

# Monolayer semiconductors:

## Valley dynamics & 'valley noise'

*(Or, what can we learn about dynamics...  
without ever actually perturbing the system?)*

Yesterday: Excitons/optoelectronics  
Not much valley stuff  
Static measurements, high B

Today: Valley *dynamics* ( $ps \rightarrow \mu s$ )  
Ultrafast optics, not much B  
Noise (& quantum measurement)

**Scott Crooker**  
NHMFL Los Alamos

# **Useful / interesting review-type papers on monolayer TMDs (with an emphasis on optics and/or valleytronics):**

## **Valleytronics in 2D materials**

JR Schaibley, H. Yu, G. Clark, P. Rivera, J. S. Ross, K. Seyler, W. Yao, X. Xu  
*Nature Reviews Materials* **1**, 16055 (2016)

## **Light-valley interactions in 2D semiconductors**

KF Mak, D. Xiao, J. Shan  
*Nature Photonics* **12**, 451 (2018)

## **Why all the fuss about 2D semiconductors?**

Andres Castellanos-Gomez  
*Nature Photonics* **10**, 202 (2016)

## **Photonics and optoelectronics of 2D semiconductor TMDs**

K. F. Mak and J. Shan  
*Nature Photonics* **10**, 216 (2016)

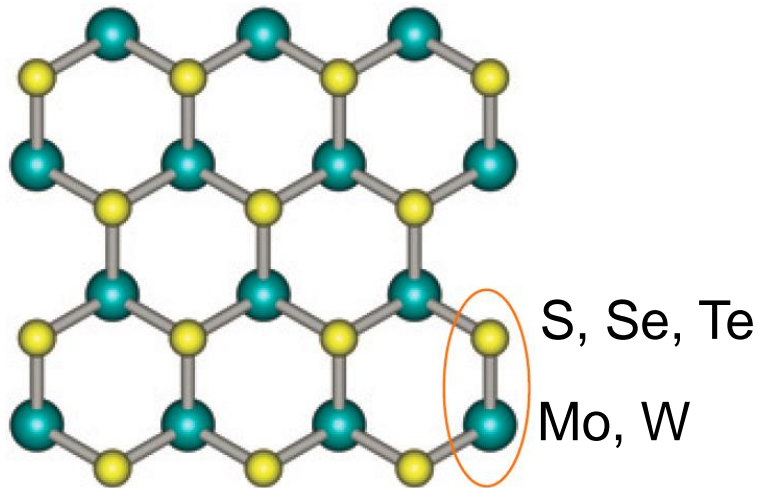
## **Spins and pseudo-spins in layered TMDs**

Xiaodong Xu, Wang Yao, Di Xiao, Tony F. Heinz  
*Nature Physics* **10**, 343 (2014)

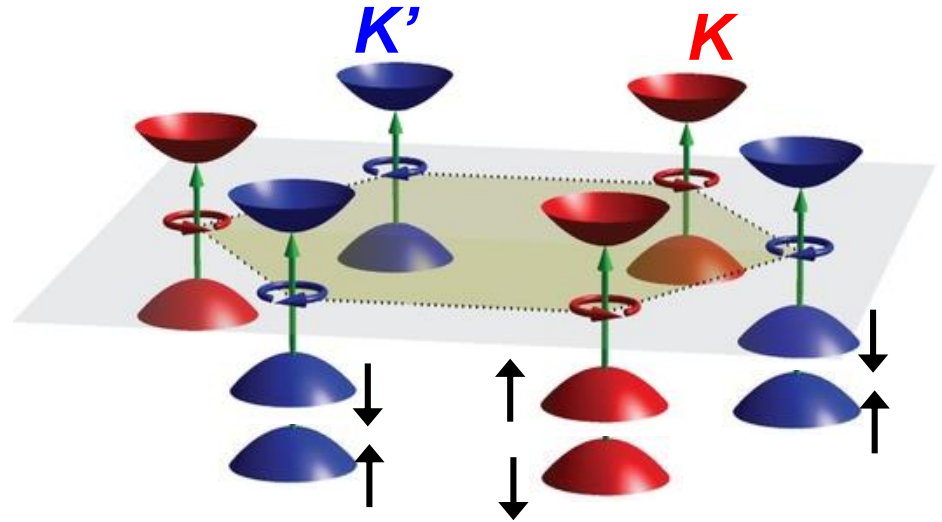
## **Van der Waals heterostructures**

A. K. Geim and I. V. Grigorieva  
*Nature* **499**, 419 (2013)

# Reminder: 'Valley pseudospin' & valleytronics



-from X. Xu *et al.*, *Nat. Phys.* **10**, 343 (2014)



**Key point:** lack of inversion + SOC: *spin-valley locking*

**RCP & LCP light couple *selectively* to  $K$  &  $K'$  valleys**

*Easy optical access to valley degrees of freedom*

**First paper:** Di Xiao *et al.*, *PRL* **108**, 196802 (2012)

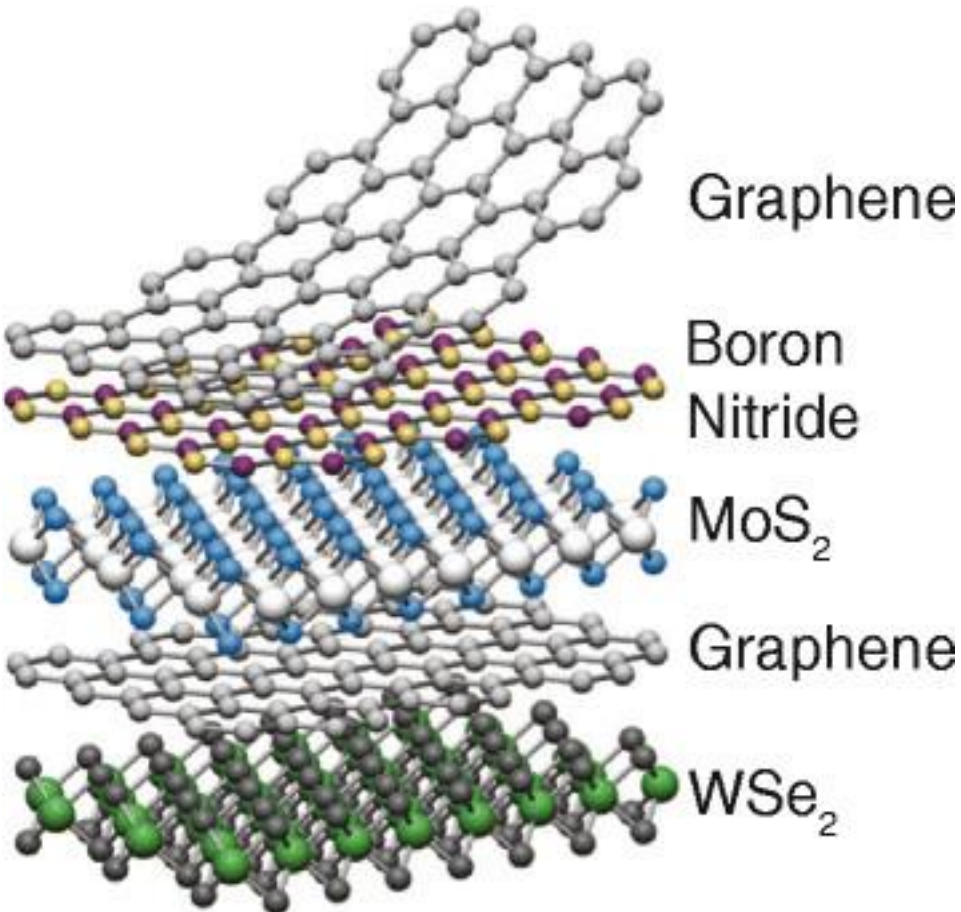
**Excellent reviews:** J. Schaibley, X. Xu *et al.*, *Nature Reviews* **1**, 16055 (2016)

X. Xu, D. Xiao, W. Yao, & T. Heinz, *Nat. Physics* **10**, 343 (2014)

K. F. Mak, D. Xiao, & J. Shan, *Nat. Photonics* **12**, 451 (2018)



# “Valleytronic” devices based on 2D TMDs?

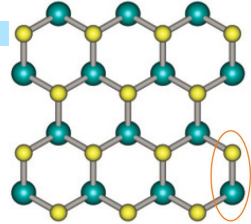


## We still need to know:

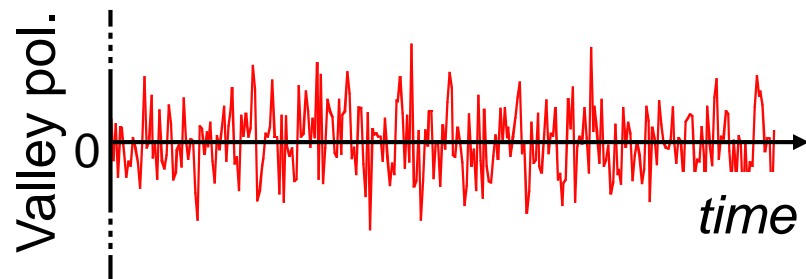
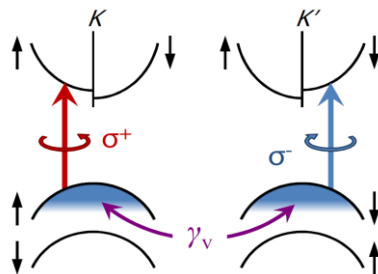
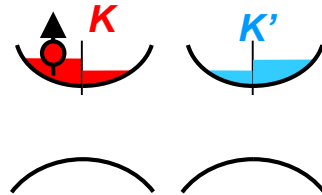
- 1) Spin & valley relaxation?
- 2) Resident carriers (*not* excitons)
- 3) Electrons vs. holes?

# Today: Spin/valley dynamics in monolayer TMD semiconductors

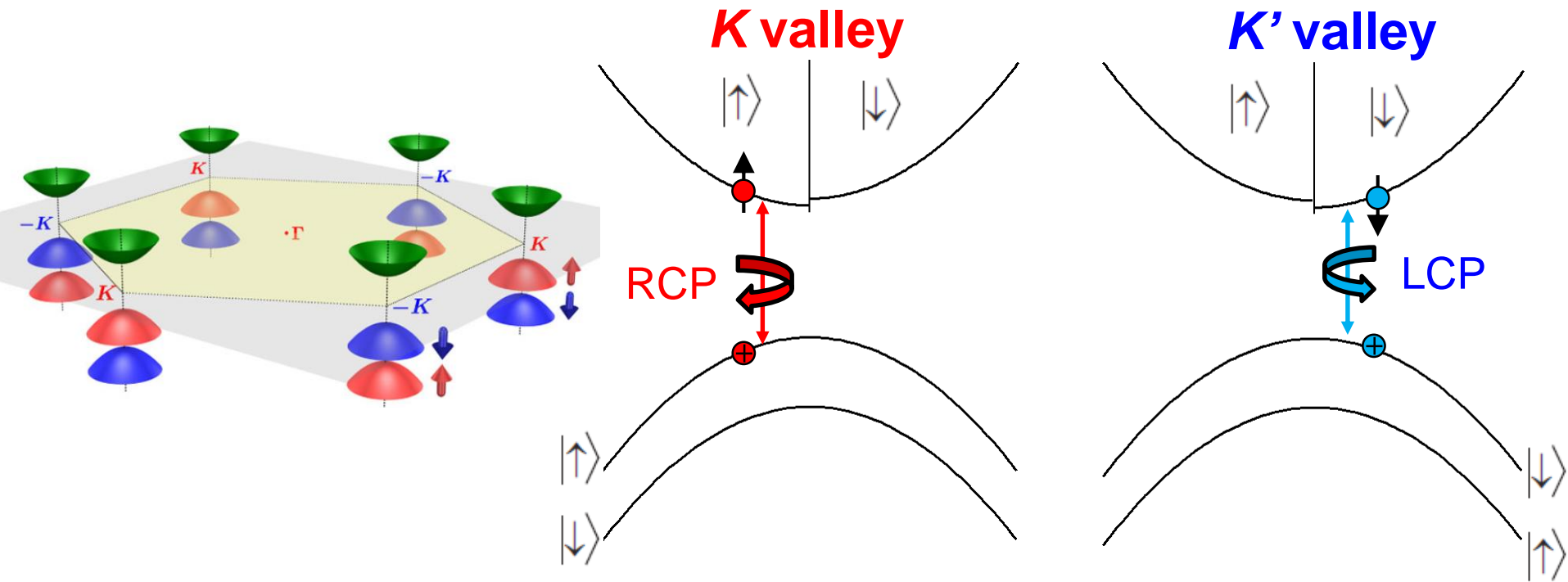
## Outline:



- **Brief history of “robust valley degree of freedom” in ML TMDs**
  - *photoluminescence of (short-lived) excitons*
- **Spin/valley dynamics of *resident* electrons & holes**
  - *actually useful parameters for real quantum devices*
  - *$\mu$ s valley polarization of holes (promising!)*
- **Spontaneous thermodynamic “valley noise” of electrons & holes**
  - *nonperturbative (quantum?) measurements based on fluctuations*
  - *“valley noise” reveals intrinsic valley dynamics*



# Valley-polarized *excitons* in 2D semiconductors

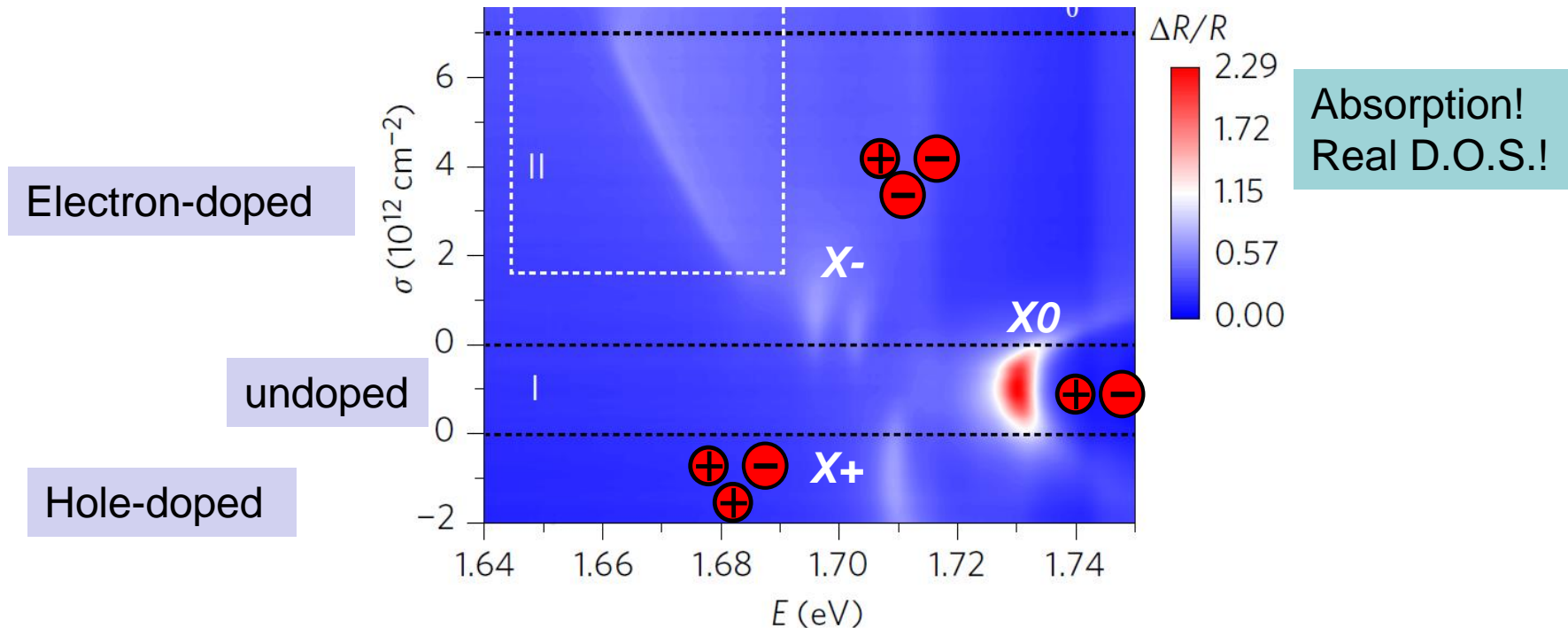


- **Optical selection rules at “A” exciton:**  
RCP light couples to **spin-up** excitons in  **$K$  valley**  
LCP light couples to **spin-down** excitons in  **$K'$  valley**

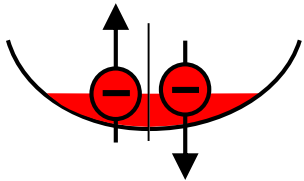
**First paper:** Di Xiao *et al.*, *PRL* **108**, 196802 (2012)

**Excellent reviews:** X. Xu, D. Xiao, W. Yao, & T. Heinz, *Nat. Physics* **10**, 343 (2014)  
K. F. Mak, D. Xiao, & J. Shan, *Nat. Photonics* **12**, 451 (2018)

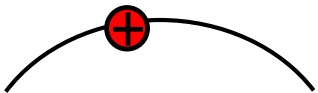
# Also: Positively/negatively charged excitons



From Wang, Shan, & Mak, *Nature Nanotech.* **12**, 144 (2017)



Trion absorption depends *explicitly* on the density of resident carriers. *No resident carriers -> no trion D.O.S.*

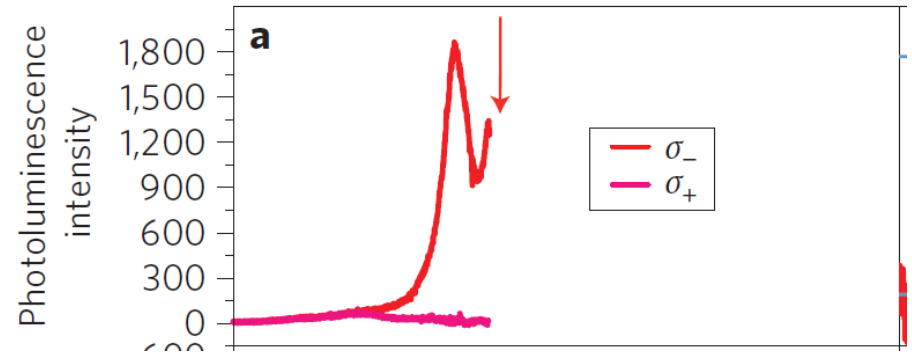
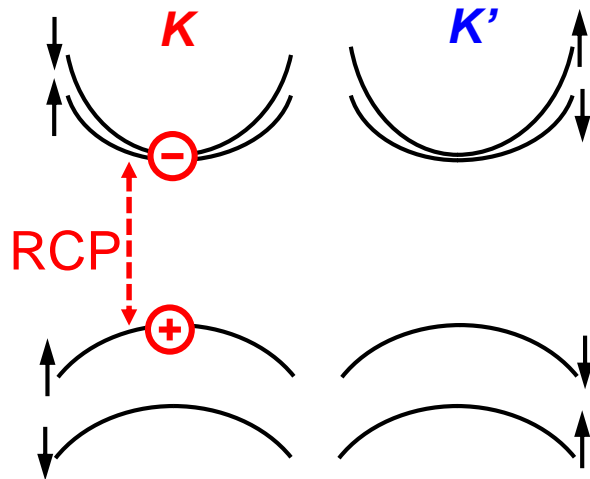


**Key point:**

Signals at *trion* energy should tell us about polarization of Fermi sea.

# Initial PL studies suggested robust valley pol.

In 2012, several groups studied circularly-polarized photoluminescence of monolayer  $\text{MoS}_2$ . PL was co-polarized.



Cao et al., *Nature Commun.* **3**, 887 (2012)  
Zeng et al, *Nature Nanotech.* **7**, 490 (2012)  
Mak et al, *Nature Nanotech.* **7**, 494 (2012)  
Sallen et al., *PRB* **86**, 081301 (2012)

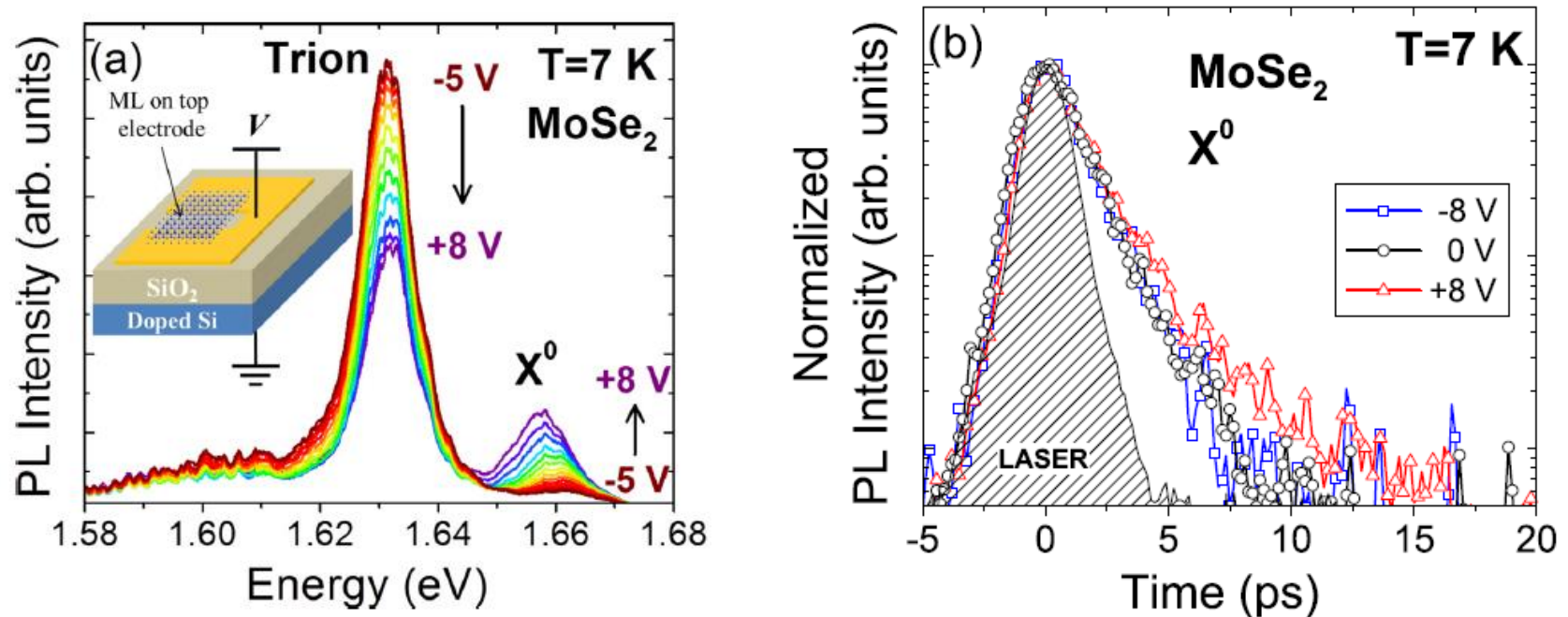
**But** : photoluminescence is a (nonequilibrium) exciton effect  
So -- either exciton valley relaxation is indeed slow (“robust”)  
...or...

*maybe excitons are just really short-lived*



# Indeed: Exciton recombination is really fast!

$e$ - $h$  recombination lifetimes  $< 10$  ps at low temperatures

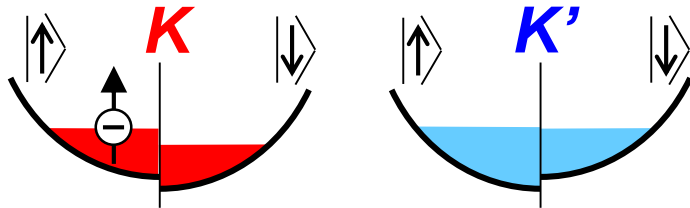


[data from C. Robert, B. Urbaszek, X. Marie *et al.*, PRB **93**, 205423 (2016)]

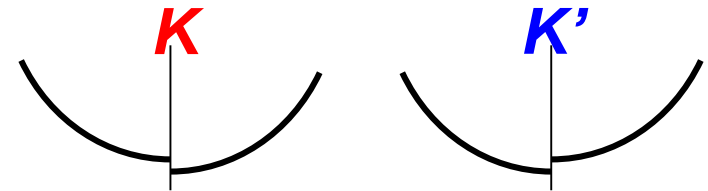
There are many interesting ultrafast studies of the fs & ps dynamics of excitons ( $K \rightarrow K'$  scattering, coherence effects, etc...)

