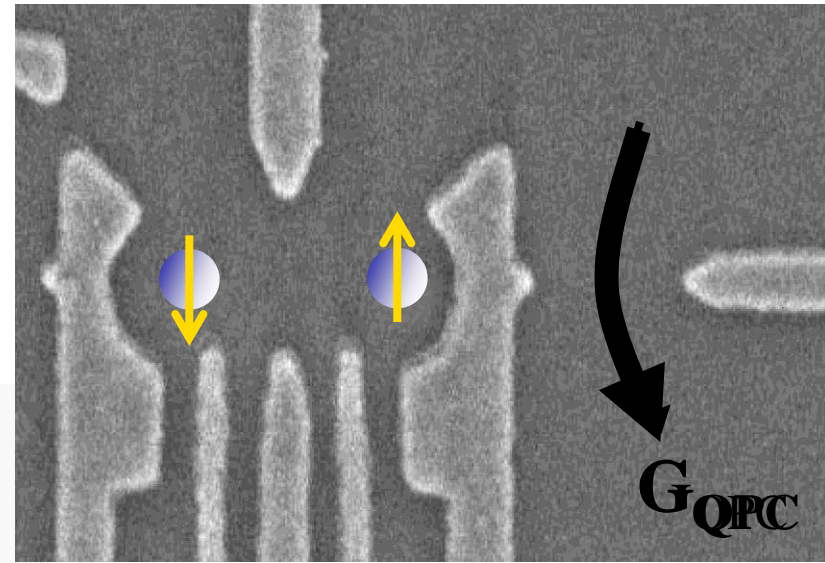


Spin state measurement (spin-to-charge conversion)

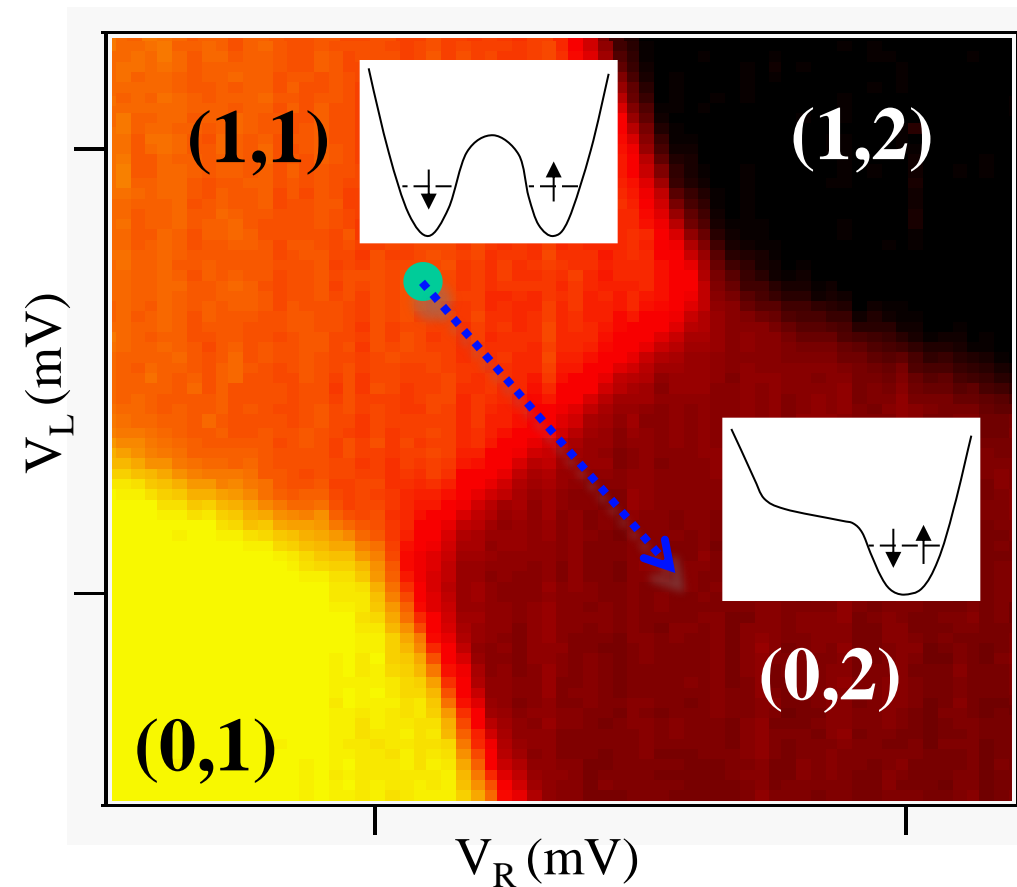


Singlet measurement

Petta, Science **309**, 2180 (2005)

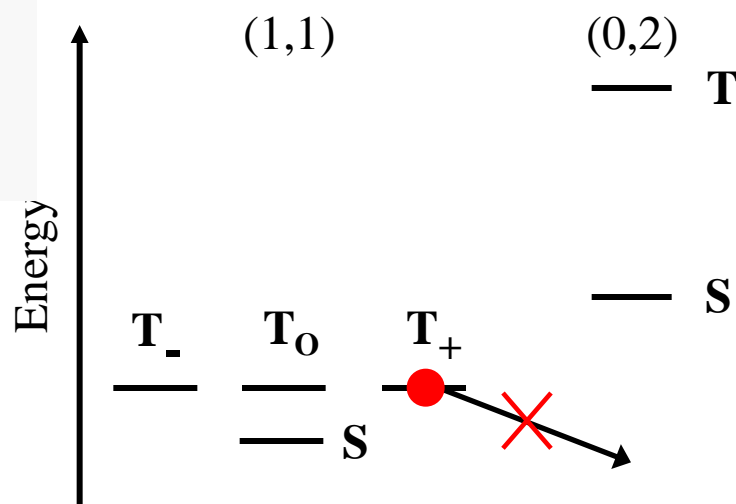
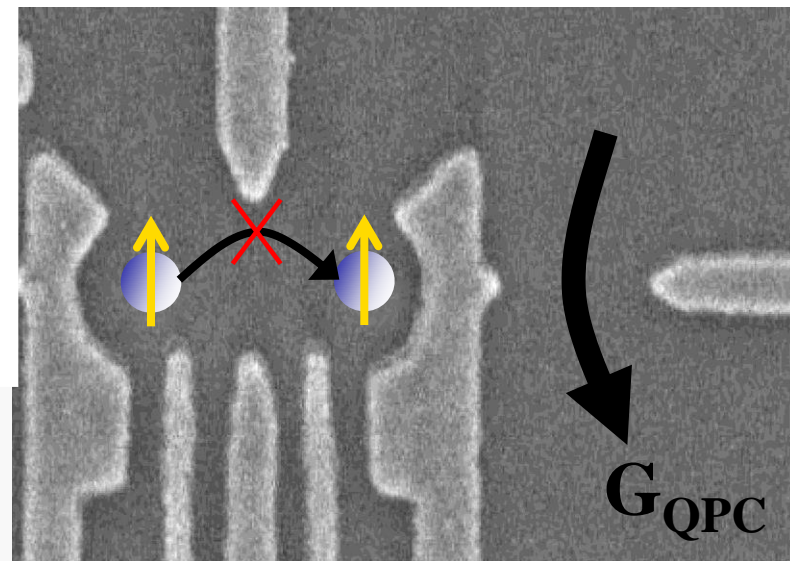


Spin state measurement (spin-to-charge conversion)

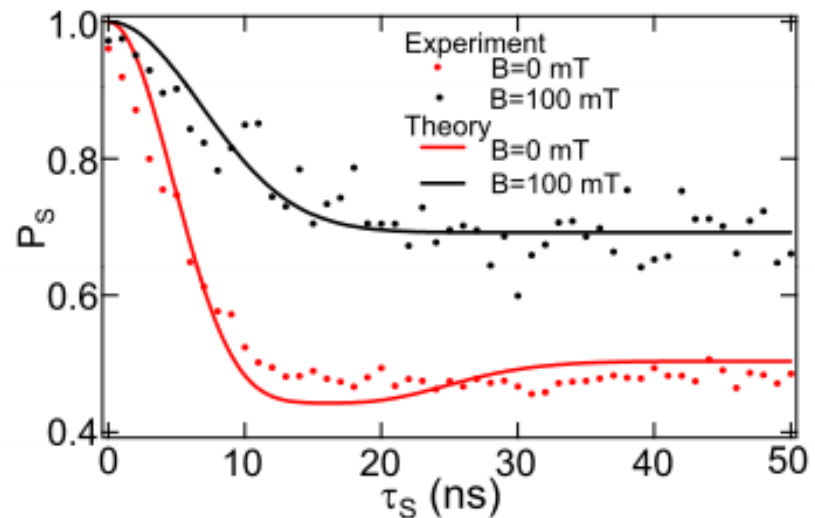
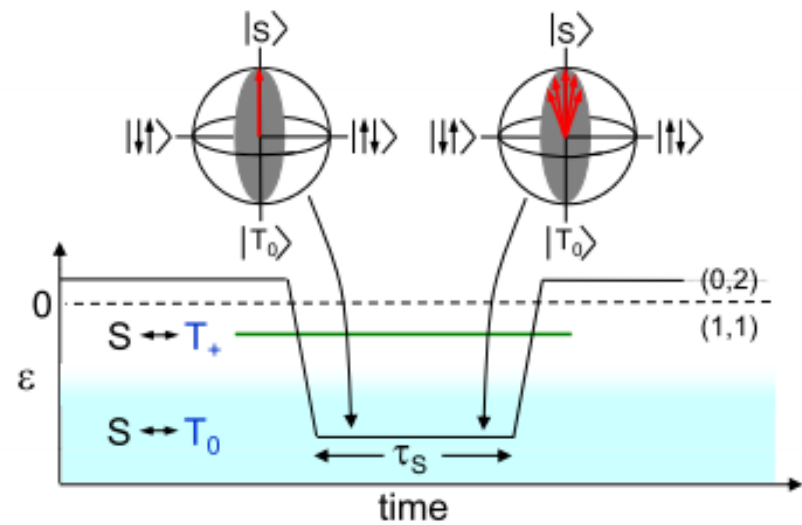
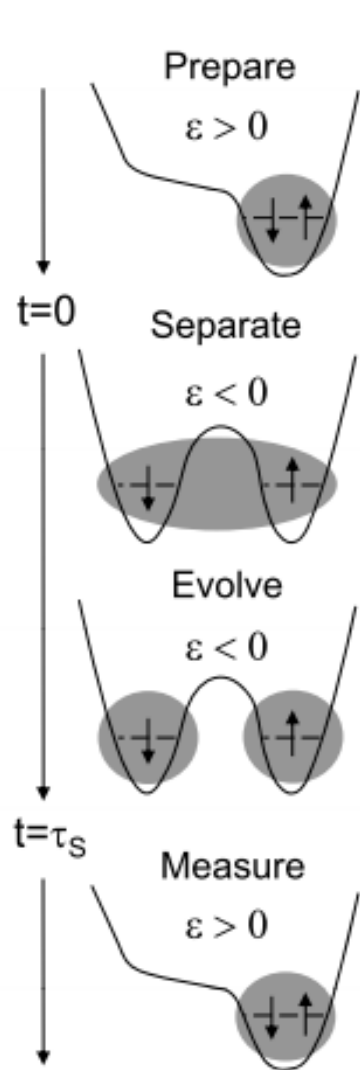


Triplet measurement

Petta, Science **309**, 2180 (2005)



Dephasing of the singlet spin state: T_2^* measurement



$B_{\text{nuc}} = 2.3$ mT and $T_2^* = 10$ ns

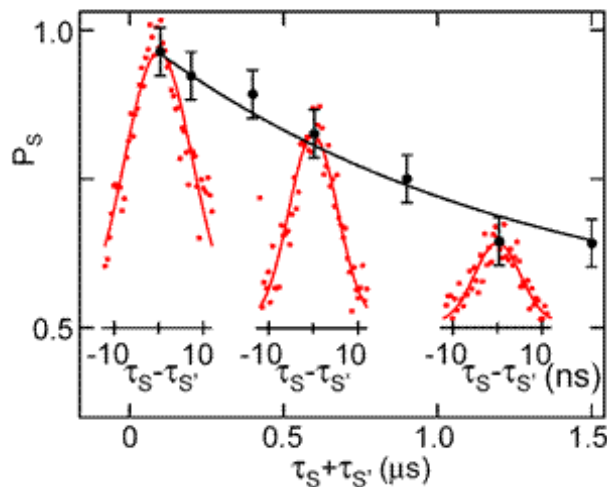
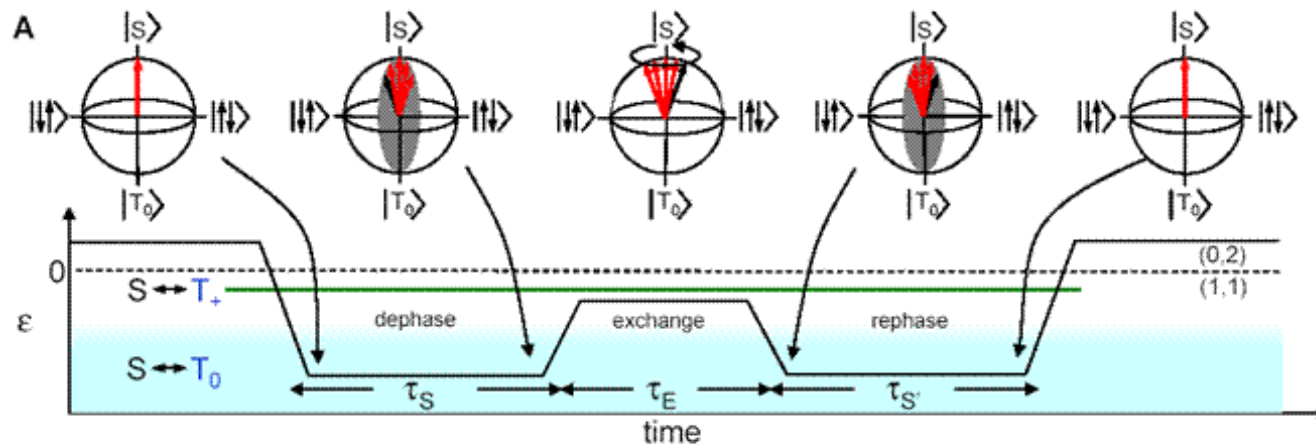
Petta *et al.*, Science **309**, 2180 (2005).

Different effective nuclear fields in the two dots (T_2^* not T_2)

Singlet/Triplet Qubits

use 2 electrons to make 1 qubit

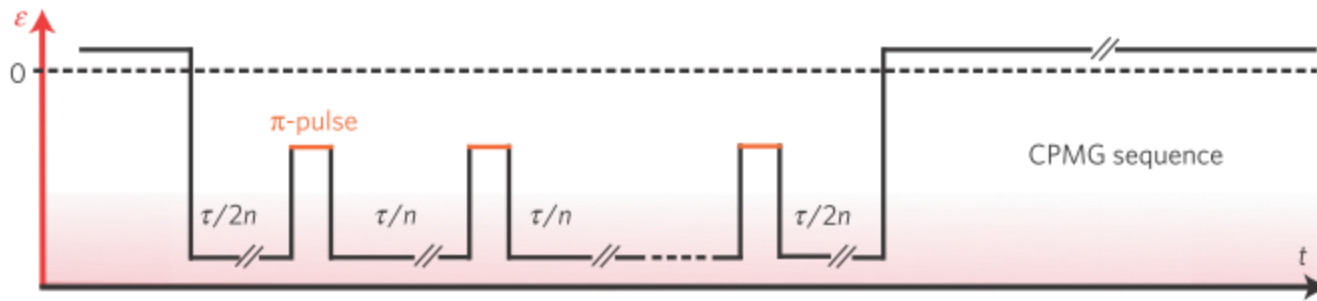
“Spin echo” $\Rightarrow T_2$ (decoherence)



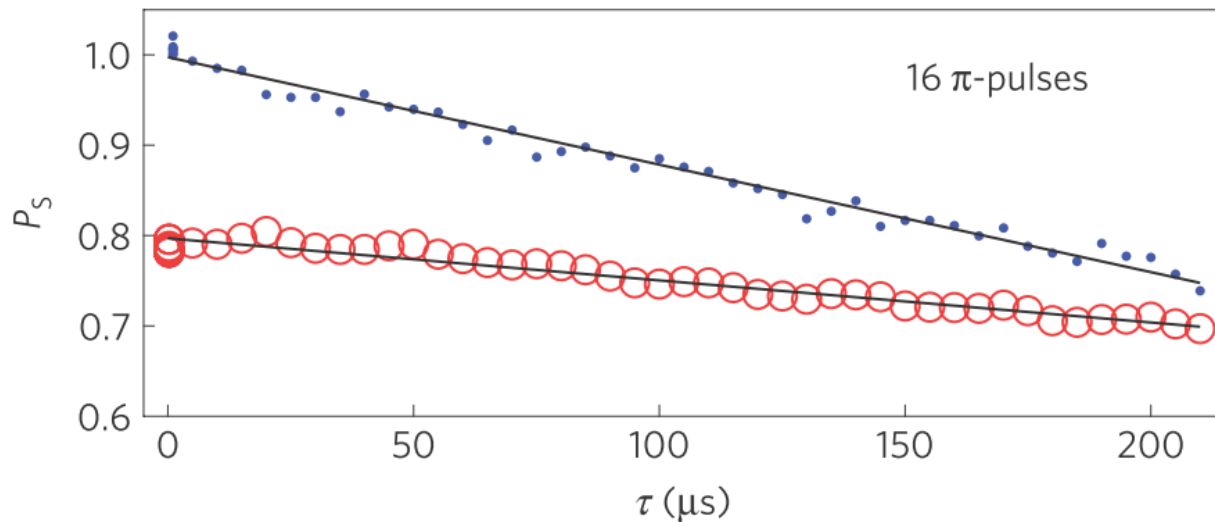
$\Rightarrow T_2 \sim 1 \mu\text{s}$

Note: All done at $< 100\text{mK}$, but tried it at 300mK and works just as well

Extending coherence – dynamical decoupling



Red is reference.
Difference
represents the
loss of coherence



Coherence can be extended to $> 200 \mu\text{s}$ with CPMG

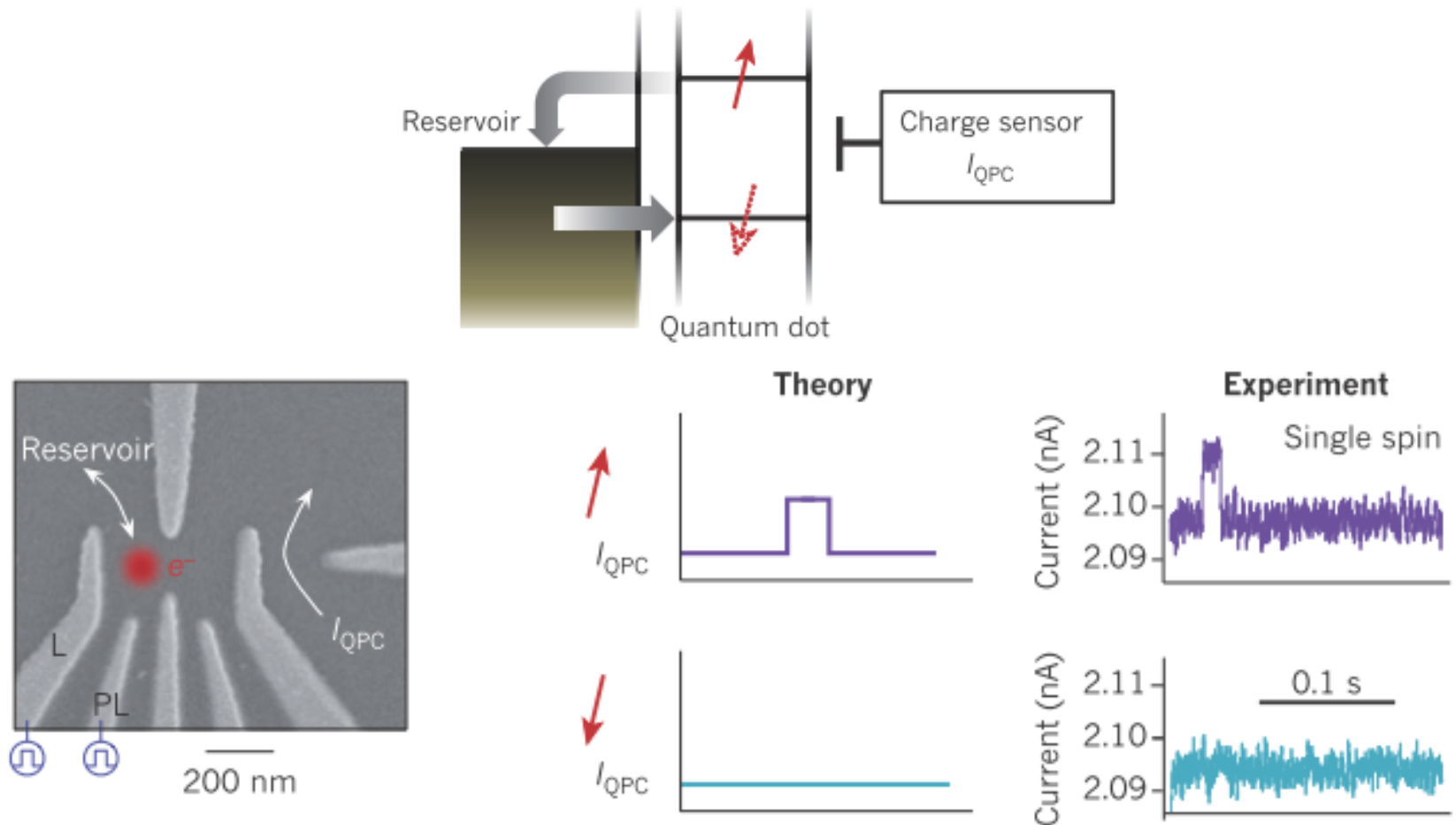
Where are GaAs/AlGaAs dots?

- Qubits
- Singlet-Triplet pairs in double QD (DQD)
- 1 and 2 qubit gates
- Two DQD's dots have been coupled
- Decoherence
- $\sim 200 \mu\text{s}$ with decoupling
- Initialization
- Just freeze into ground state
- Measurement
- Use QPC and spin blockade

What about Si QD's?

- Low density of non-zero spin nuclei (4.75% ^{29}Si), and isotopically enriched ^{28}Si is available
- Medium $m^* \sim 0.2 \Rightarrow$ need smaller dots than for GaAs
- Multiple conduction band valleys could cause complications
- Si/SiGe heterostructures are analogous to GaAs/AlGaAs structures, but more difficult to grow and still somewhat lower mobility (if that matters?)

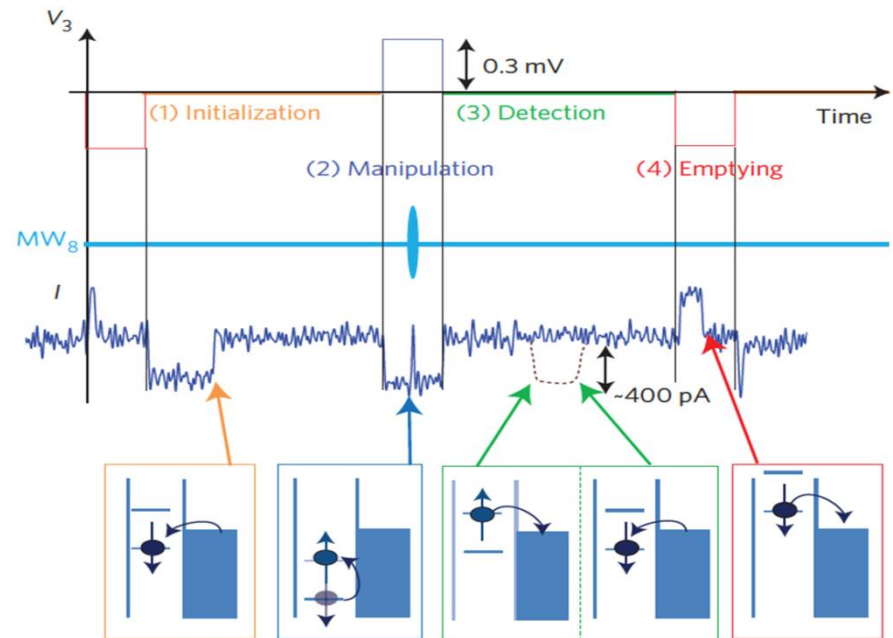
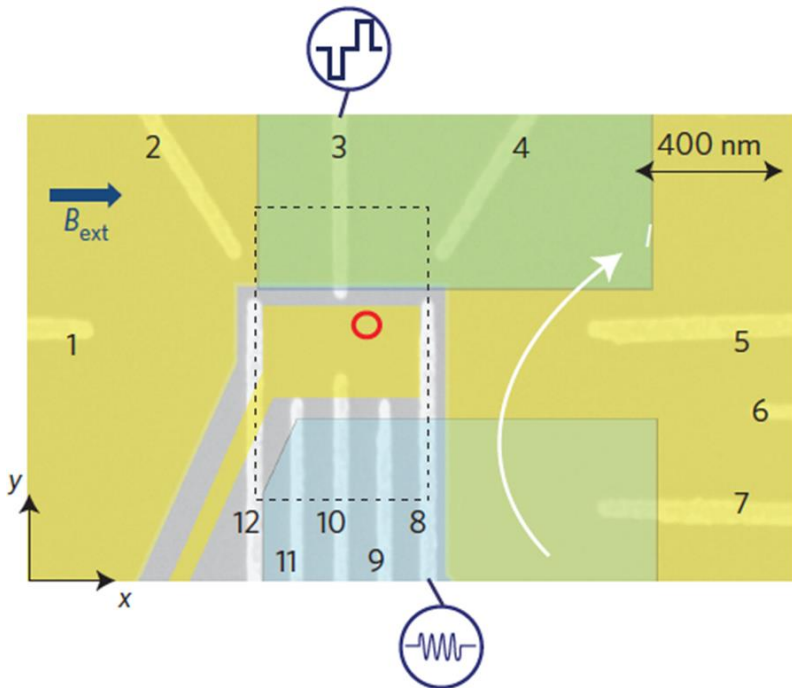
Spin measurement with Si/SiGe QD



Here the spin was measured “single shot” rather than signal averaging over many electrons

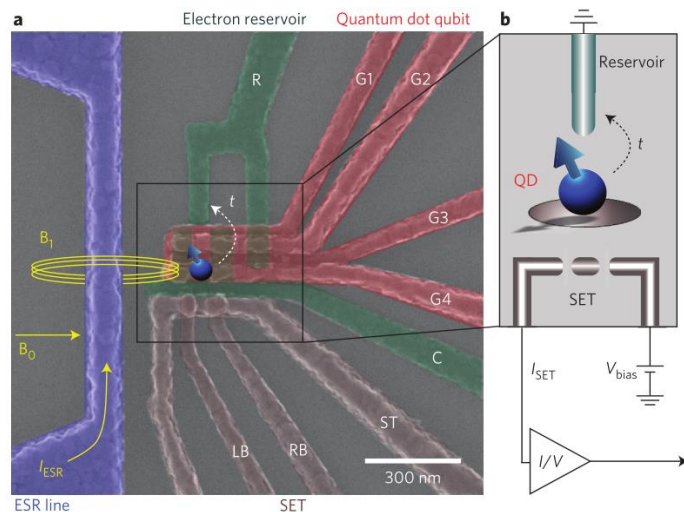
Driving Spin Electrically in ^{nat}Si/SiGe

- Microwave B-fields often (low-power) spread out $\sim \lambda$
 - Electric fields better confined
- ⇒ Address individual dot/electron
- Results: $T_2^{\text{Hahn}} \sim 70\mu\text{s}$, $T_2^{\text{XY8x16}} \sim 400\mu\text{s}$ (extra charge noise)
 - Gate fidelity $\sim 98 - 99\%$

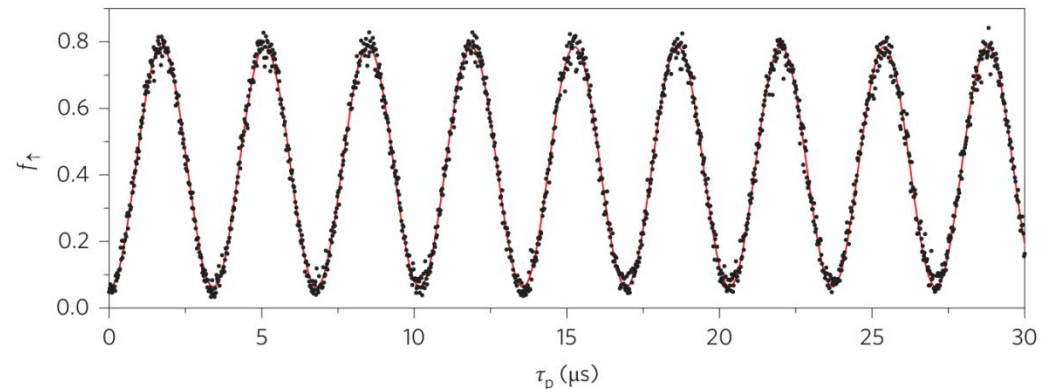


^{28}Si MOS Quantum Dots

- Metal-oxide-Si (MOS) is close to Si industry
- ^{28}Si eliminates decoherence from nuclear spins