# A very different (& very important!) question: Spin/valley dynamics of *resident electrons* & *holes*?

## Electron-doped (*n*-type) regime



## Hole-doped (*p*-type) regime



**Expectation of robust spin/valley polarization for  
resident *holes* (“spin-valley locking”)**

D. Xiao *et al.* PRL **108**, 196802 (2012)

## Three pathways for electrons...

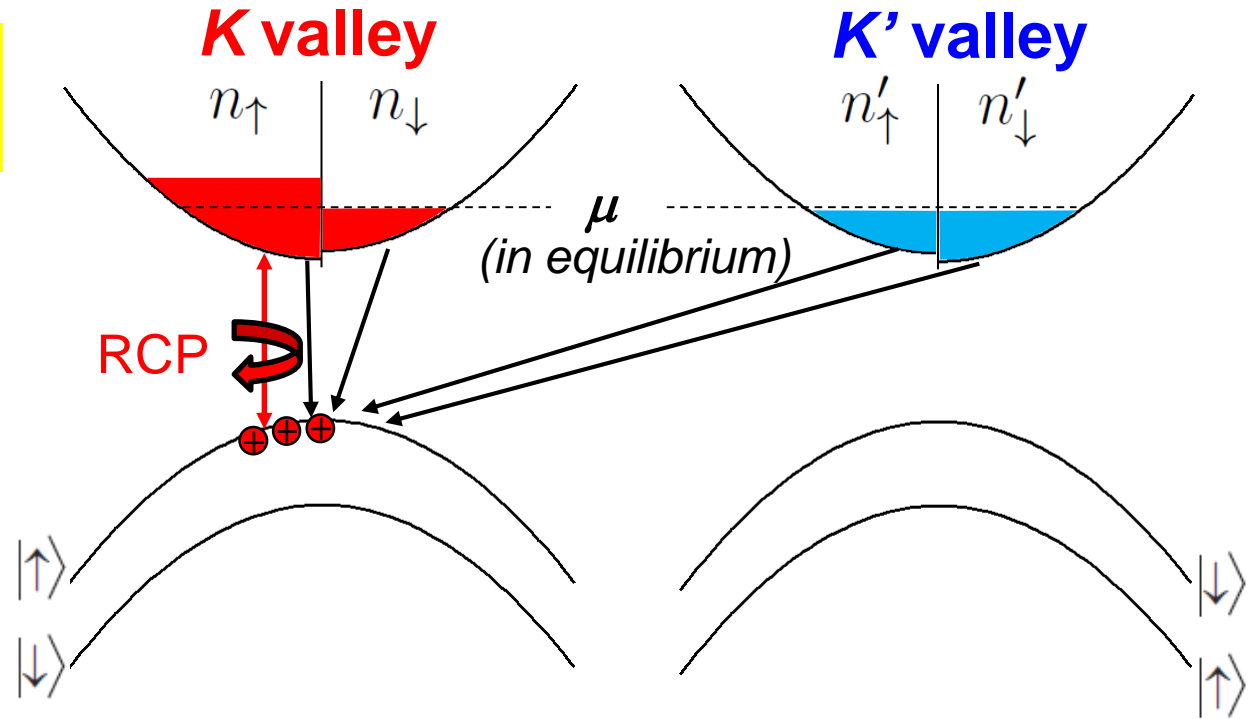
- 1) spin scattering within a valley
- 2) spin-*conserving* intervalley
- 3) spin-*flip* intervalley (slow)

## ONE pathway for holes...

- 1) spin-*flip* intervalley (slow)

# How to measure dynamics of *resident* carriers?

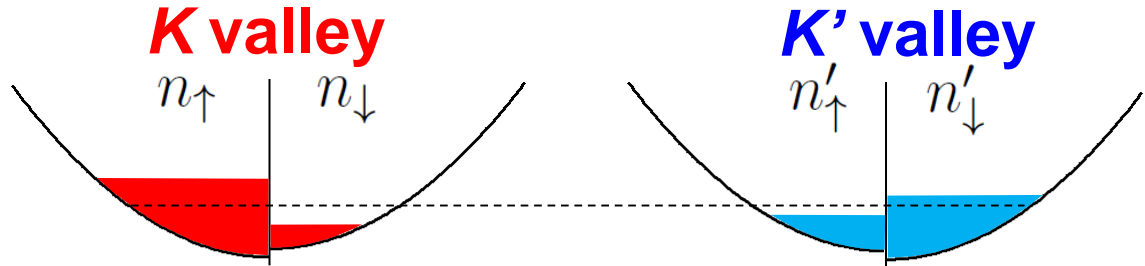
Conventional pump-probe  
(ultrafast optical) method:



- **$t < 0$** : resident carriers in equilibrium ( $\mu_{\uparrow} = \mu_{\downarrow} = \mu'_{\uparrow} = \mu'_{\downarrow}$ )
- **$t = 0$** : pump **RCP** at 'A' exciton
- **$t \sim 0-100$  ps**: minority carriers recombine with resident carriers (*i.e.*, excitons & trions form & recombine)

# How to measure dynamics of *resident* carriers?

Conventional pump-probe  
(ultrafast optical) method:



**Physics goal:**  
**Measure spin & valley relaxation of these resident e- (or h+).**  
**Time scales may be very long!**

$|\downarrow\rangle$

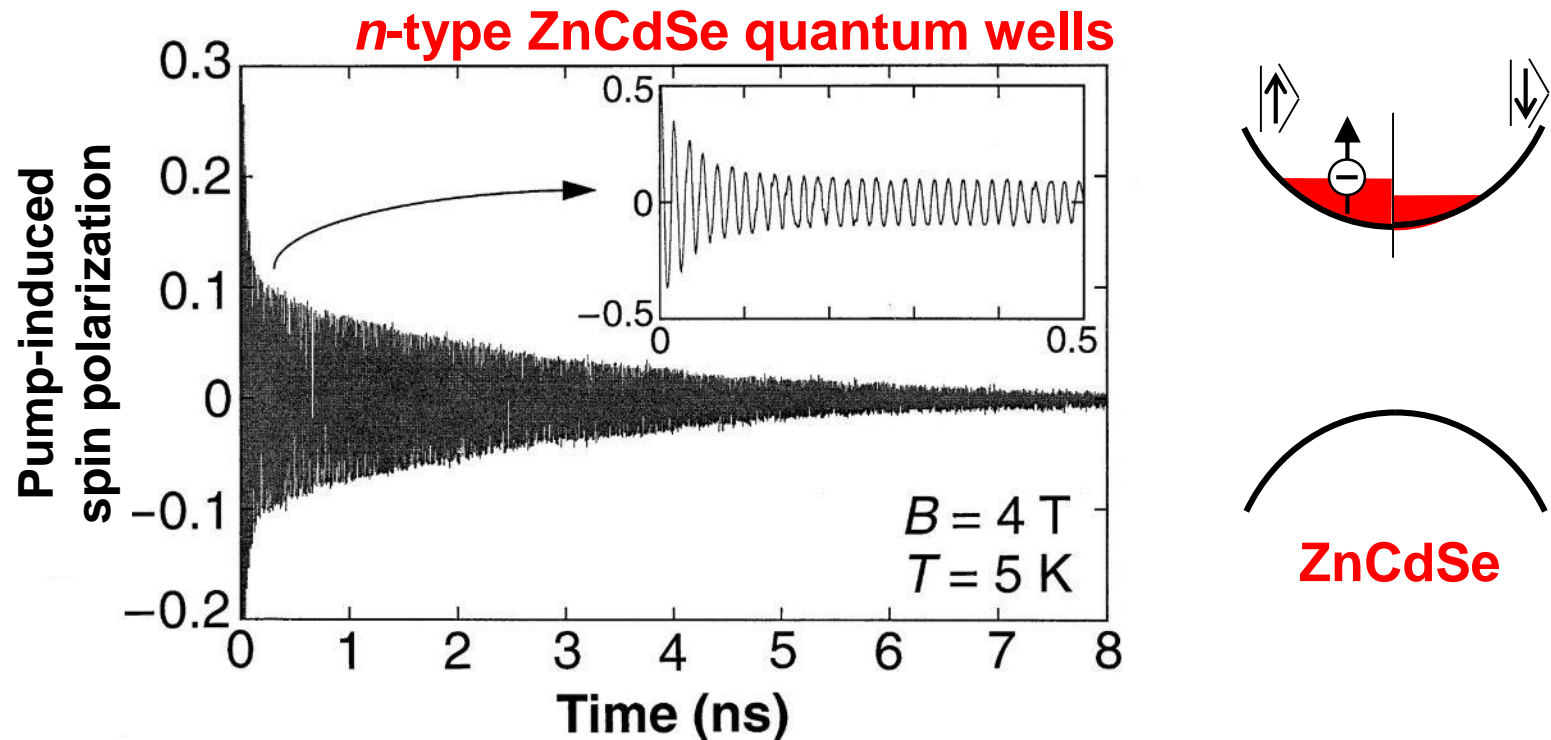
$|\uparrow\rangle$

**Key point:**  
 **$t > 100$  ps:** Non-equilibrium resident carriers *only*  
 $\mu_{\uparrow} \neq \mu_{\downarrow} \neq \mu'_{\uparrow} \neq \mu'_{\downarrow}$   
Spin polarization:  $S_z = n_{\uparrow} + n'_{\uparrow} - n_{\downarrow} - n'_{\downarrow}$   
Valley polarization:  $N_v = n_{\uparrow} + n_{\downarrow} - n'_{\uparrow} - n'_{\downarrow}$

# Historical interlude: early days of “spintronics”

“Room temperature spin memory in 2D electron gases”

Kikkawa, Samarth, Smorchkova, Awschalom, *Science* **277**, 1284 (1997)



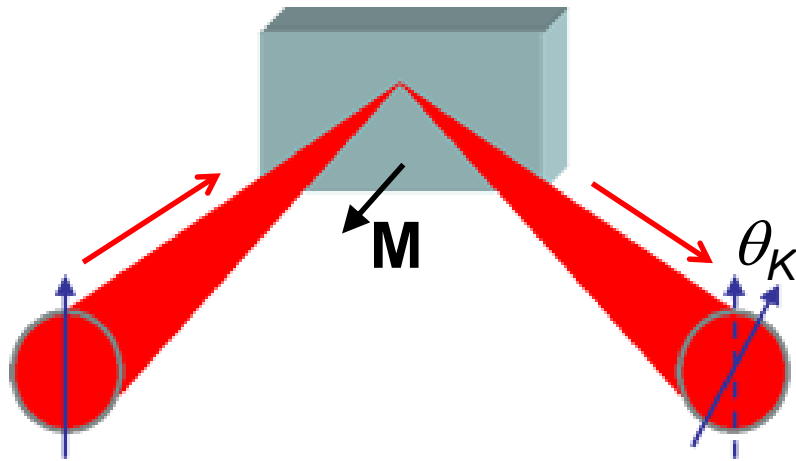
Exciton lifetime: <50 ps

Spin lifetime of resident electrons: 5 ns ! (At room temp!)