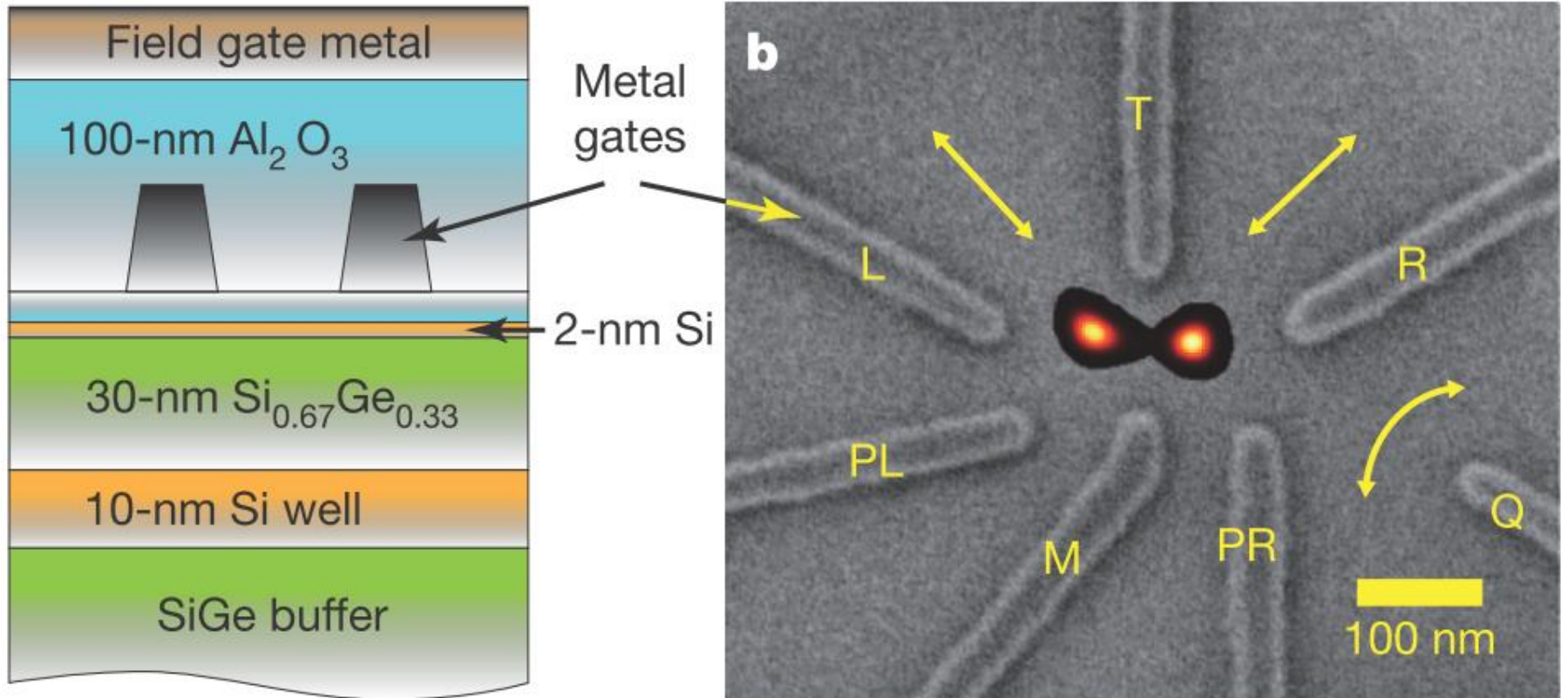


Rabi oscillations



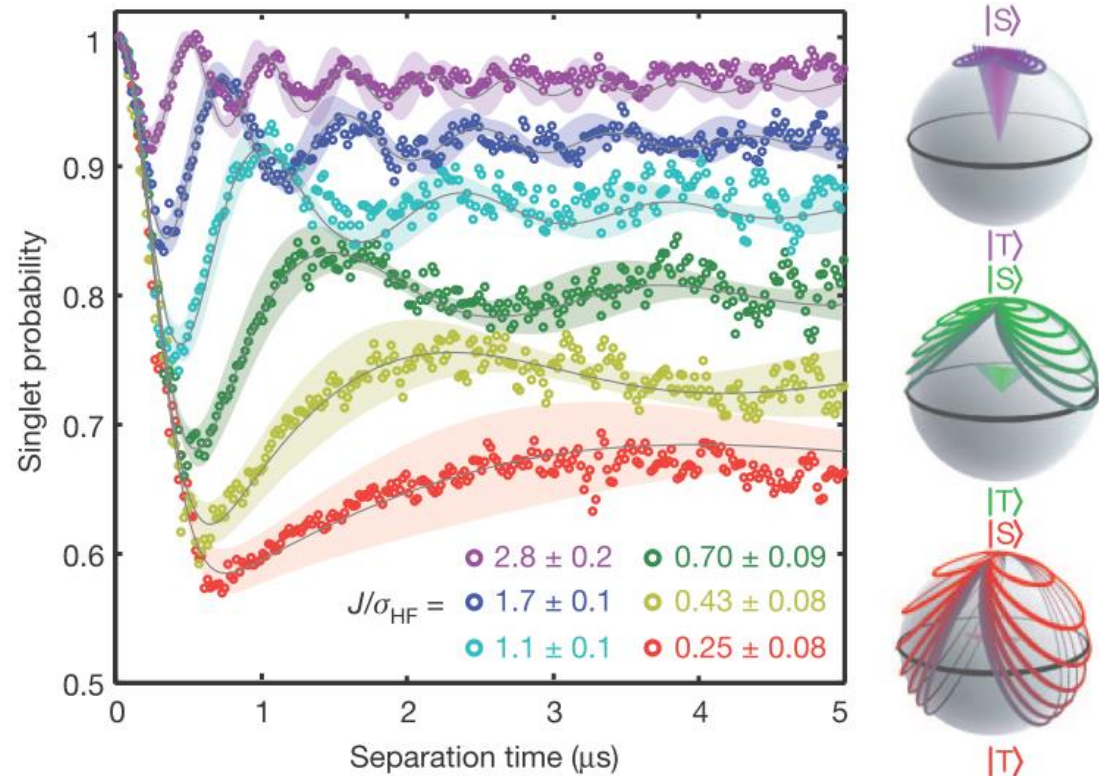
- Results: $T_2^* \sim 120 \mu\text{s}$ (Ramsey fringe)
 $T_2^{\text{Hahn}} \sim 1.2 \text{ ms}$ (Ramsey echo)
 $T_2^{\text{CPMGx500}} \sim 28 \text{ ms}$
- Gate fidelities $\sim 99.2\% - 99.9\%$

Undoped Si/SiGe double quantum dot



Maune, Nature, **481**, 344 (2012)

T_2^* in $^{\text{nat}}\text{Si}$ double quantum dot



Find $T_2^* \sim 350$ ns

Couldn't make J small enough for whole Bloch Sphere

Do we **need** singlet-triplet qubits in Si?

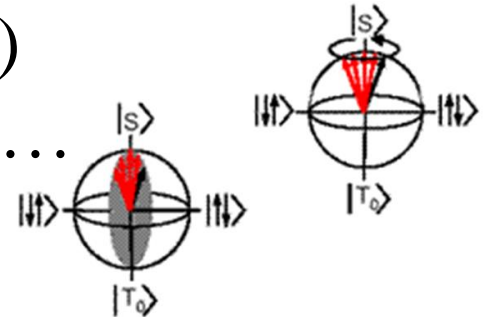
➤ No

- T_2 with just Hahn echo is longer than GaAs S-T qubit
- World's best ^{28}Si (50 ppm) and similarly enriched Ge might make $T_2^* \sim 10 \mu\text{s}$
 \Rightarrow need dynamical decoupling and limited by gate noise

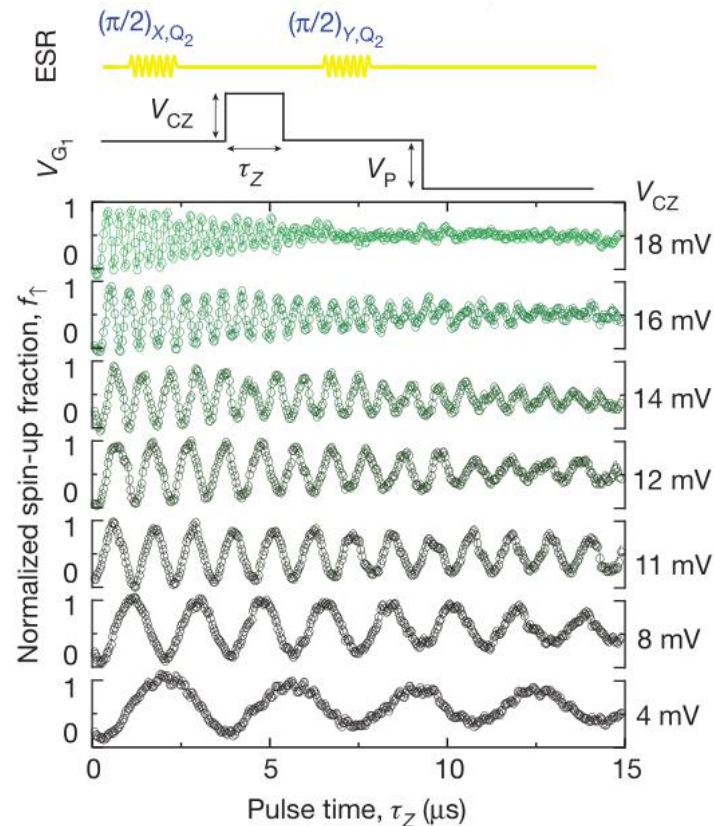
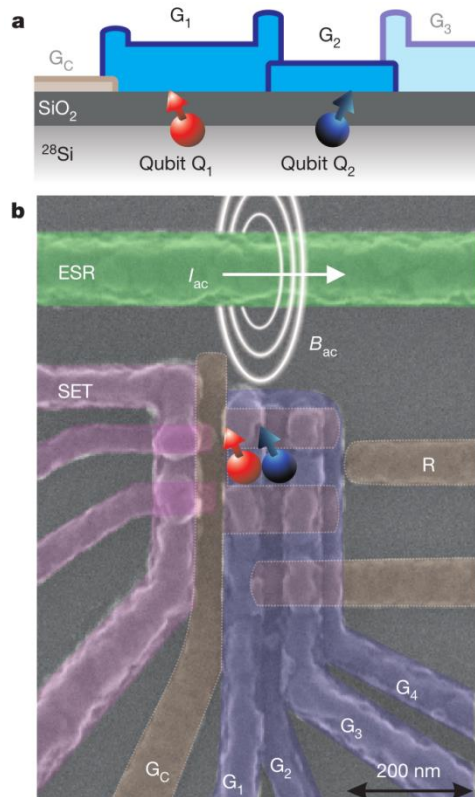
Do we **want** singlet-triplet qubits in Si?

➤ Maybe

- Inherently insensitive to B (decoherence-free subspace)
- One fast 1-qubit operation (exchange)
- Other 1-qubit operation difficult, but ...
 - Need micromagnet for ΔB ?

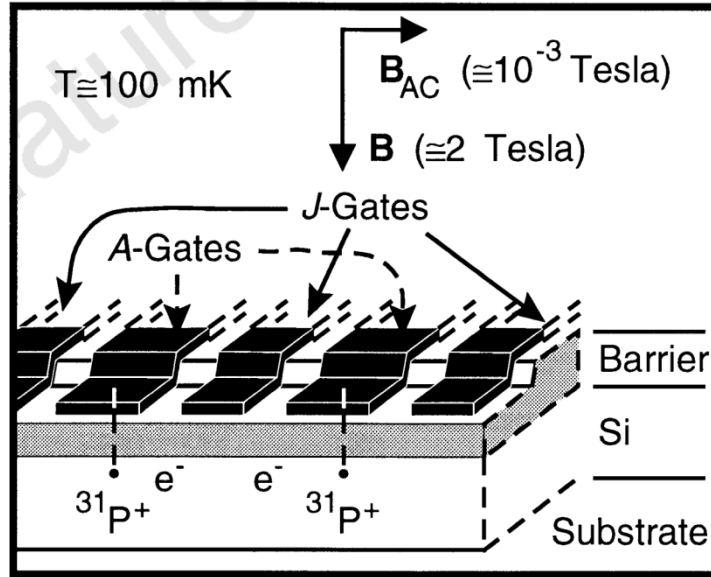


^{28}Si -MOS 2-Electron Double Dot



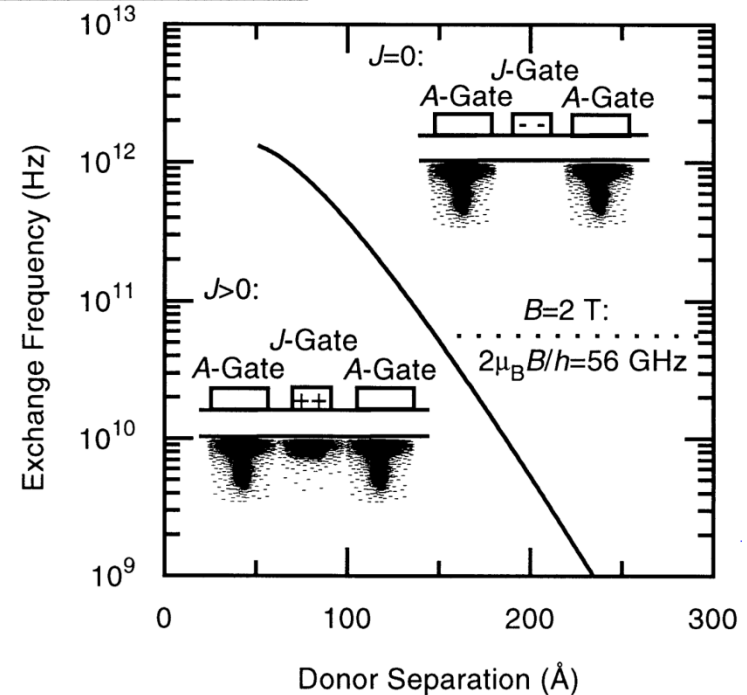
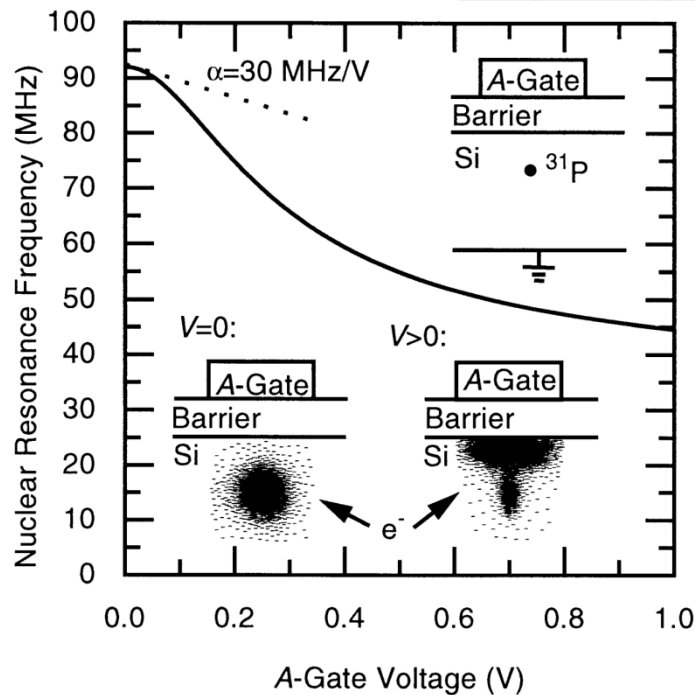
- CPHASE between 2 electrons \rightarrow CNOT
- Now working on improving fidelity

Donors in Si – the Kane Scheme

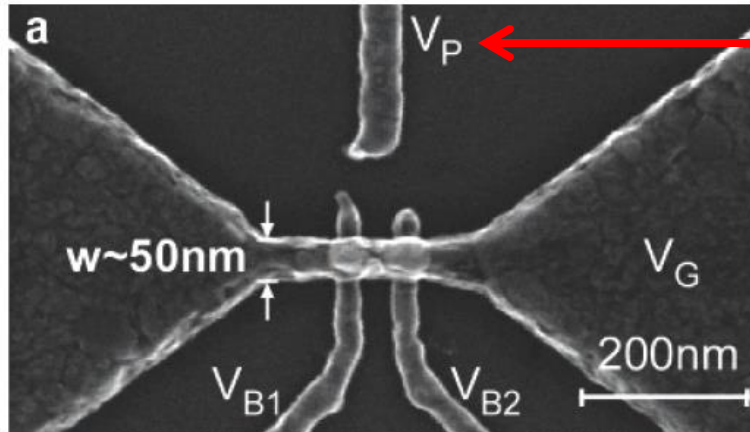


1-Qubit

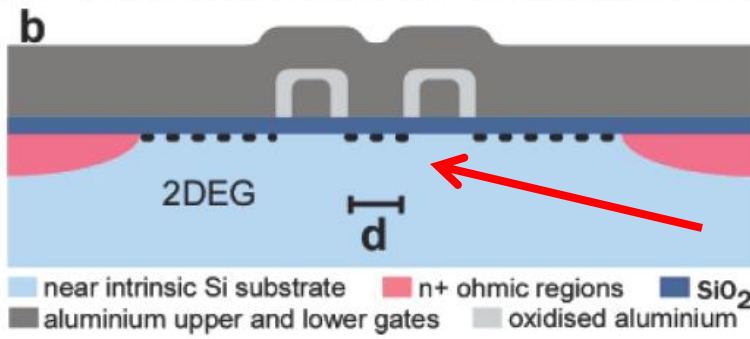
2-Qubit



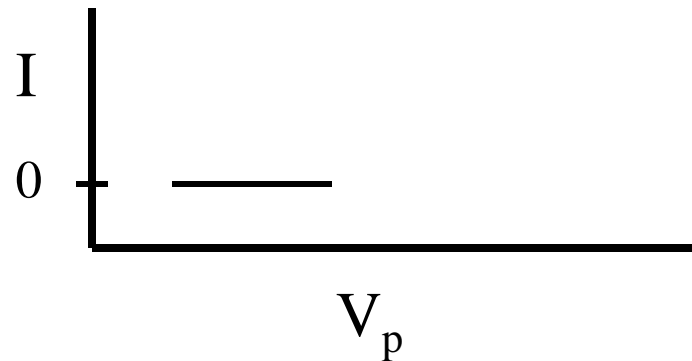
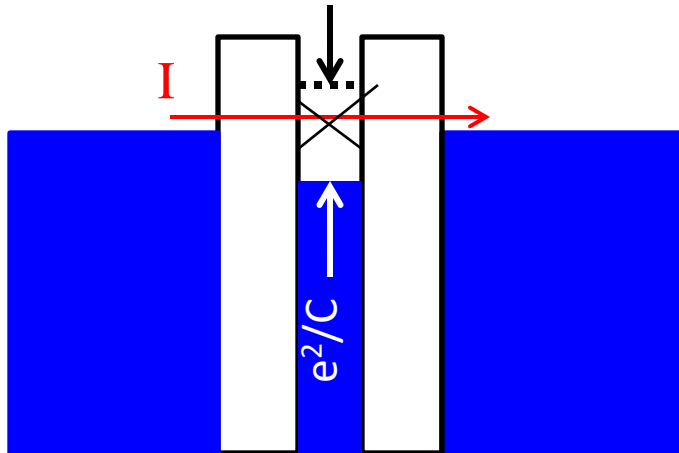
Single electron transistor (SET)



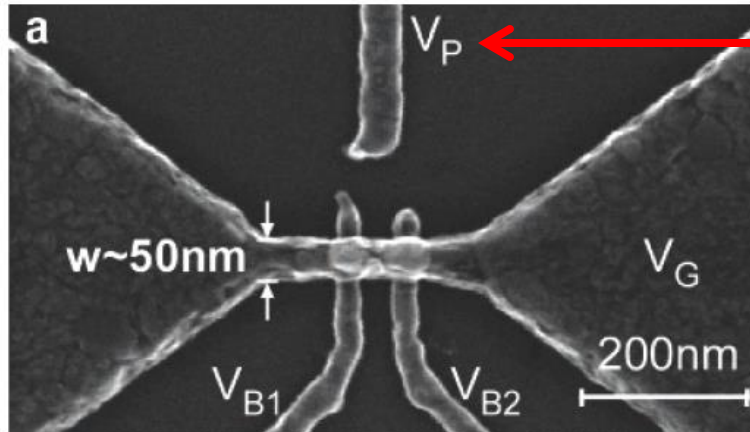
Plunger ← Angus, Nano Lett. 7, 2051 (2007)



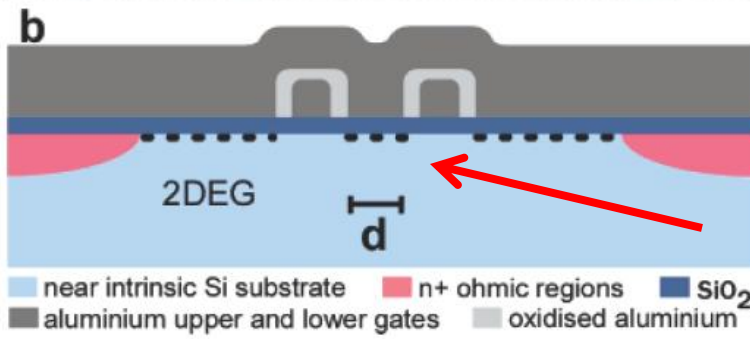
The “island”, length d , is small enough that the simple Coulomb energy to add an electron ($\frac{1}{2} e^2/C$) is non-negligible. The current has spikes as a function of plunger-gate voltage, V_p .



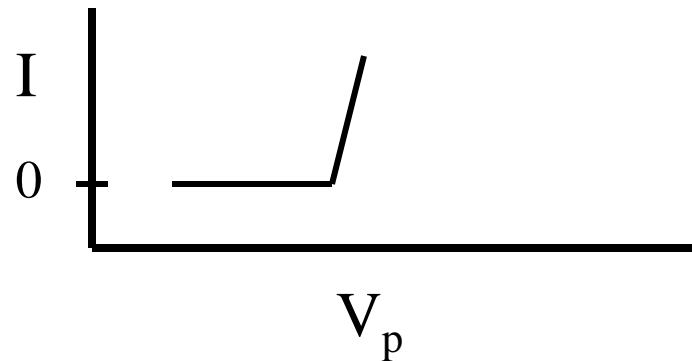
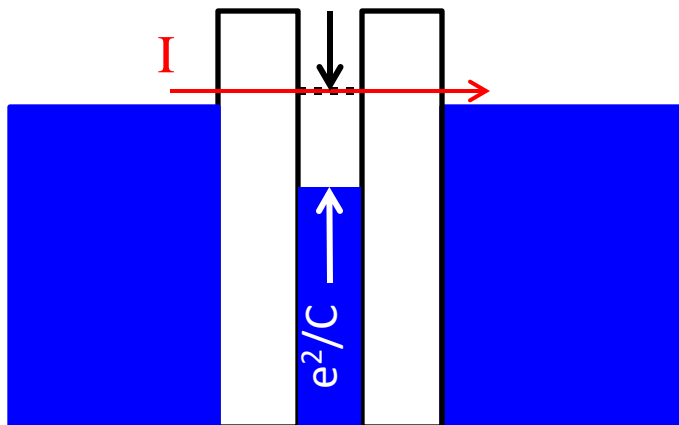
Single electron transistor (SET)



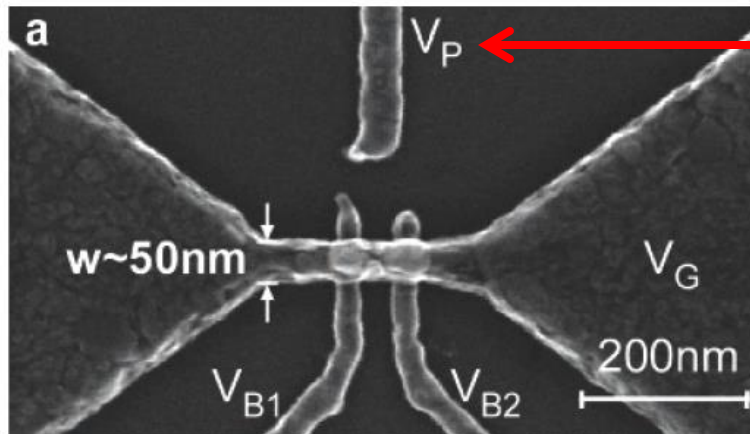
Plunger Angus, Nano Lett. 7, 2051 (2007)



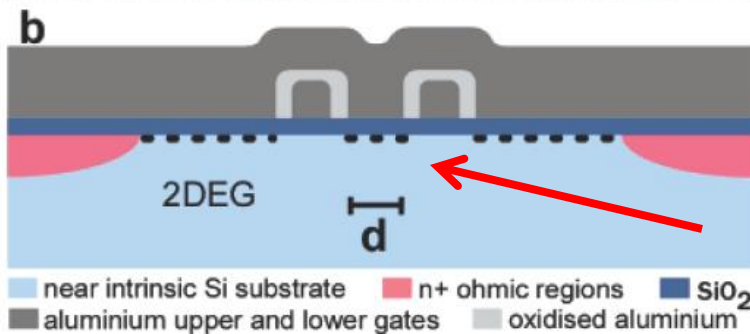
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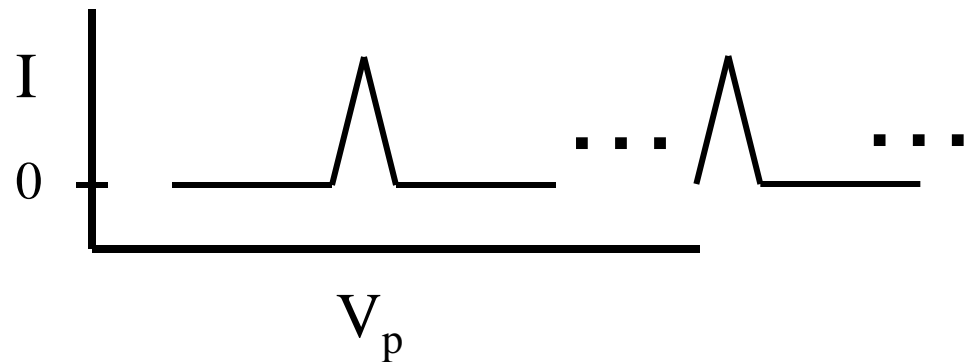
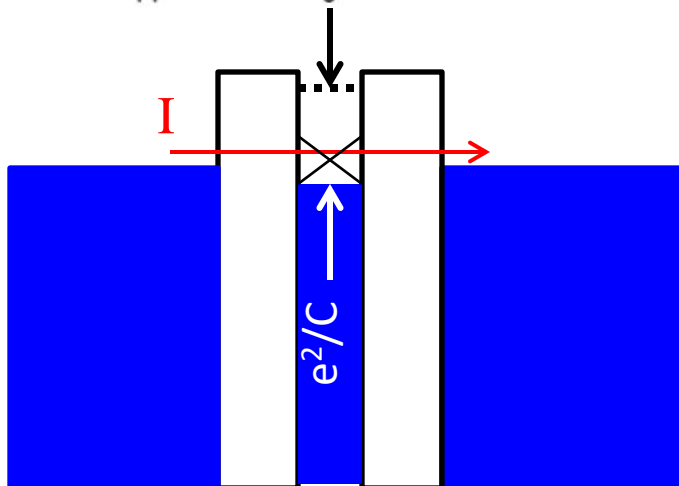
Single electron transistor (SET)



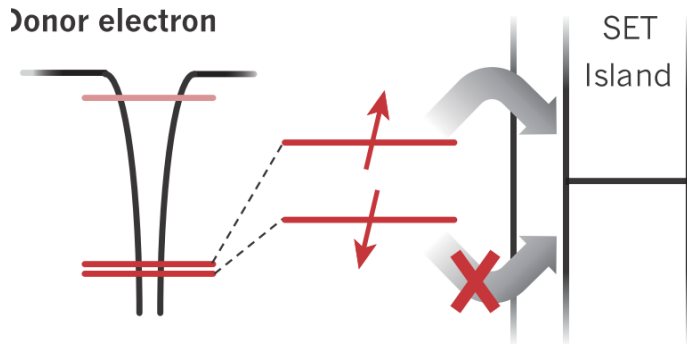
Plunger Angus, Nano Lett. 7, 2051 (2007)



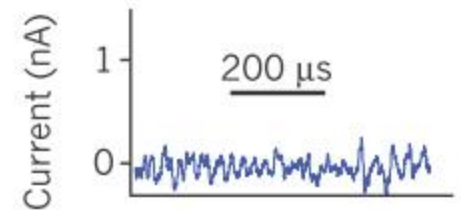
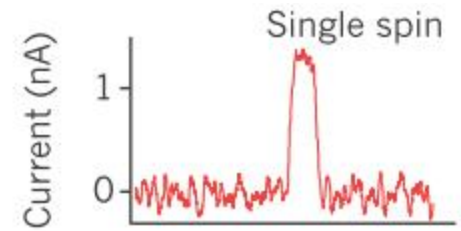
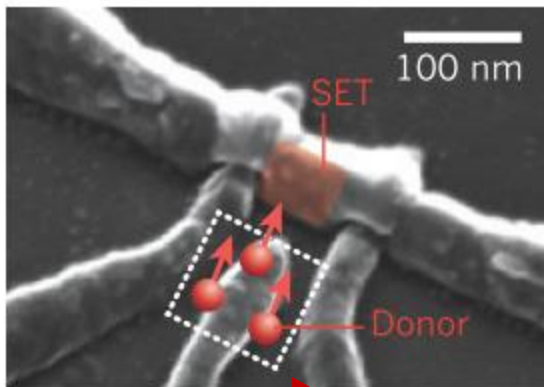
The “island”, length d , is small enough that the simple Coulomb energy to add an electron ($\frac{1}{2} e^2/C$) is non-negligible. The current has spikes as a function of plunger-gate voltage, V_p .