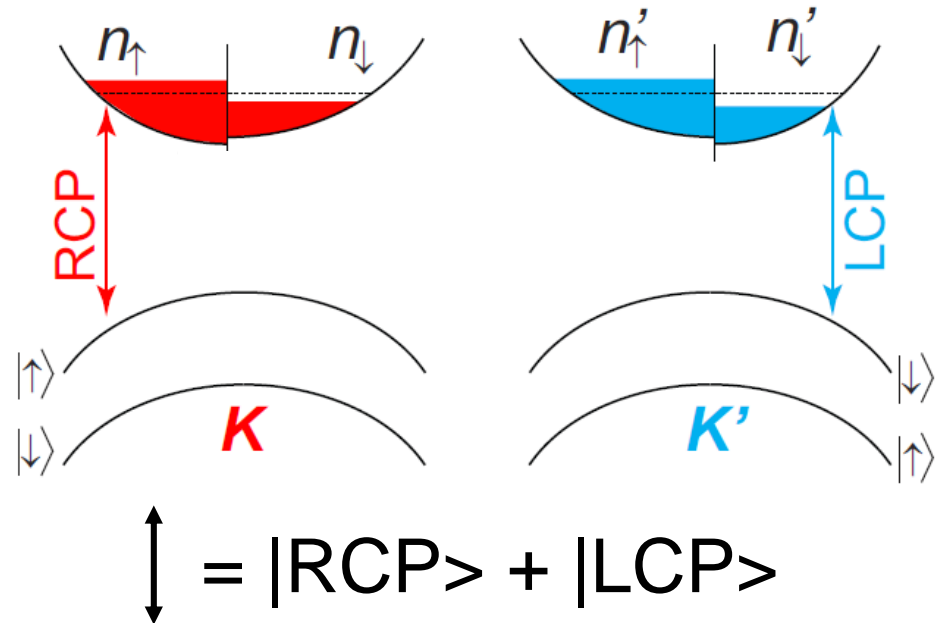


# Detection: optical Kerr/Faraday rotation

A direct probe of the resident carrier polarization



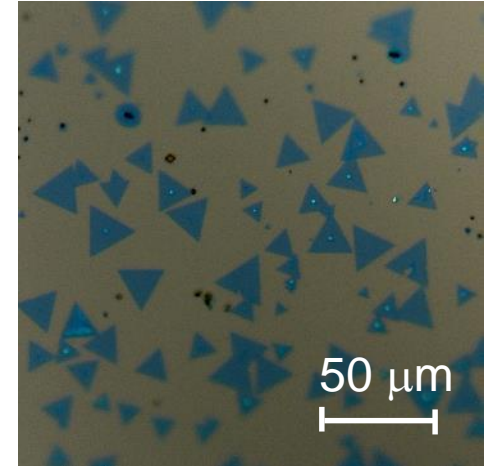
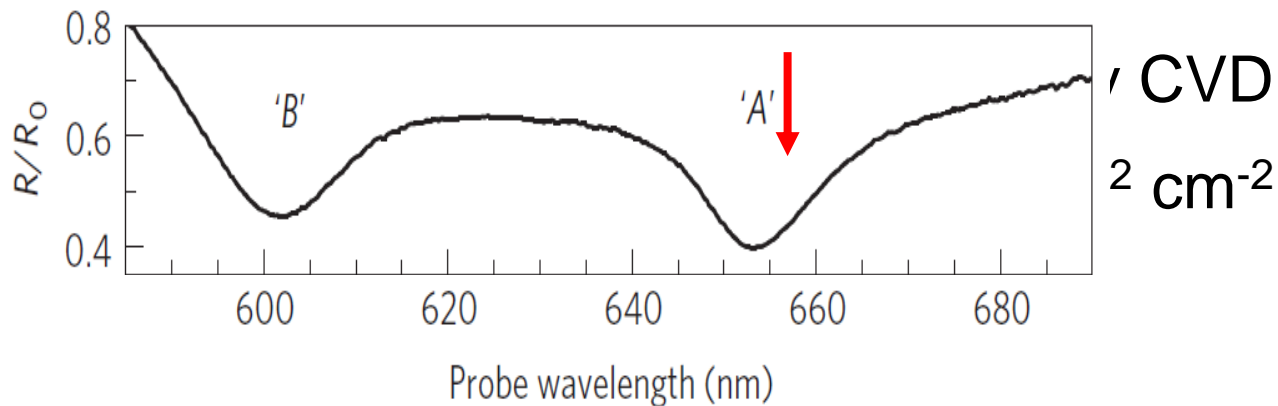
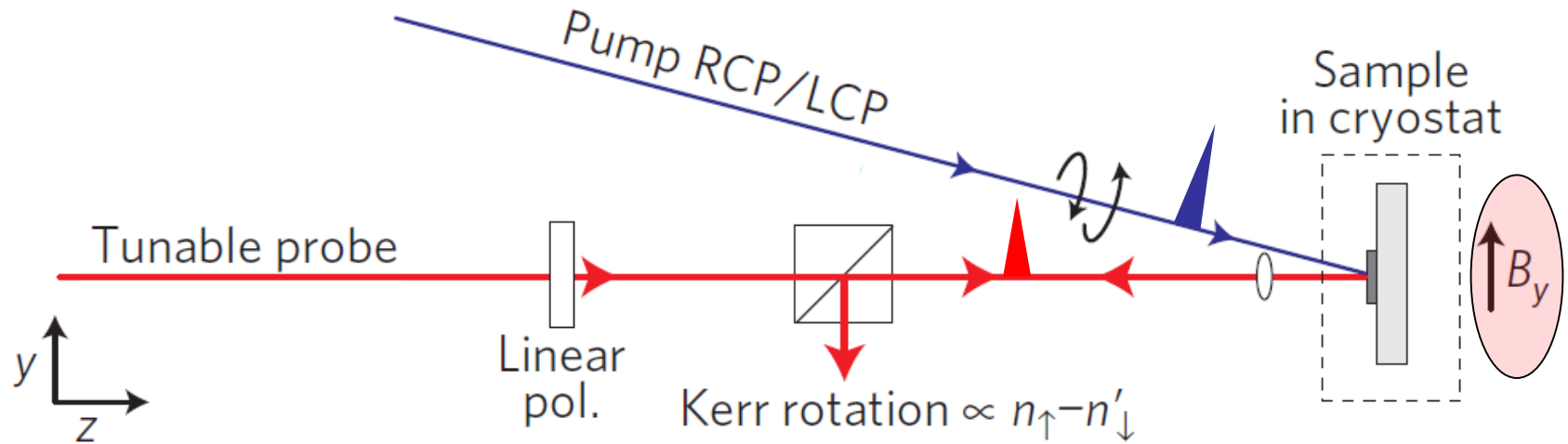
Optical Kerr rotation,  $\theta_K$   
 $\propto (\alpha_{\text{RCP}} - \alpha_{\text{LCP}})$



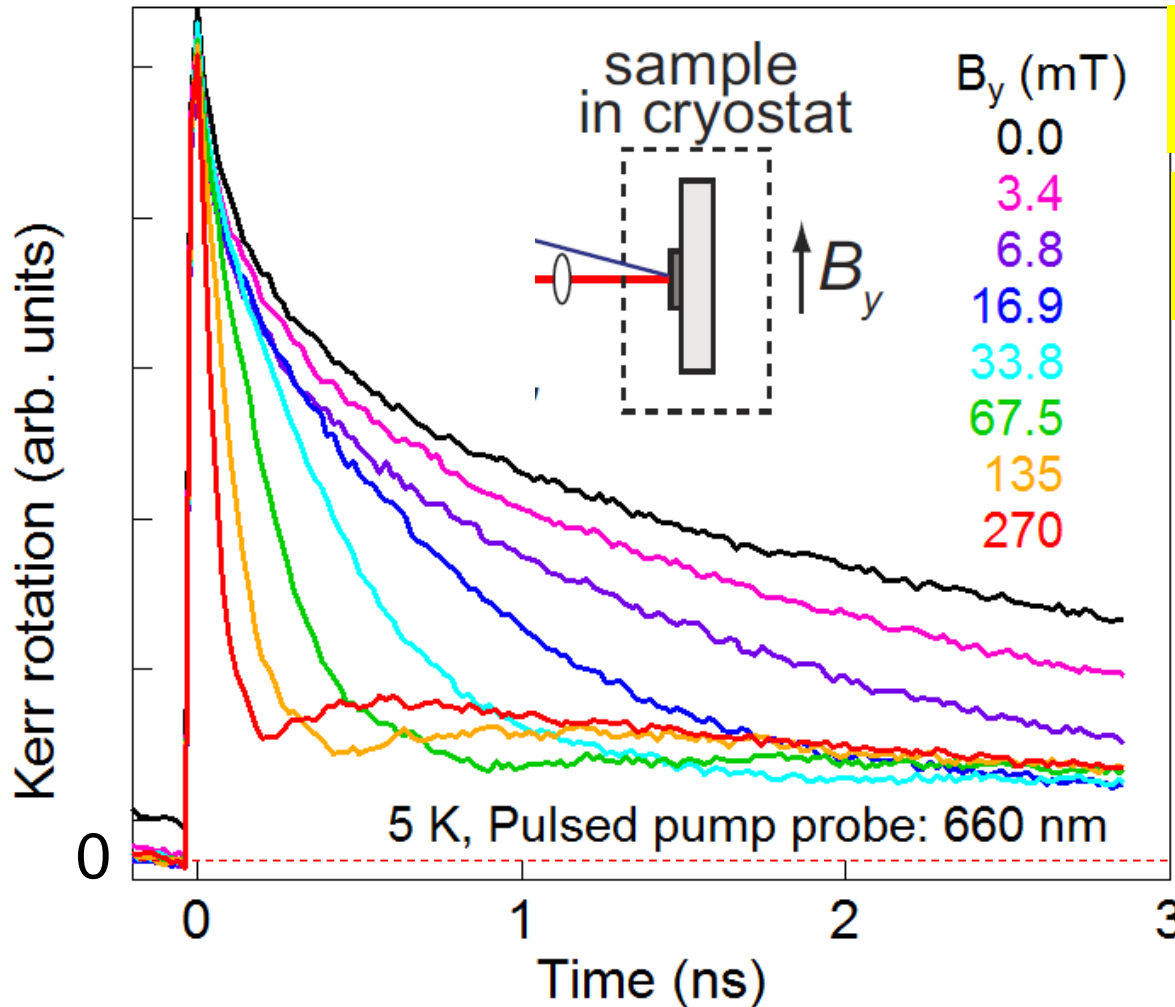
$$\theta_K \sim (n_\uparrow - n'_\downarrow) \sim (S_z + N_v)/2$$

Measure carrier spin/valley polarization...  
**...long after minority species are gone**

# Experiment: Time-resolved Kerr rotation of MoS<sub>2</sub>



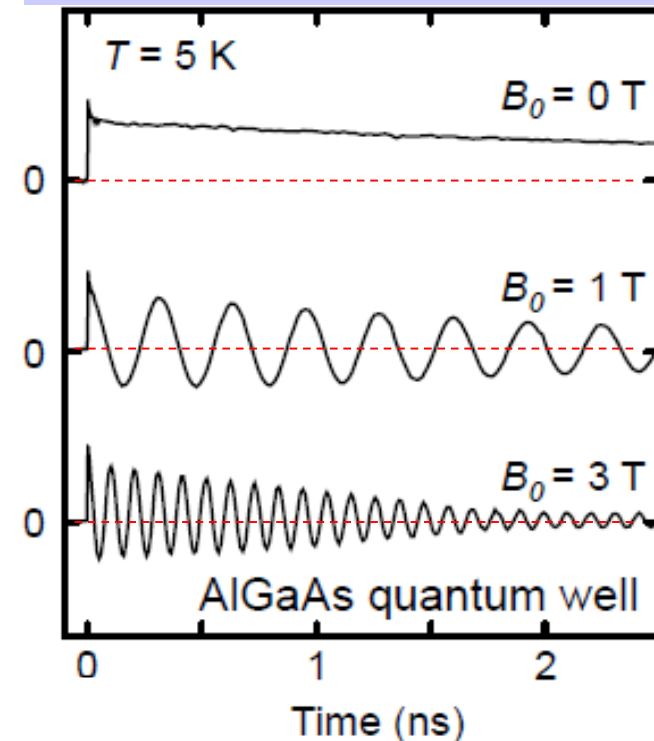
# Time-resolved Kerr rotation of MoS<sub>2</sub>



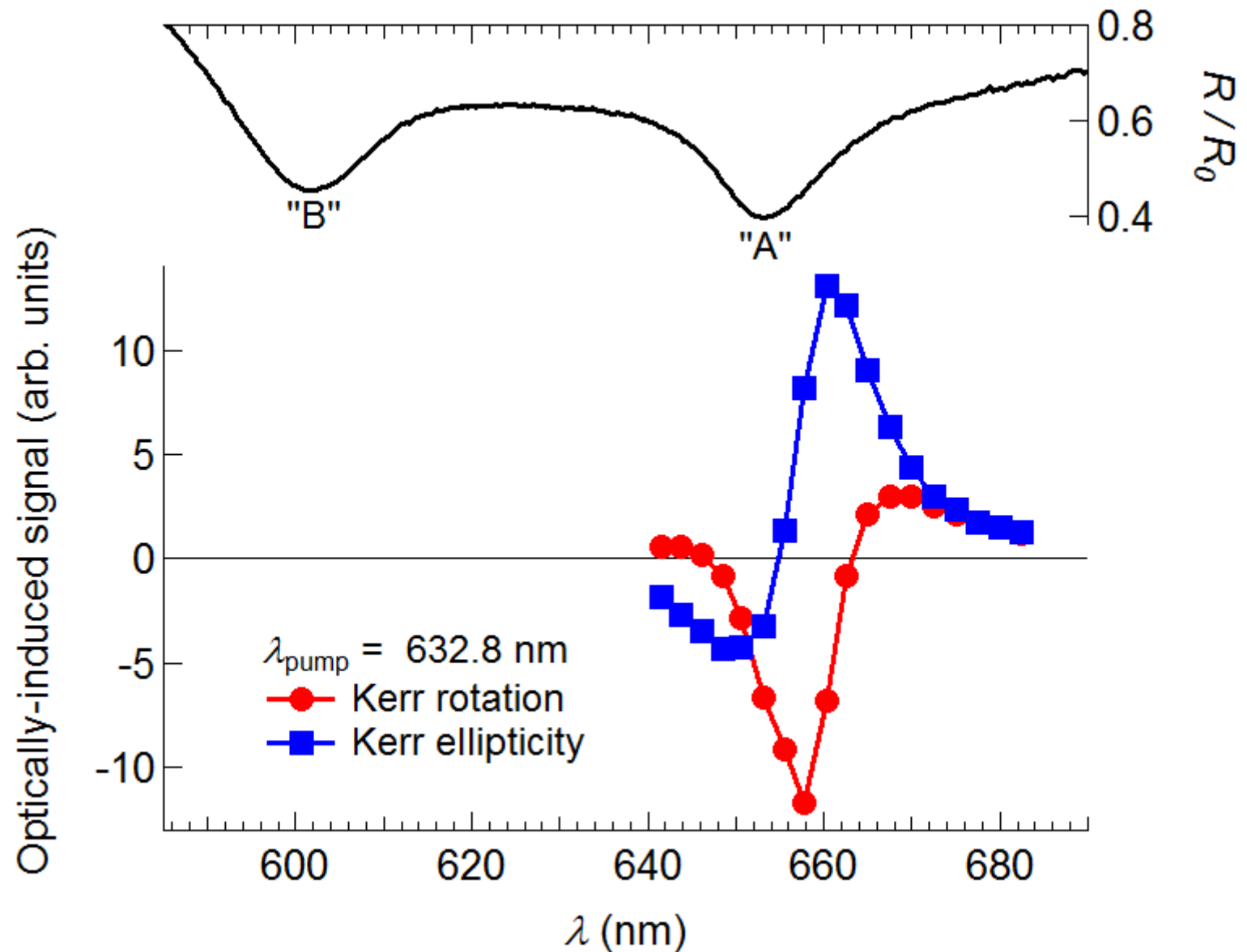
- $\sim 3$  ns decay at  $B_y = 0$
- small  $B_y$ : faster decay (spin relaxation)

• **BUT**: no prominent spin precession.