Measuring T_1 with the SET



The measurement proceeds like the quantum dot measurements of single electron, with the donor being the dot. **Obtained $T_1 \sim 6$ s**

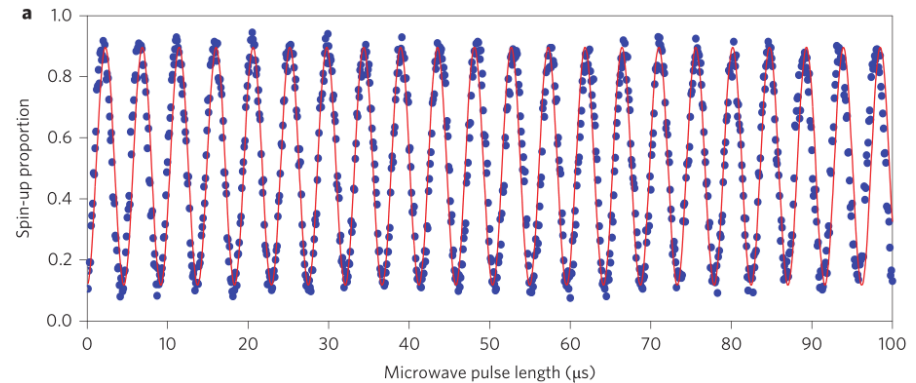
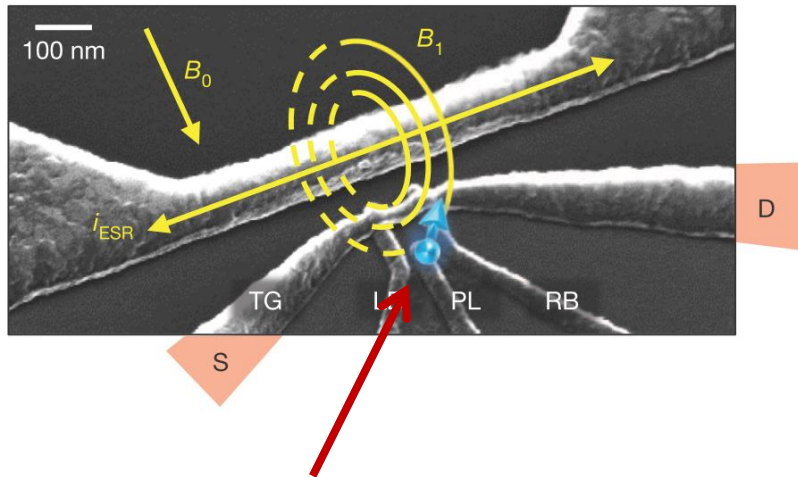


~ dozen donors

Measuring T_2 of a single donor electron

Send microwaves down shorted transmission line, as with the dots

Rabi oscillations



~ dozen donors

Muhonen, Nat. Nano, **9**, 986 (2014)

Results: $T_2^* \sim 200 \mu\text{s}$ (Ramsey fringe)

$T_2^{\text{Hahn}} \sim 1 \text{ ms}$ (Ramsey echo)

$T_2^{\text{CPMG} \times 8000} \sim 0.5 \text{ s}$

Nuclear spin

$T_2^{\text{CPMG}} \sim 35 \text{ s}$

Issues with Si qubits

- Stark tuning donor spin requires high fields for MHz tuning
- Donor pitch too tight
 - Donor wavefunction $\sim 2\text{nm}$
- Donor “exchange oscillations”
 - Exchange interaction between two donors is not monotonic in the distance between them (varies by 10x, or more, while donor moves 1 lattice constant)

Every spin is the same, right?

- Linewidth:
 - Assume surface code cycle = $1\mu\text{s}$
 - Allowed phase error/cycle = 0.1% $\Rightarrow 2 \times 10^{-3} \pi$
 - Maximum linewidth = 1kHz (10^{-3} cycles in $1\mu\text{s}$)
 - Bulk $^{28}\text{Si}:\text{P} \Rightarrow$ few kHz to 10's kHz (not really understood)
 - Epitaxial $^{28}\text{Si}:\text{P}/^{\text{nat}}\text{Si} \Rightarrow$ 100's kHz
 - **Can we individually tune 10^9 qubits?**
- Large local strains from oxide & gate metals
 - Probably contributes to donor linewidth
 - Seems to be much bigger in SOI

Who Cares About Defects?

- Defects (thermodynamics says there are some)?

$\sim 10^{10}/\text{cm}^2$ with depth $\geq 3\text{meV}$ at MOS interface

$\Rightarrow \sim 100\text{nm}$ between traps

- Are they a problem?

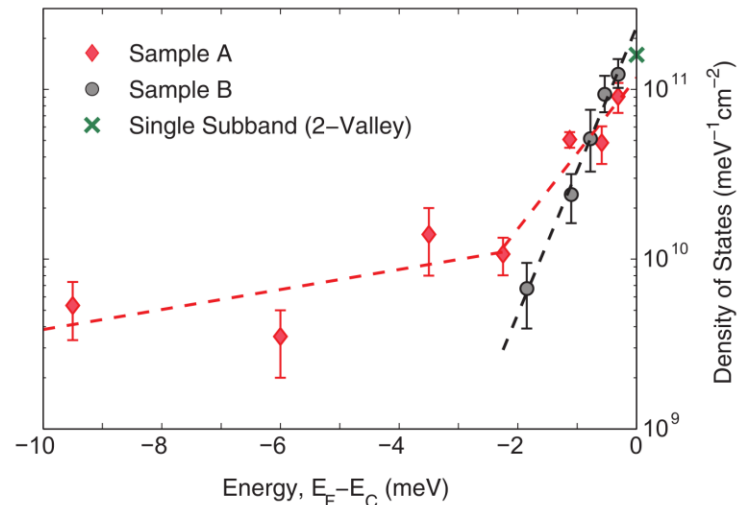
- Distort donor-dot energies

- “Just” calibration issue?

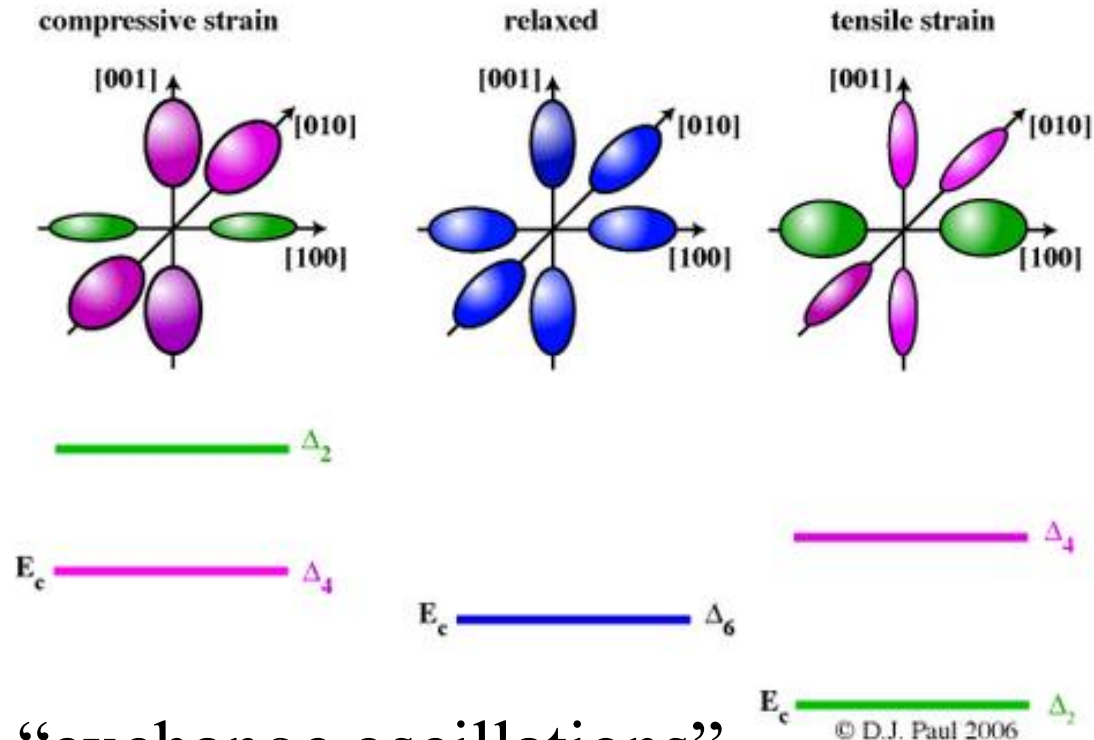
- Extra trapped electrons

- Exchange with dot electrons or transiting electrons?

- Mess up microwave coupling?

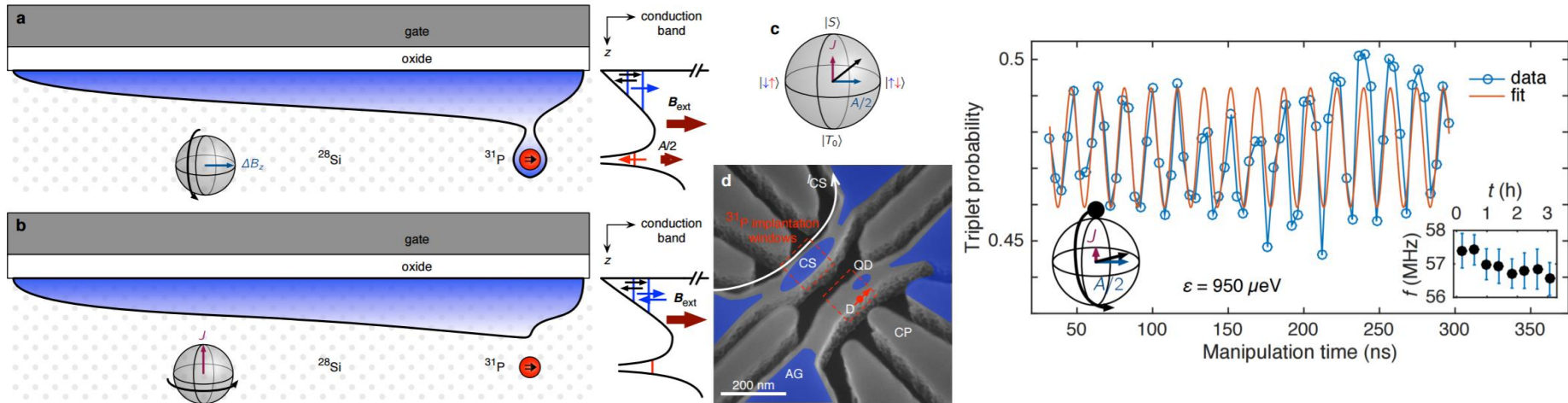


Conduction band valleys in Si



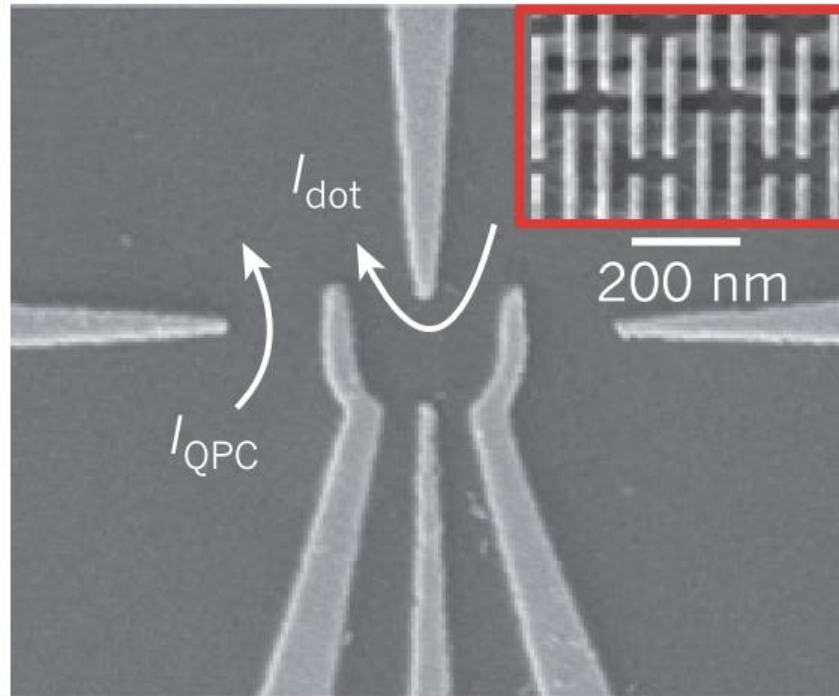
- Donor “exchange oscillations”
- Valley splitting \sim Spin splitting
 - Get valley states mixing with spin states in dots \Rightarrow bad!
 - Interface details (atomic steps?) \Rightarrow valley splitting

Coupling Donor to Quantum Dot

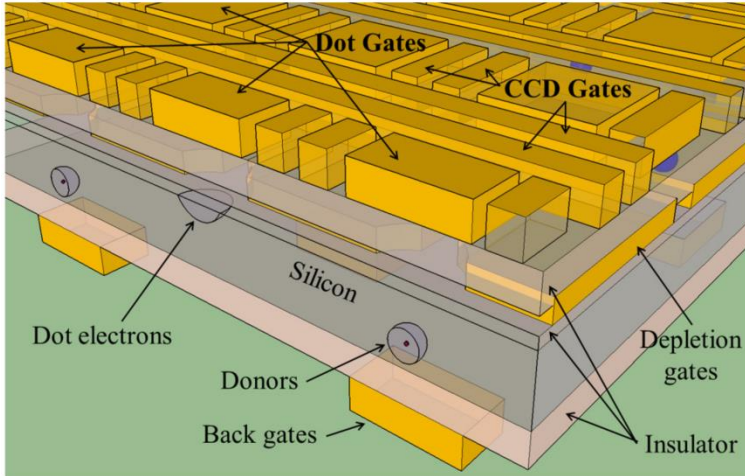


- Singlet-triplet qubit with one electron on/off phosphorus
- Electron on donor \Rightarrow rotate between S & T_0 (vertically)
- Electron off donor \Rightarrow just exchange (rotate horizontally)
- Fit oscillations, including $J \neq 0$ with electron on donor
- Used 4 electrons not 2, because small valley splitting
 - Filled lower valley states, so only consider upper pair