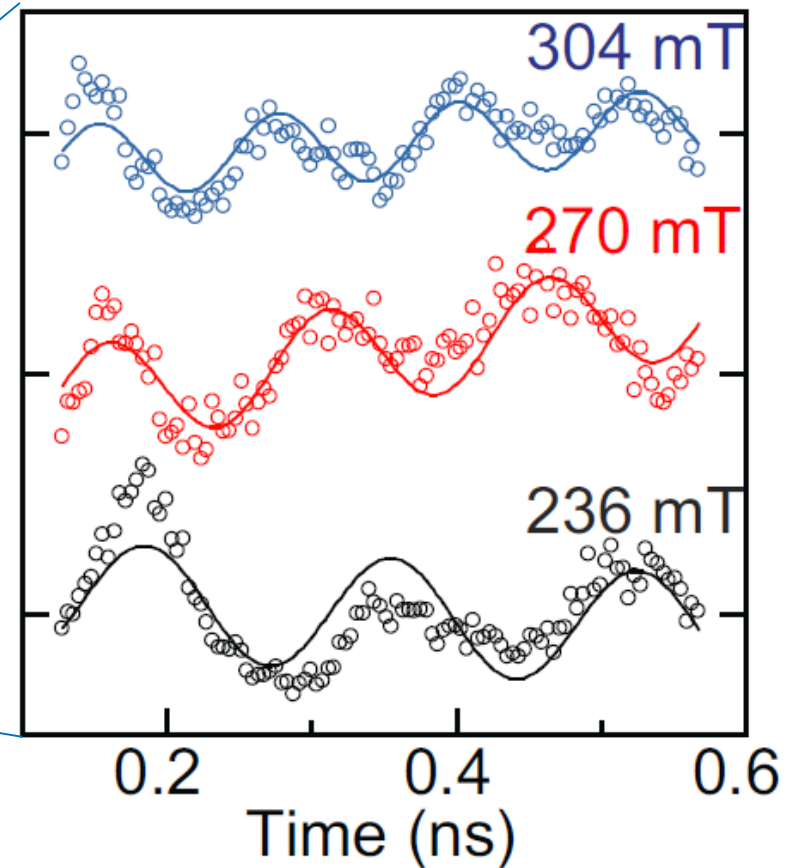
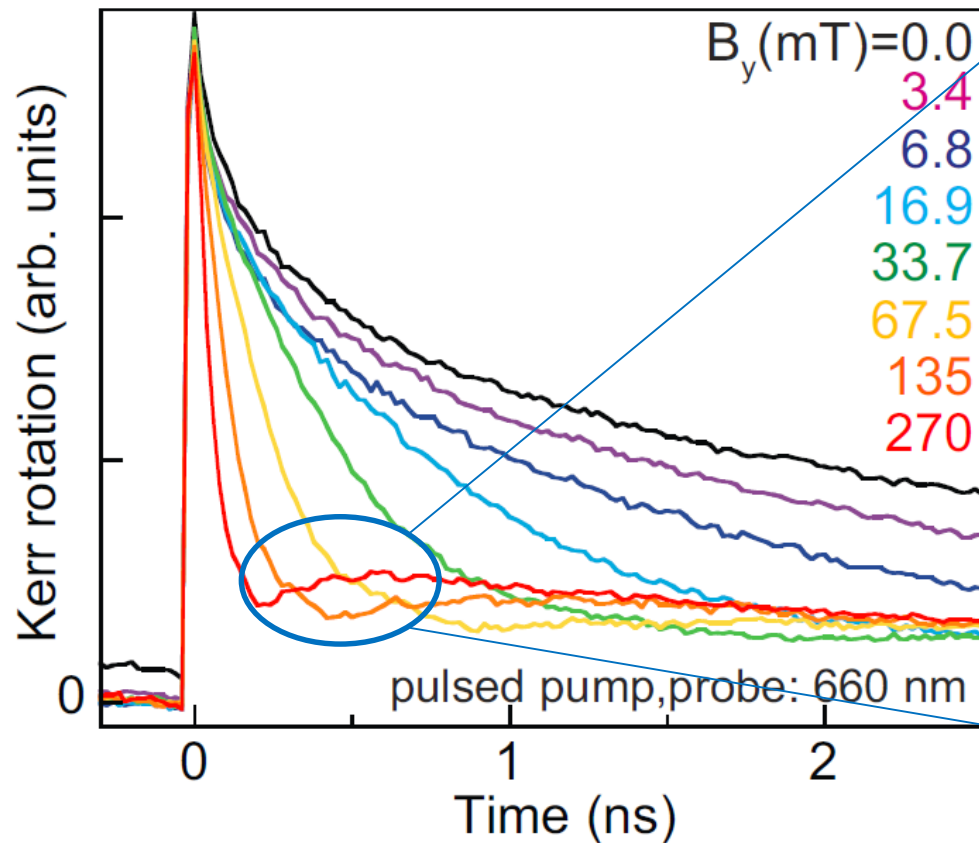
*Different than, e.g., GaAs*



# Spectral dependence of Kerr signals



# Actually... some (tiny) coherent spin precession



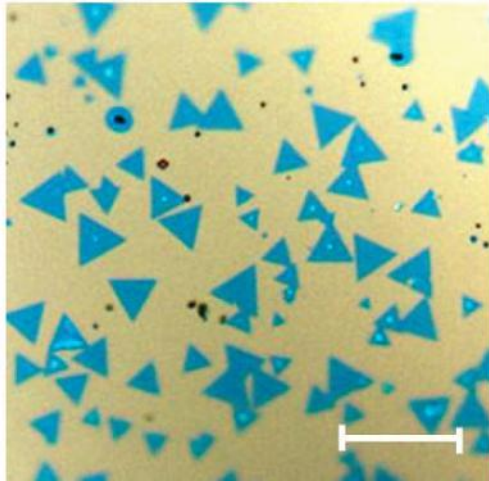
**Some electrons undergo coherent spin precession.**

**Localized electrons?**



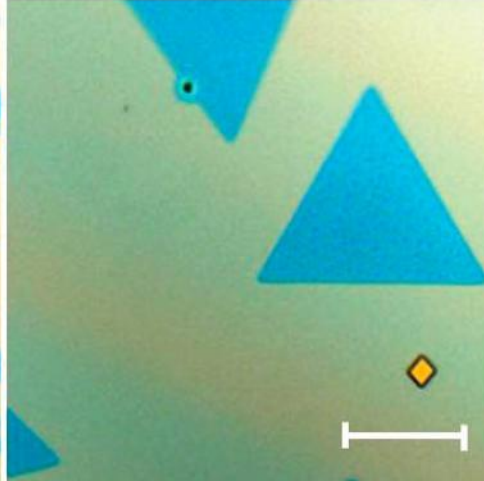
# Different MoS<sub>2</sub> samples grown by CVD

sample 1



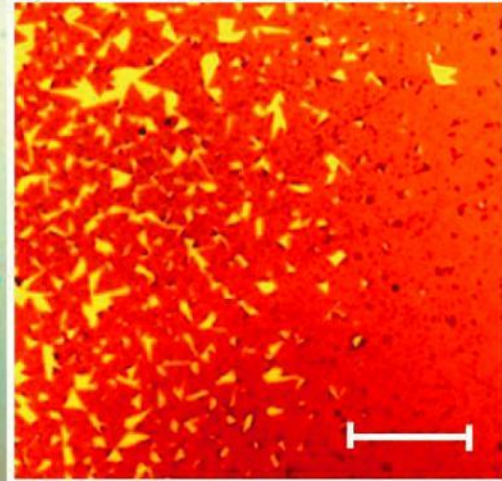
Rice U.

sample 2



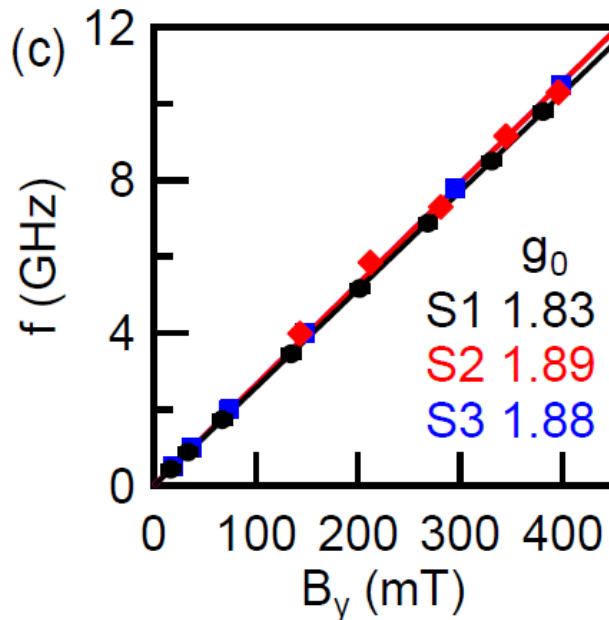
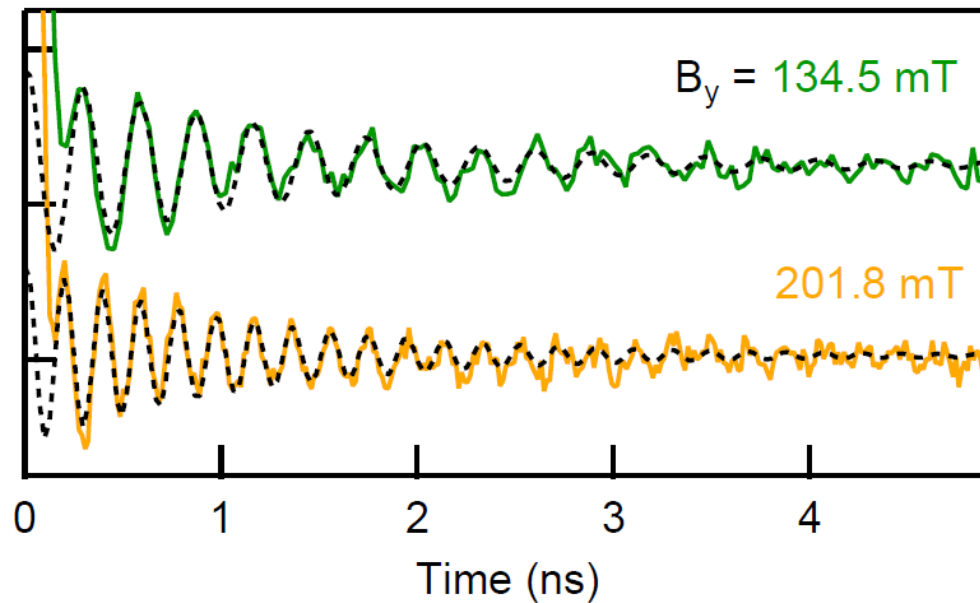
Rice U.

sample 3



NRL

# Coherent spin precession of (localized?) electrons



Spin coherence persists for nanosec.