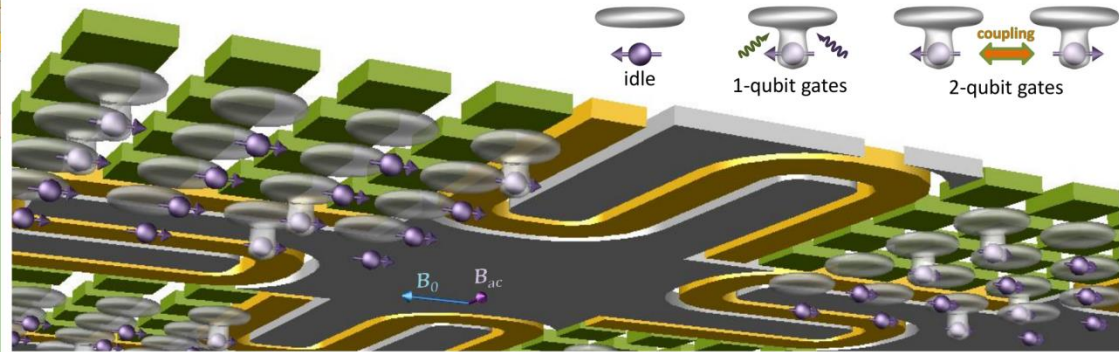
Si quantum dot vs. SRAM



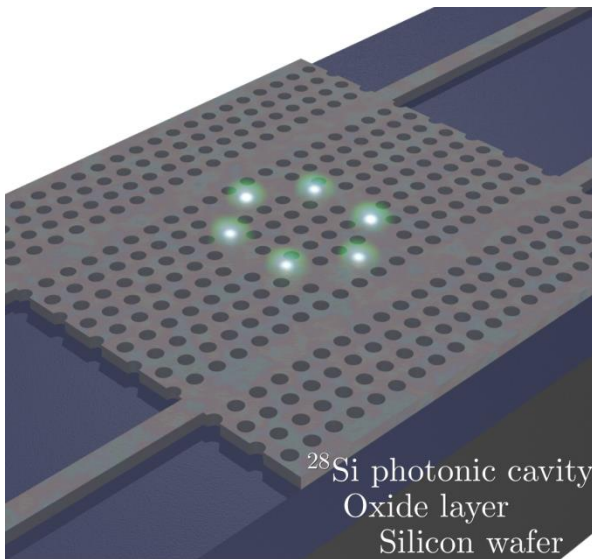
Alternate Schemes



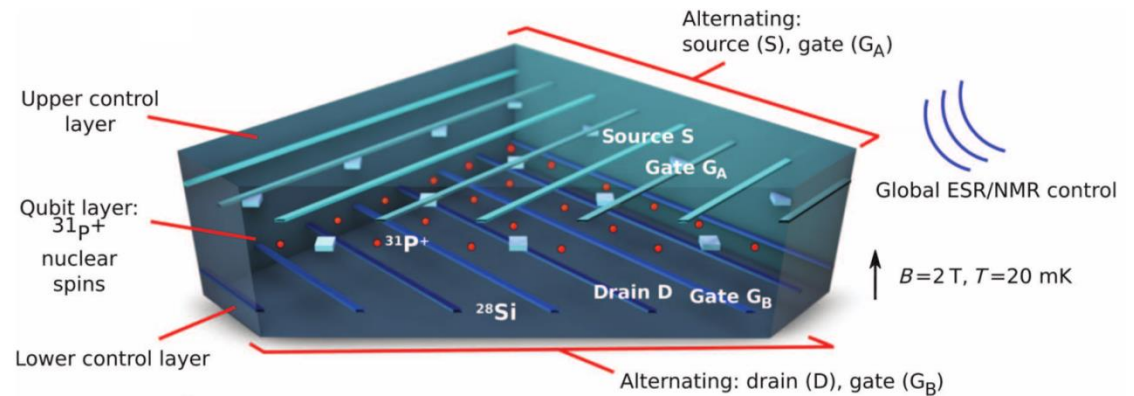
Pica, PRB **93**, 035306 (2016)



Tosi, ArXiv:1509.08538 (2105)

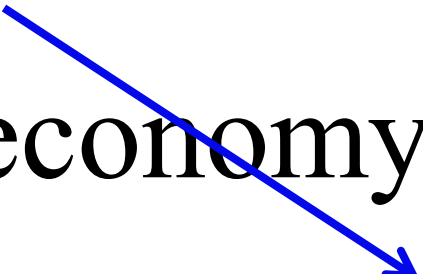


Morse, arXiv:1606.03488 (2016)



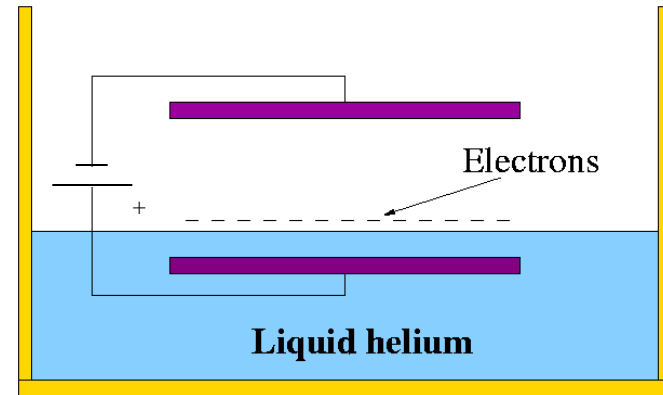
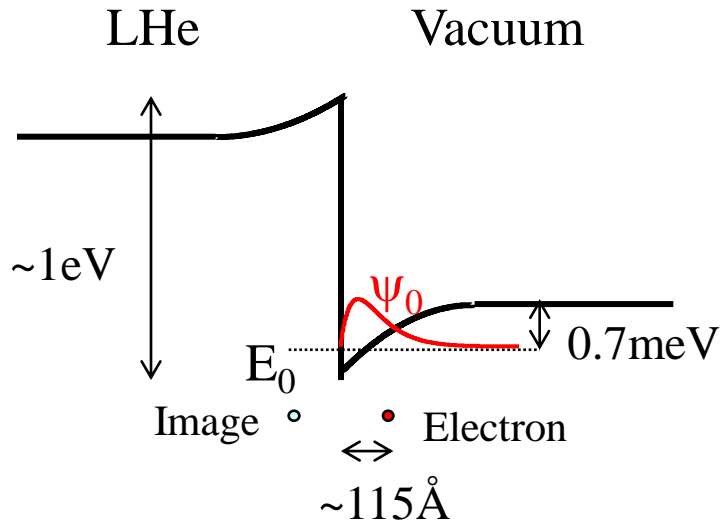
Hill, Sci Adv **1**, e1500707 (2015)

It's the economy, stupid.*
materials



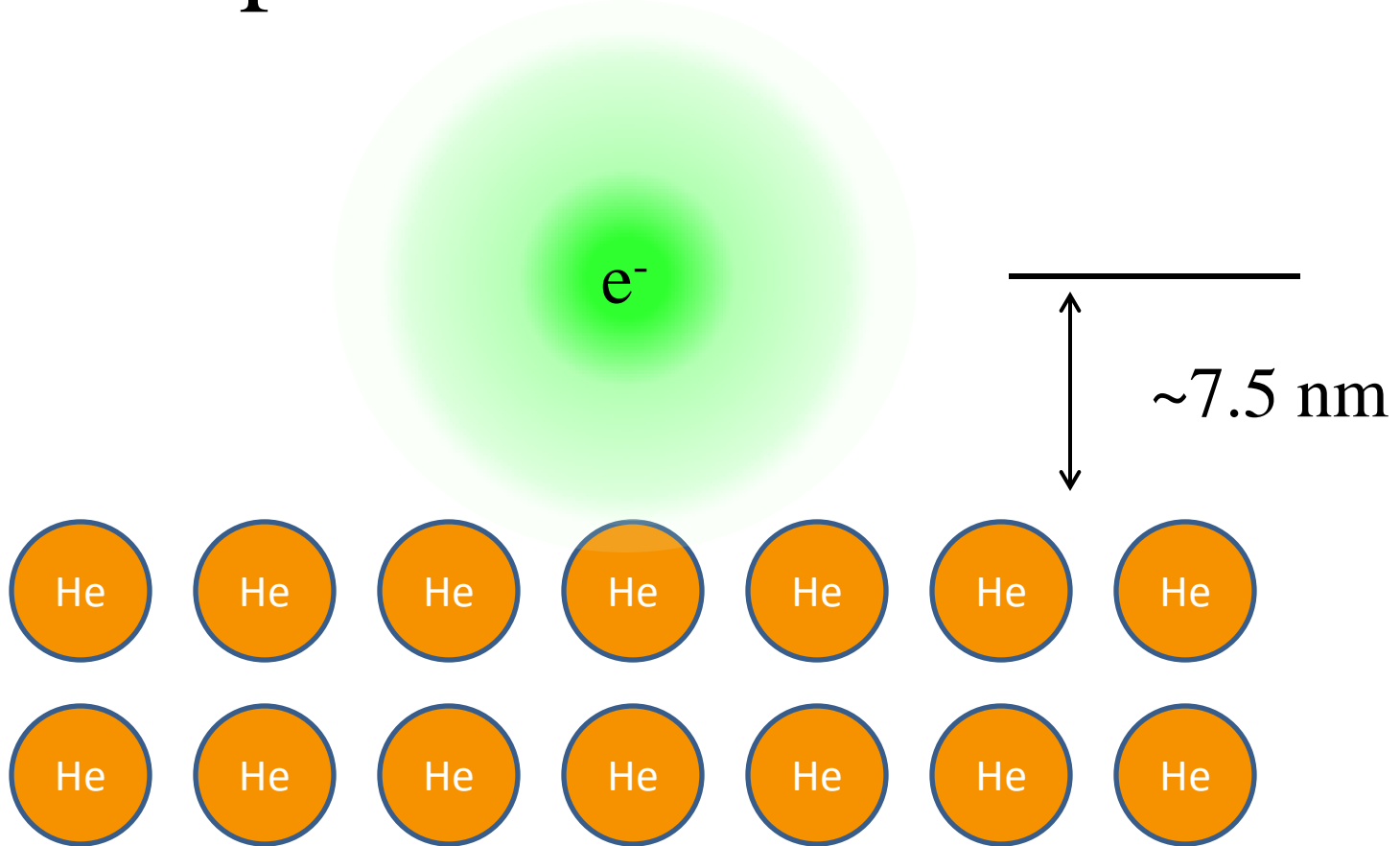
* James Carville

Experimental System



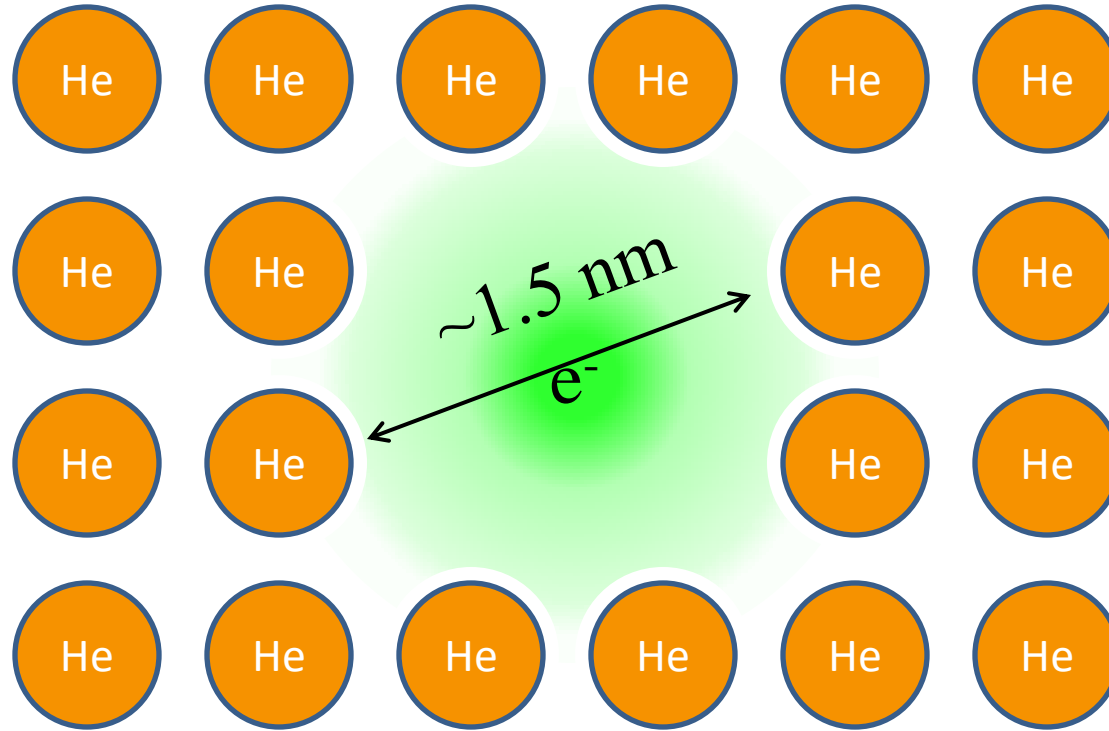
- Electron bound to image in liquid He
 - $\psi_z =$ radial hydrogenic wave function
 - $\psi_{x,y} =$ plane waves
 - Submerged gates can modify binding
 - Extremely mobile electrons ($\sim 100 \times 10^6 \text{ cm}^2/\text{V-s}$)
 - Low density 2D system ($10^9 \dots 10^5/\text{cm}^2$)

Spin Orbit Interaction



Overlap of electron above surface with helium 2P-band?