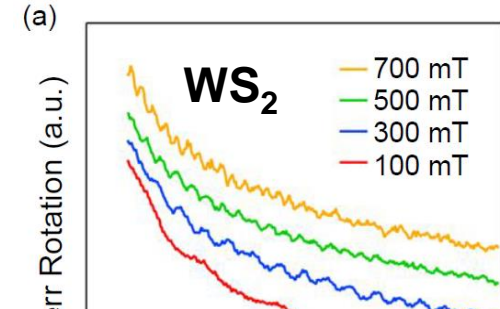
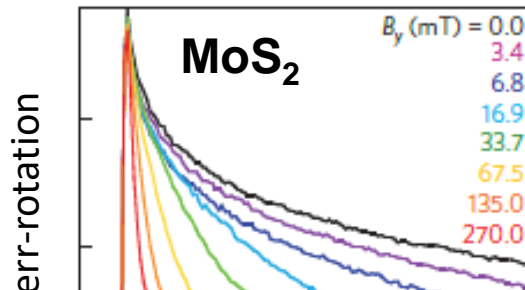
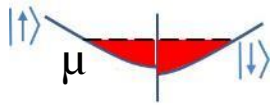
Precession frequency increases *linearly* with applied field:  **$g \sim 1.85$**

Sub-ensemble of localized electrons?

Nano Letters **15**, 8250 (2015)

# Initial studies of resident carrier dynamics

***n*-type**

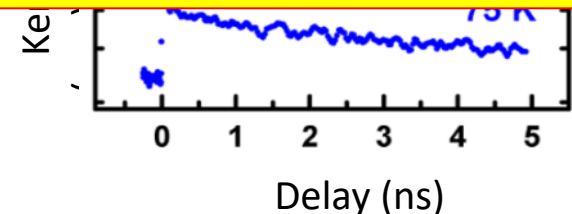
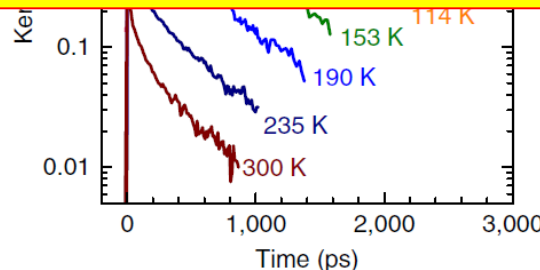


***However...***

- CVD-grown monolayers (*not exfoliated crystals*)
- Background carrier densities were fixed & not tunable
- Due to uncontrolled impurities
- Systematic trends difficult to identify

***p*-type**

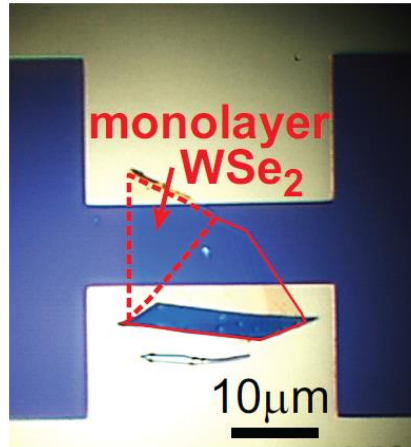
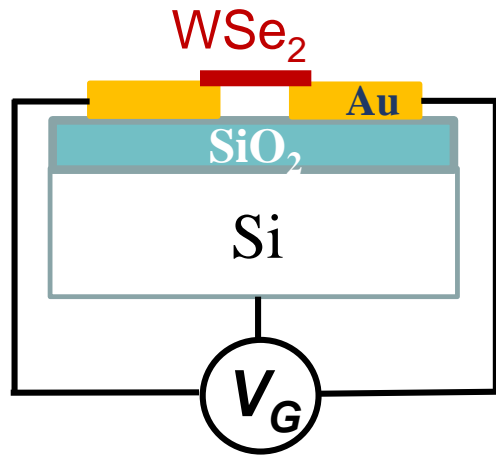
**Need: Dynamic studies in a single *charge-tunable* gated device**



Hsu, *Nat. Comm.* **6**:8963 (2015)

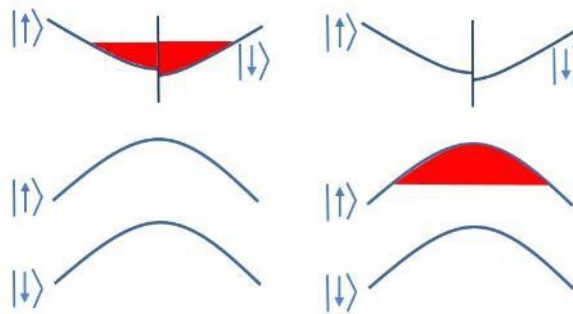
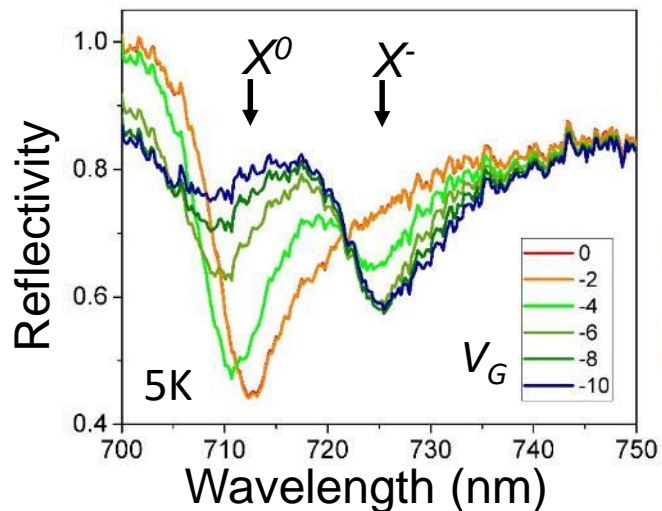
Song, *Nano Lett.* **16**, 5010 (2016)

# Gated single monolayers of exfoliated $\text{WSe}_2$

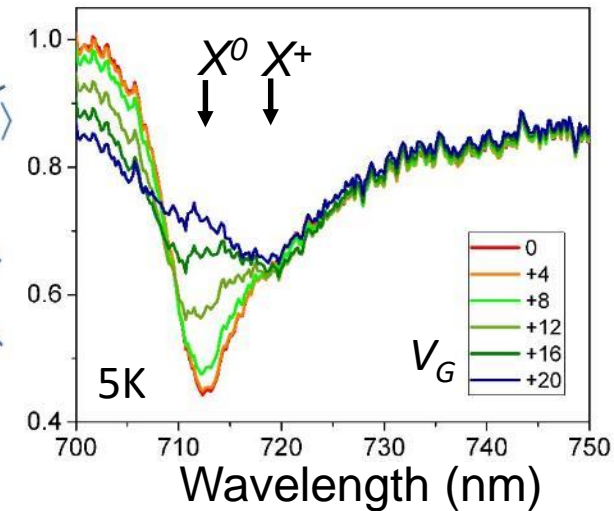


Cedric Robert  
(INSA-Toulouse)

## Electron-doped regime

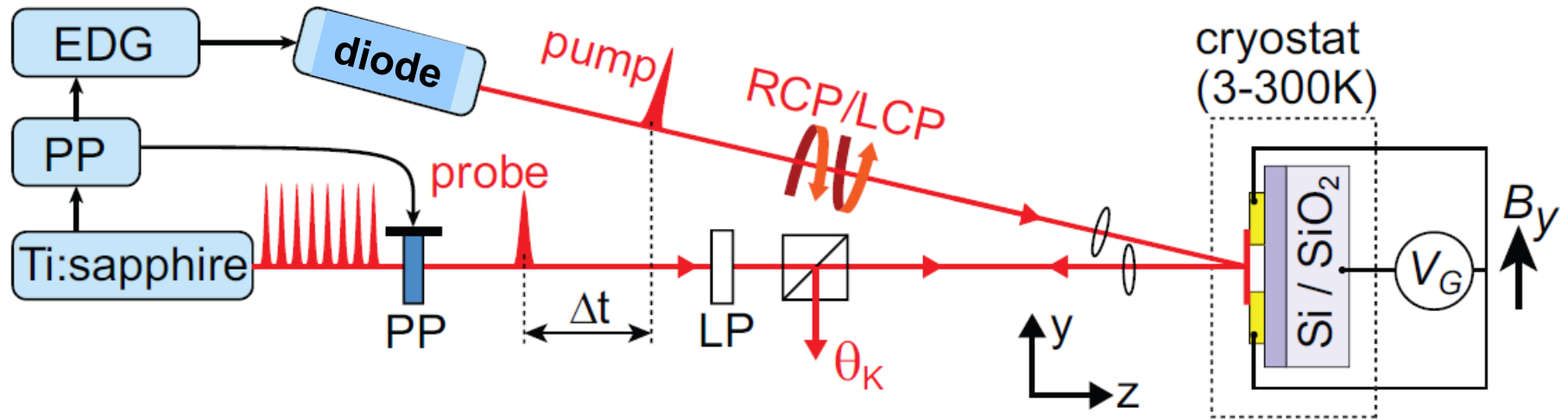


## Hole-doped regime



# Experiment: Time-resolved Kerr rotation

P. Dey *et al.*, PRL **119**, 137401 (2017)



## Important modifications:

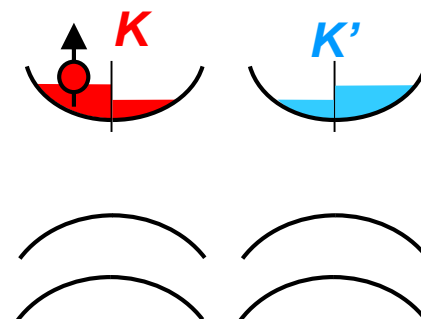
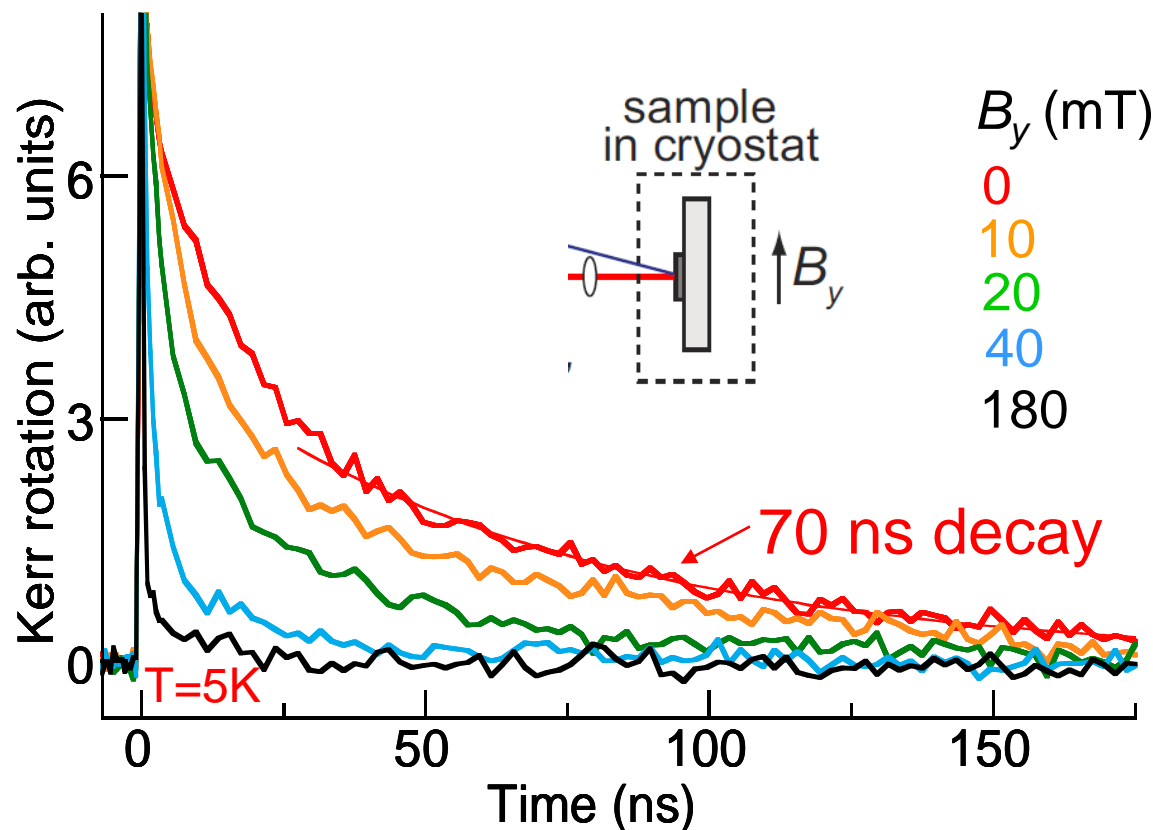
- Pulse Picker (to reduce Ti:S repetition rate)
- Electronic Delay Generator (to achieve arbitrary time delays)

**Allows direct access to microsecond-long pump-probe delays**



# Electron-doped ( $n$ -type) regime:

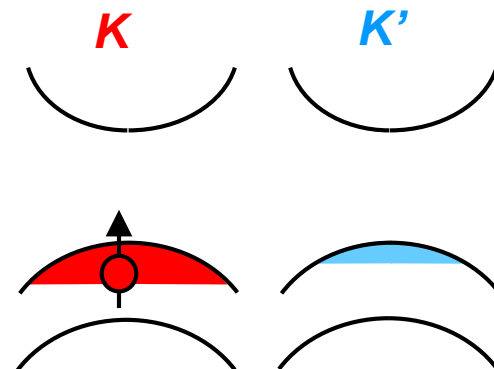
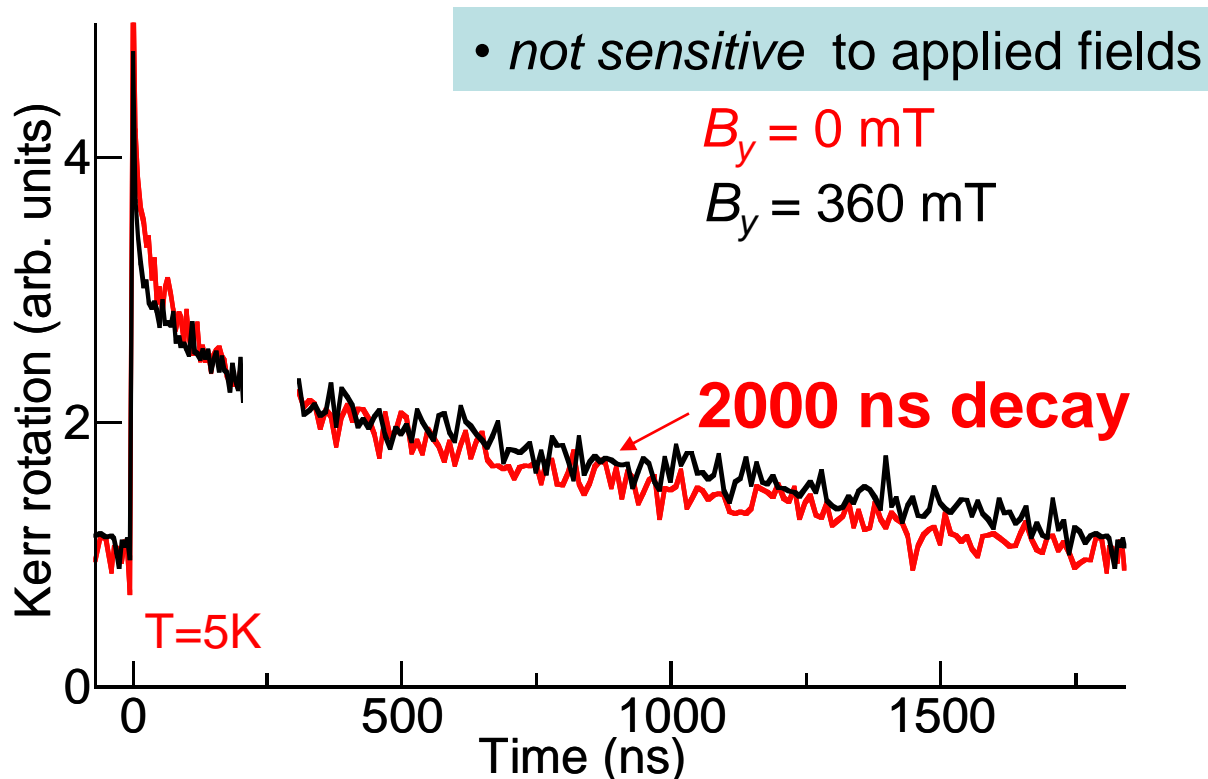
- 70 ns decay at  $B_y=0$
- small  $B_y$ : much faster decay (spin effect)



# Hole-doped ( $p$ -type) regime:

- *Extremely* long 2 microsecond polarization decay of holes at  $B_y=0$

P. Dey *et al.*, PRL **119**, 137401 (2017)



- Consistent with spin-valley locking in valence band
- Suggests holes for exceptionally robust spin/valley polarization storage

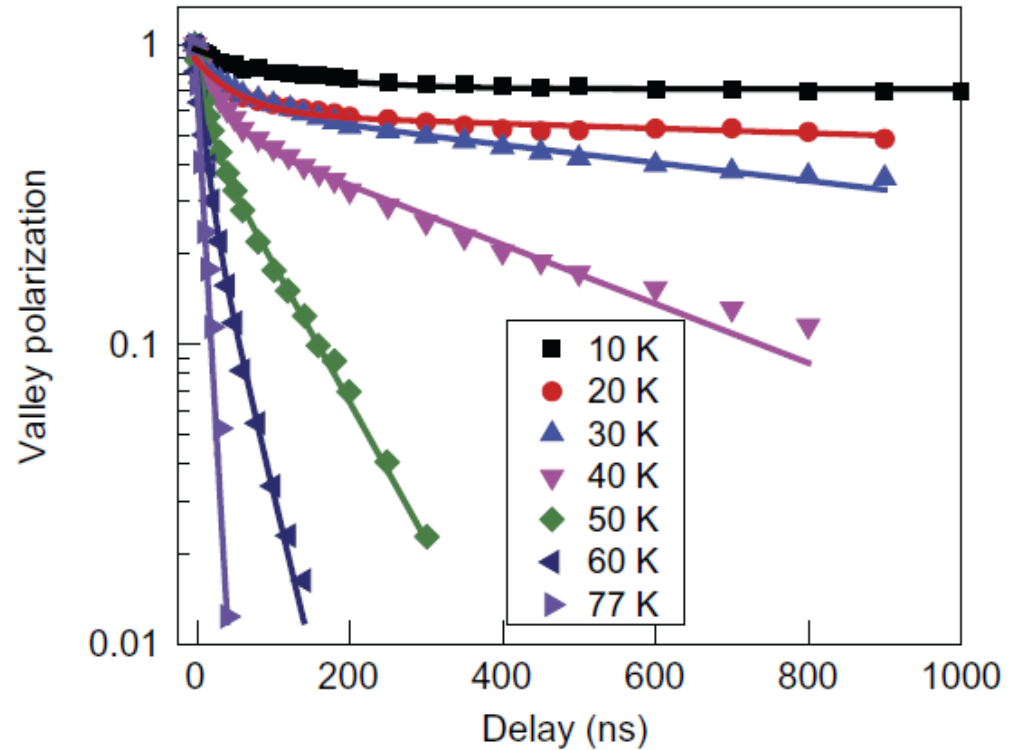
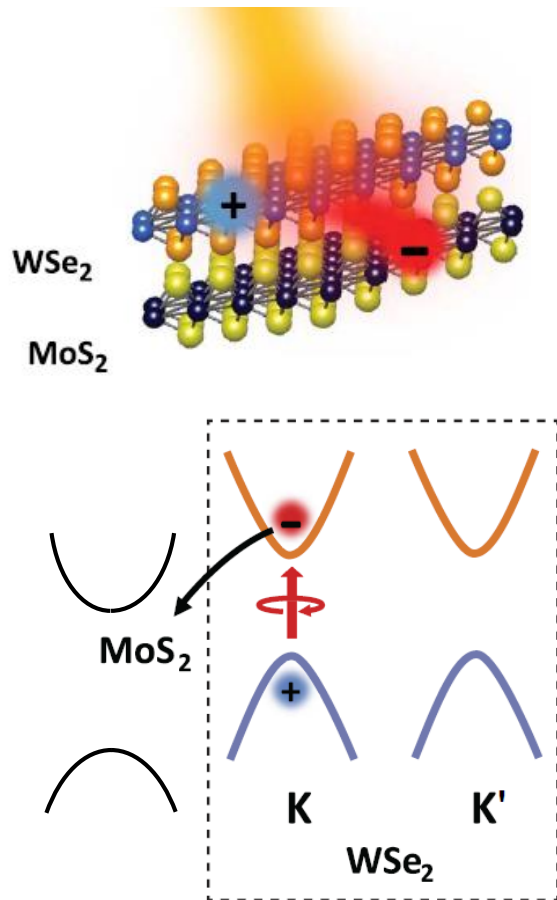
Also... J. Kim, F. Wang *et al.*, Sci. Adv. **3**, e1700518 (2017)

Also:

## Observation of ultralong valley lifetime in WSe<sub>2</sub>/MoS<sub>2</sub> heterostructures

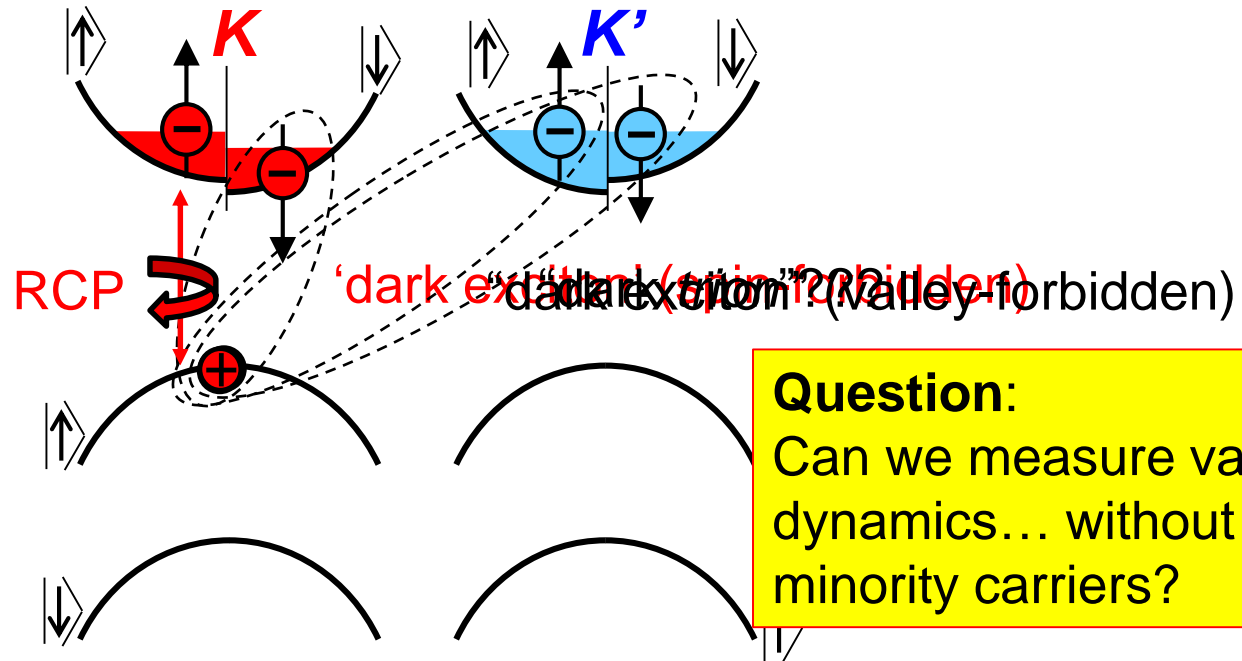
Jonghwan Kim,<sup>1,2\*</sup> Chenhao Jin,<sup>1\*</sup> Bin Chen,<sup>3</sup> Hui Cai,<sup>3</sup> Tao Zhao,<sup>1</sup> Puiyee Lee,<sup>1</sup> Salman Kahn,<sup>1</sup> Kenji Watanabe,<sup>4</sup> Takashi Taniguchi,<sup>4</sup> Sefaattin Tongay,<sup>3</sup> Michael F. Crommie,<sup>1,5,6</sup> Feng Wang<sup>1,5,6†</sup>

Science Advances **3**, e1700518 (2017)



# Lingering concerns: Pump-probe is *perturbative*

## Question: role of (long-lived?) “dark” excitons & trions



### Question:

Can we measure valley dynamics... without pumping minority carriers?

### Evidence for “dark” (or at least “grey”) excitons:

Zhang, Heinz *et al.*, Nature Nano. **12**, 883 (2017)

Zhou *et al.*, Nature Nano. **12**, 856 (2017)

Molas *et al.*, 2D Materials **4**, 021003 (2017)

Wang *et al.*, PRL **119**, 047401 (2017)

And now  
for something  
completely different...



**Question:**

Can we measure valley dynamics... without pumping minority carriers?