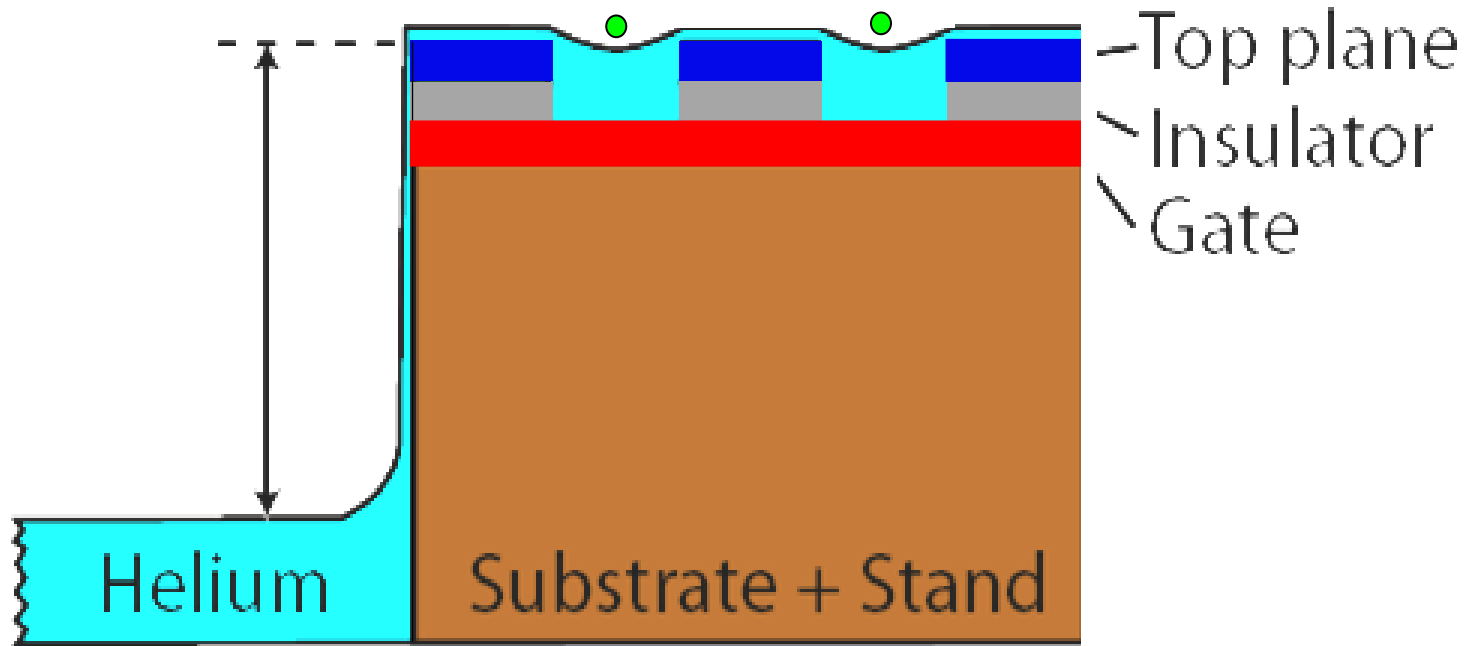
Spin Orbit in Electron Bubble



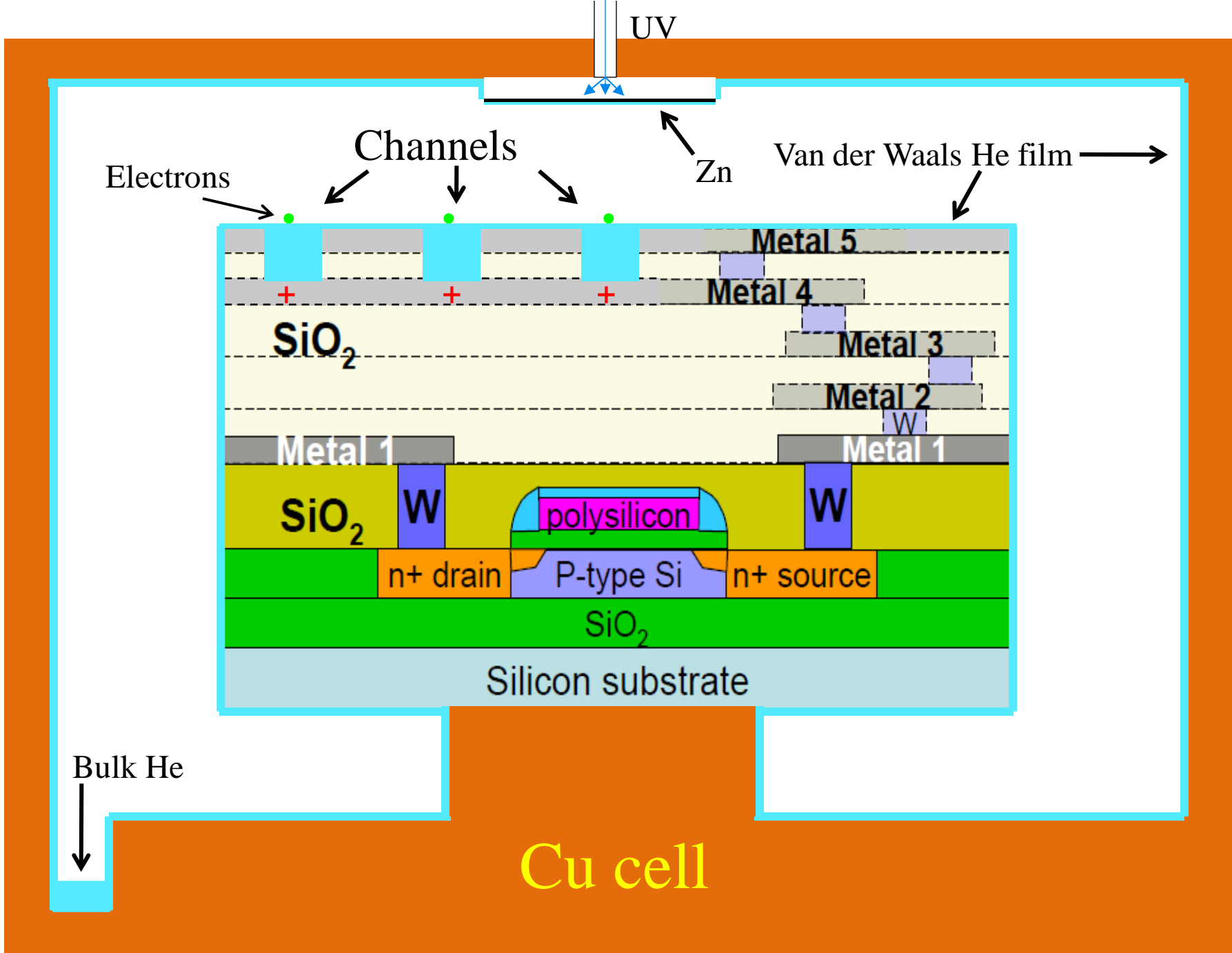
$\Delta g/g < 3 \times 10^{-7}$ vs. Si with $\Delta g/g \sim 10^{-3}$ so 10^7 less decoherence
 \Rightarrow Spin coherence for *mobile* electrons > 1 second

Reichert and Jarosik, PRB **27**, 2710 (1983).

Helium-Filled Channels



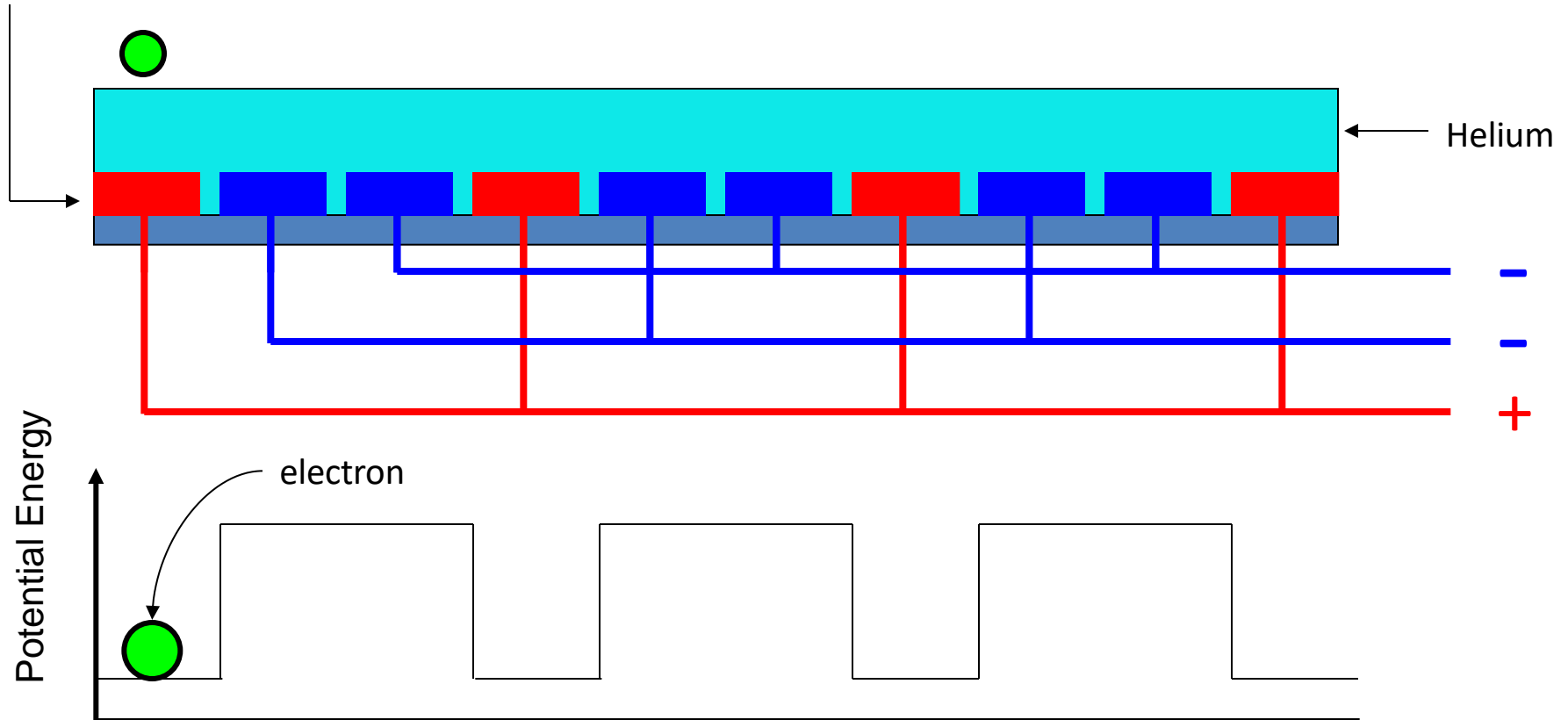
- Helium depth set by thickness of deposited layer
- Easy to make precise depths of nm to a few μm



3-phase CCD

Potential

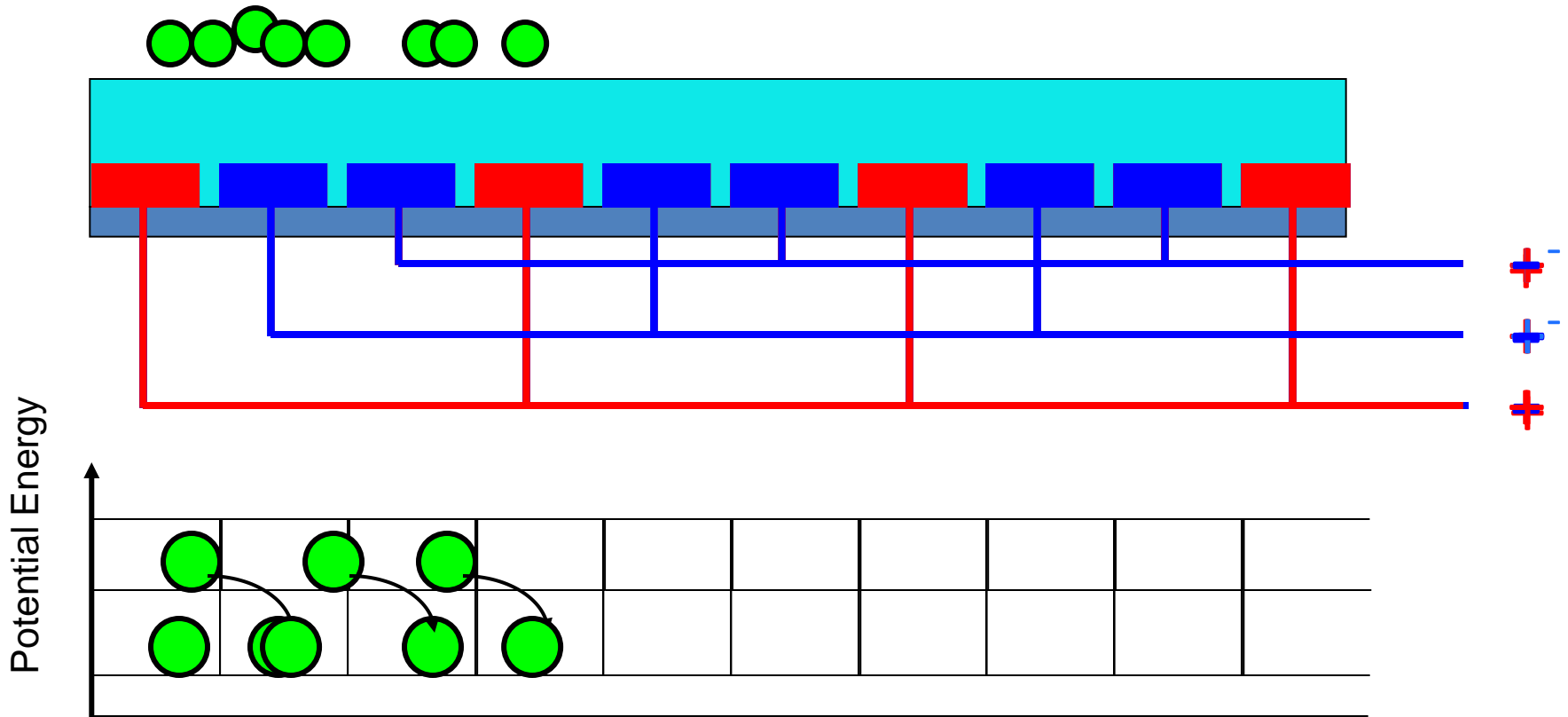
Underlying gates



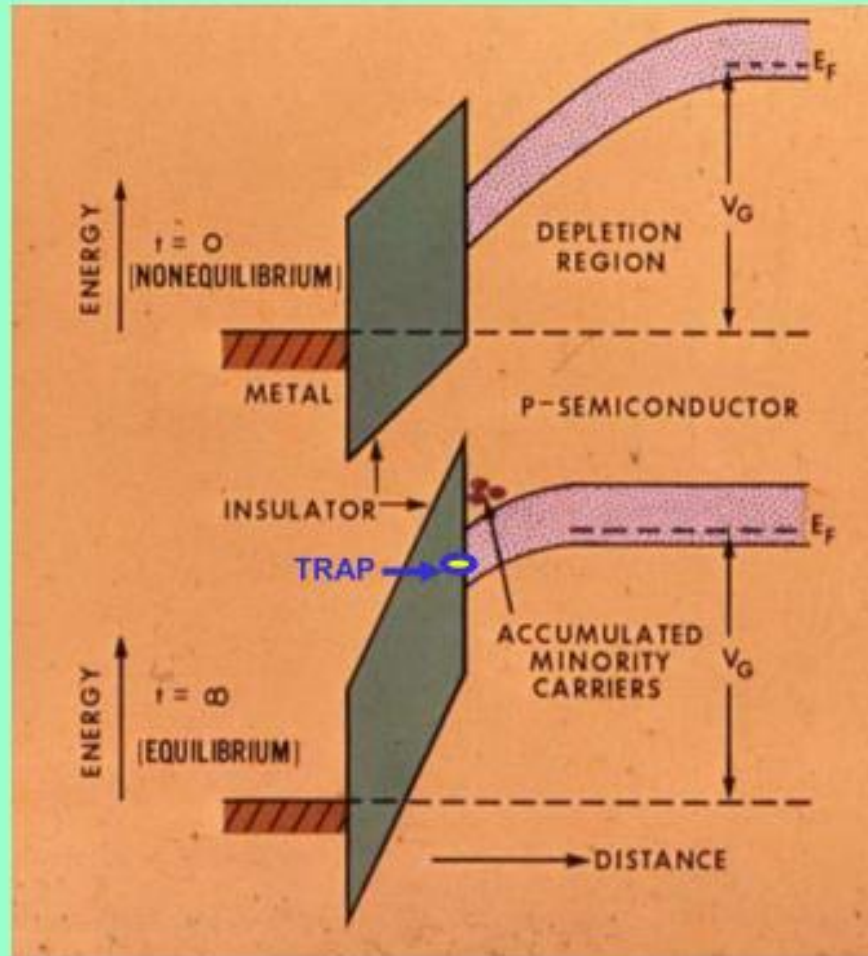
3-phase CCD

Clocking 8

Electron has moved one pixel (3 gates) to the right

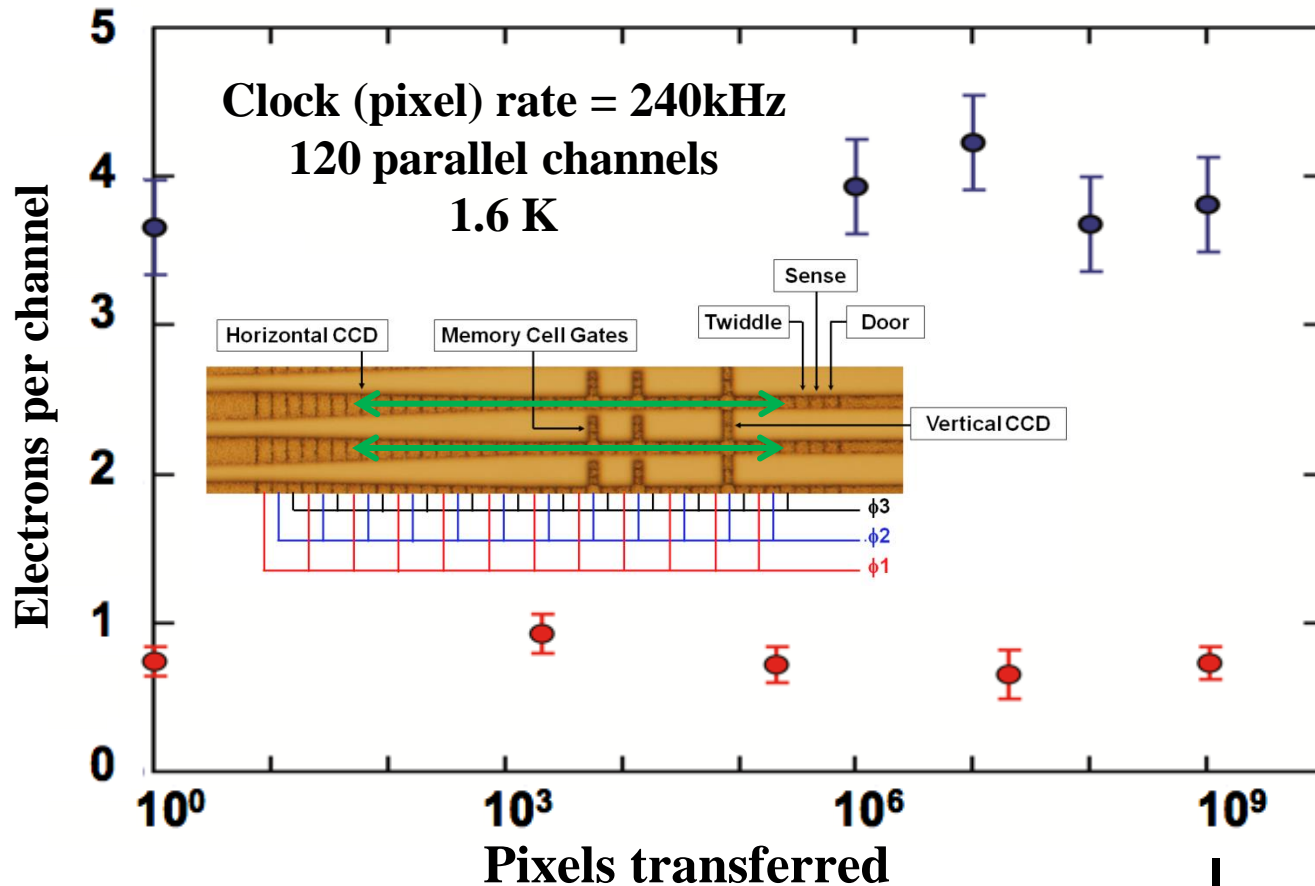


MOS Energy Diagram



George Smith, Nobel Prize Lecture on CCDs, 2009

Horizontal Clocking Efficiency



No measurable errors

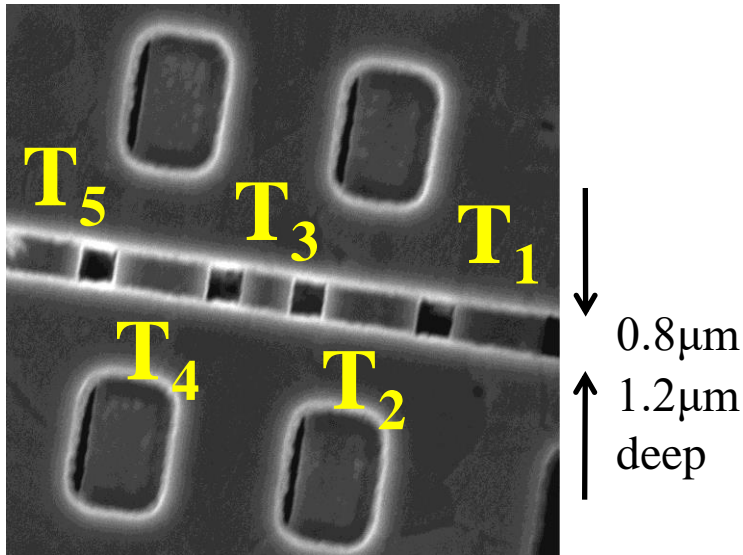
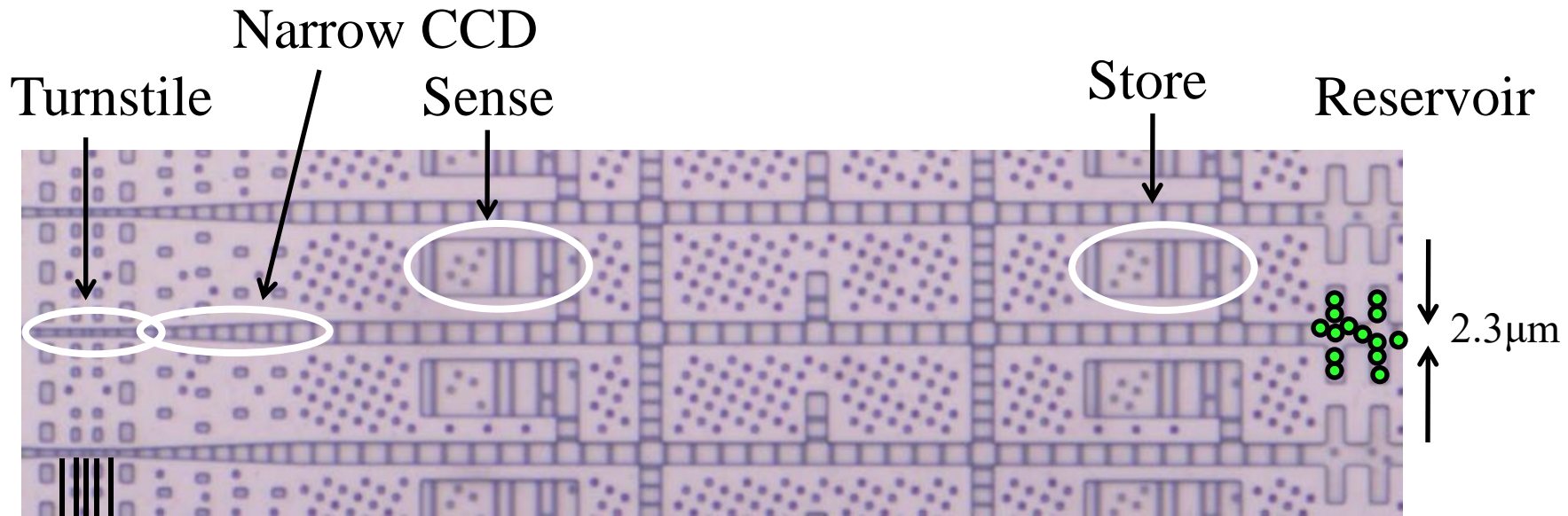
→ ~ 70 min.
→ ~ 9 km.

One Sheep per Clock



Device Structure

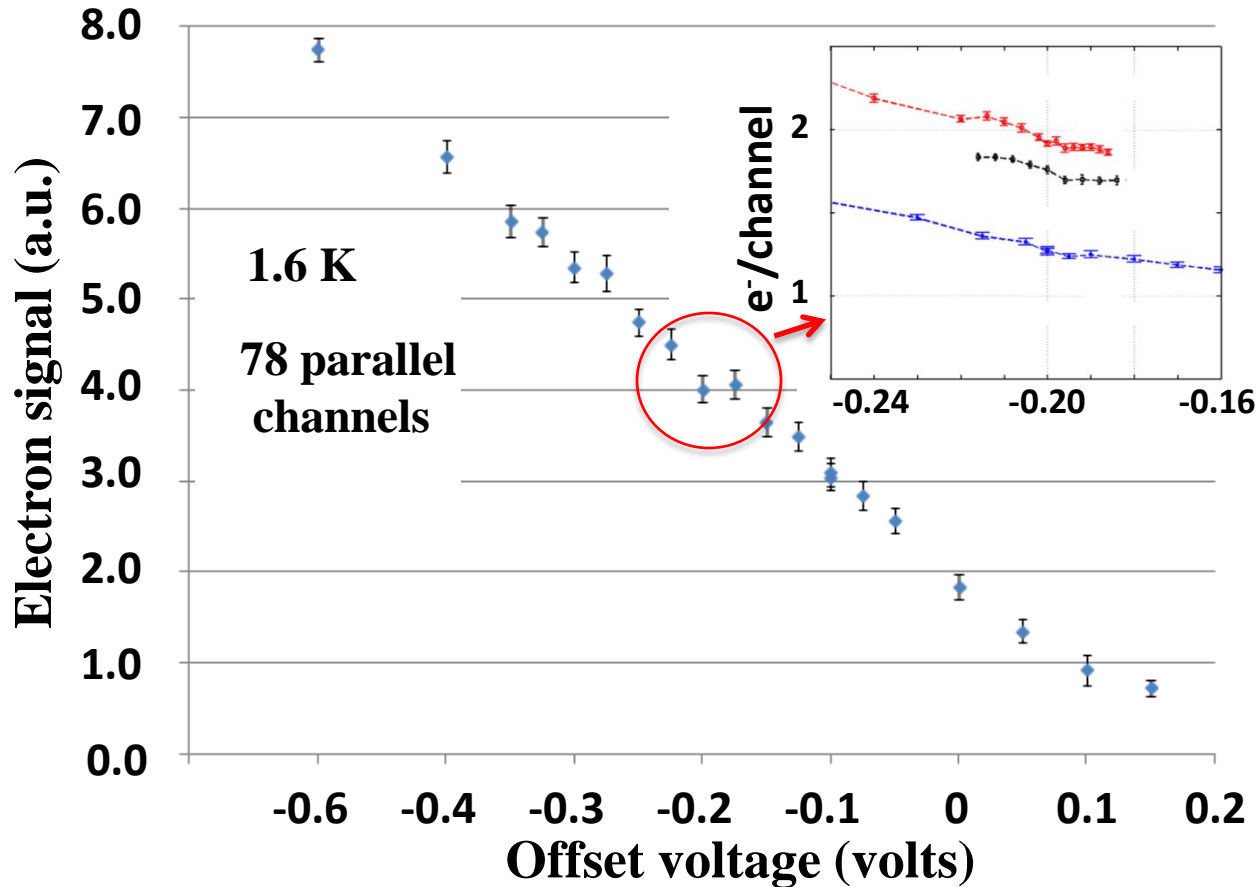
78 parallel channels



- Electrons deposited in reservoir
- Clock into channel and measure
 - Go through narrow CCD
 - Extras back to reservoir
- Clock into turnstile region
 - ~ 20 electrons/channel

Plateau

(measuring 78 channels in parallel)



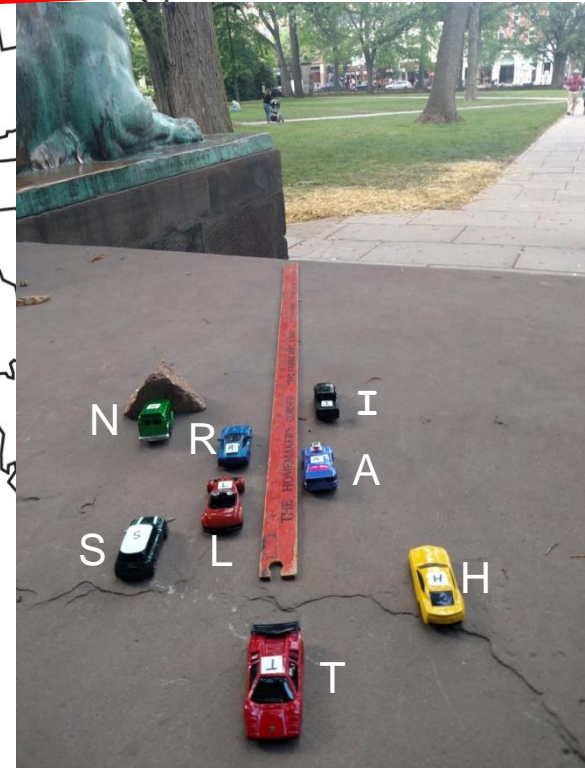
Conclusions

- Electron spin qubits in Si have long enough coherence for quantum computing
- 1 and 2 qubit gates have been demonstrated using electrons in quantum dots and electrons bound to donors
- Devices can be very small and fast
- Individual devices can have high fidelity
- Scaling to a large quantum computer will require solving some difficult materials issues
- People working on various approaches to dealing with these issues

Race to a Quantum Computer

200,000,000
inches (Qubits)

0 inches (Qubits)



I and R have a big lead.

N seems to have hit a brick wall, H is just starting, S says he's coming on fast, and T says he knows a shortcut