# “Noise spectroscopy”: a simple example

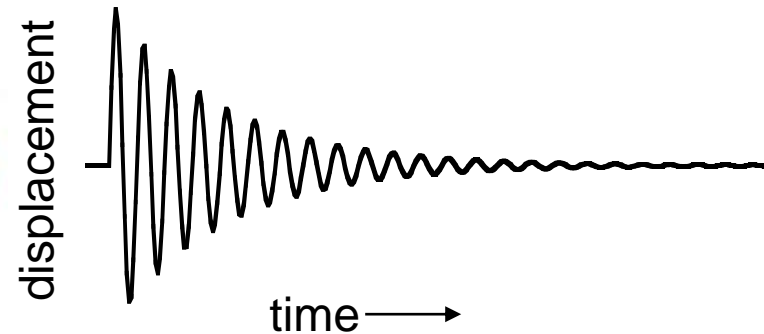
## Simple mechanical system: Cantilever (diving board)

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- What's resonant frequency ( $\omega_0$ )?
- What's ringdown time (Q)?



Method 1  
Perturbative methods...  
Measure dissipative response



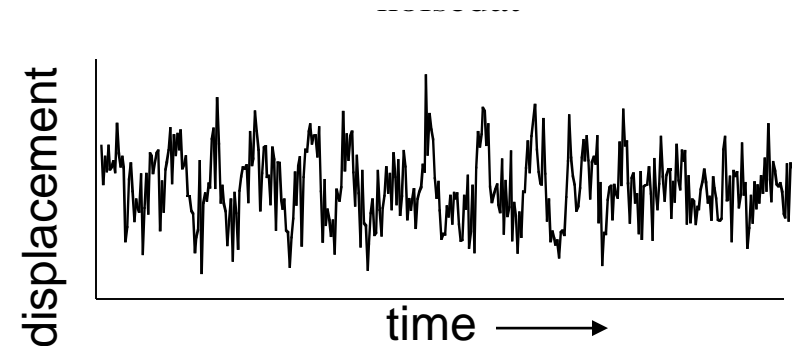
# “Noise spectroscopy”: a simple example

## Simple mechanical system: Cantilever (diving board)

- What's resonant frequency ( $\omega_0$ )?
- What's ringdown time (Q)?

### Method 2

“Listen” carefully to intrinsic thermal fluctuations (vibration noise)  
Measure  $\langle \delta x(0) \delta x(t) \rangle$



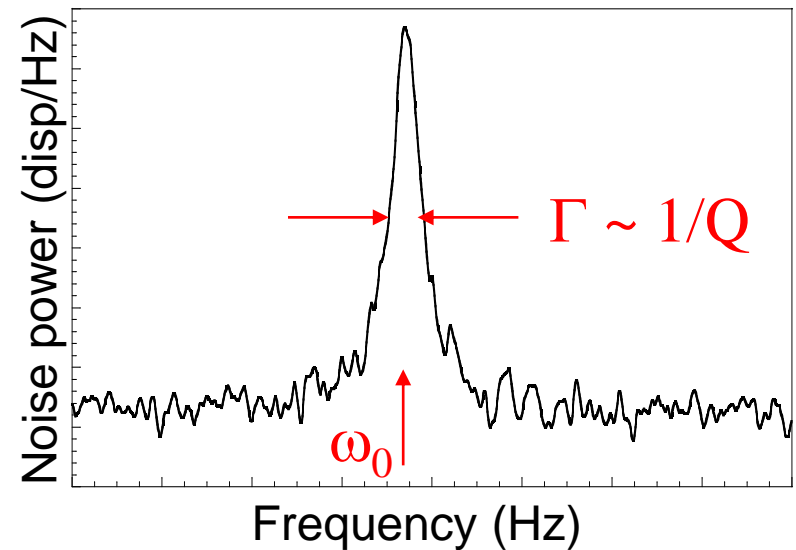
# “Noise spectroscopy”: a simple example

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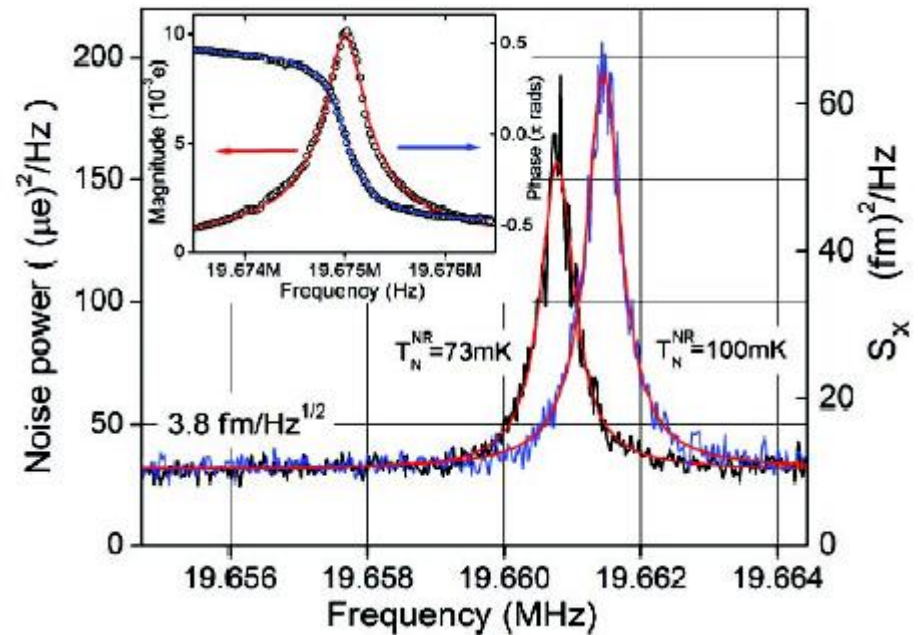
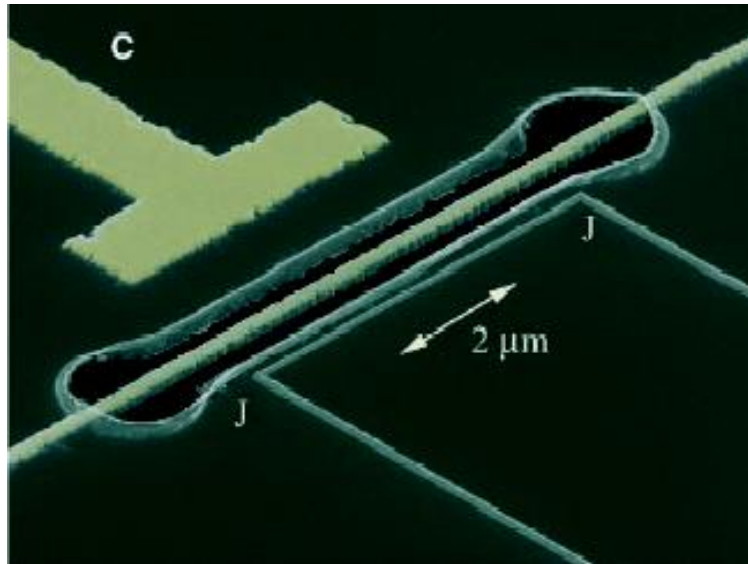
Fluctuation-Dissipation Theorem:

‘Spectrum of fluctuations completely describes the driven response’



# Nanometer-scale diving board (mechanical resonator)

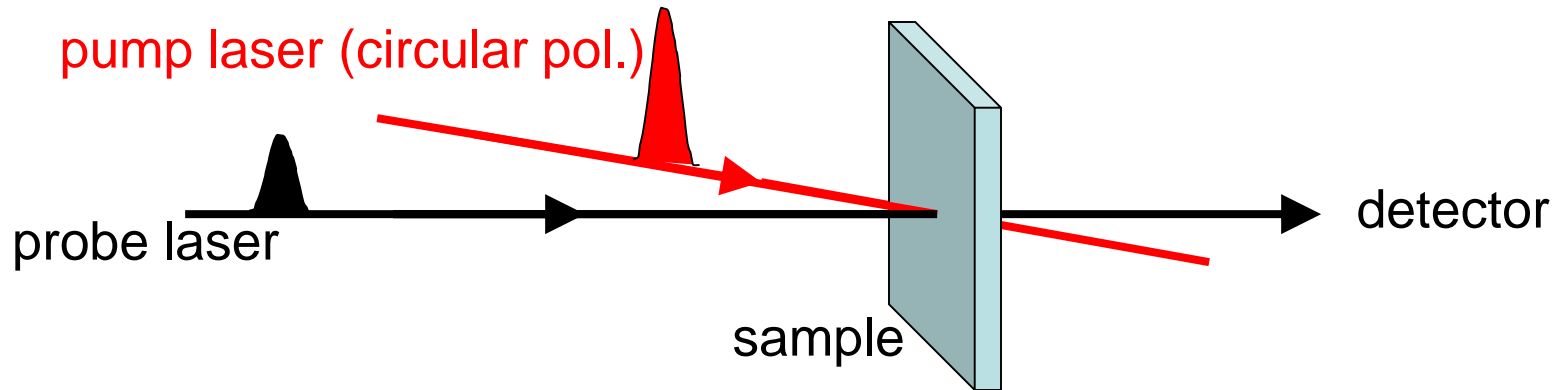
K. Schwab (Science, 2004)



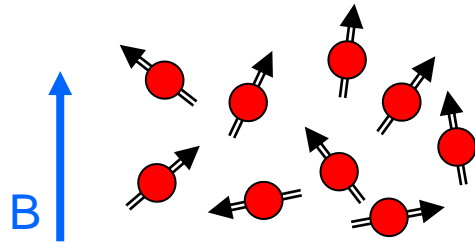
**\*\* Noise signatures become an increasing fraction of “driven” signal as things get small \*\***

# Magnetic analogy: stochastic 'spin noise'

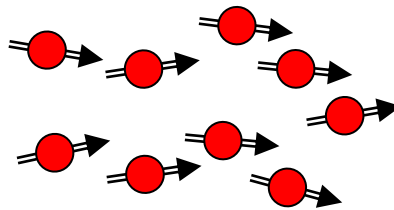
Normally, spin dynamics revealed with spin-resonance (NMR, ESR), pump-probe optics: techniques are necessarily perturbative



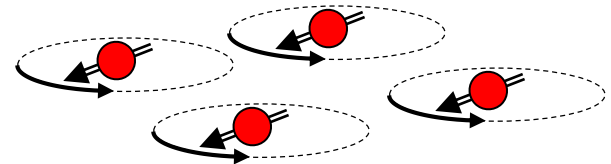
Start with spins in thermal equilibrium...



...then inject (or tip, or pump, etc...)

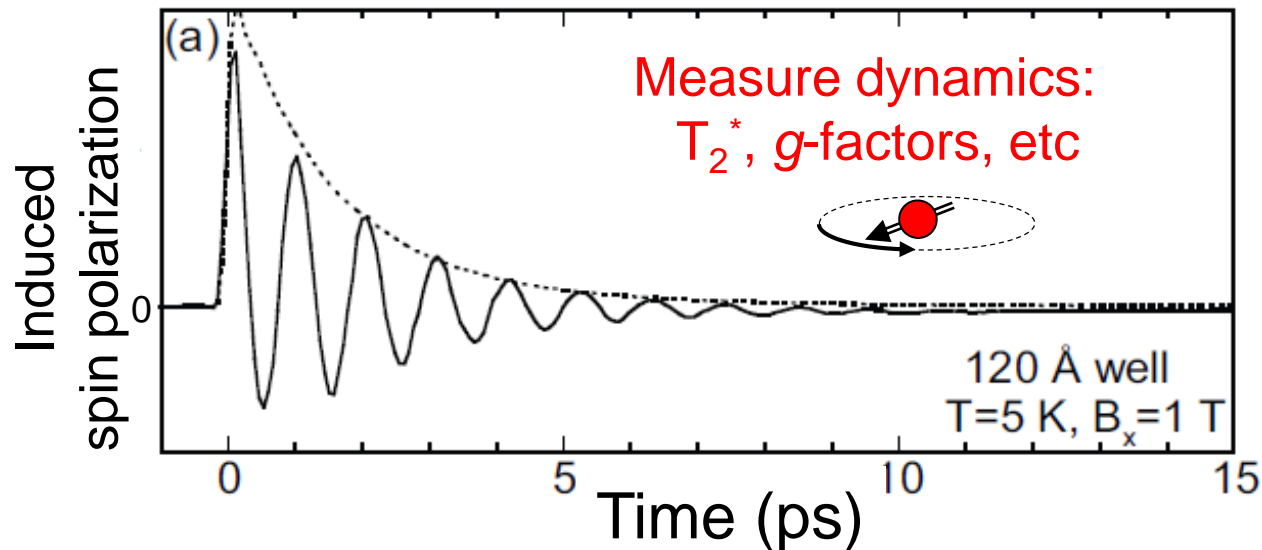
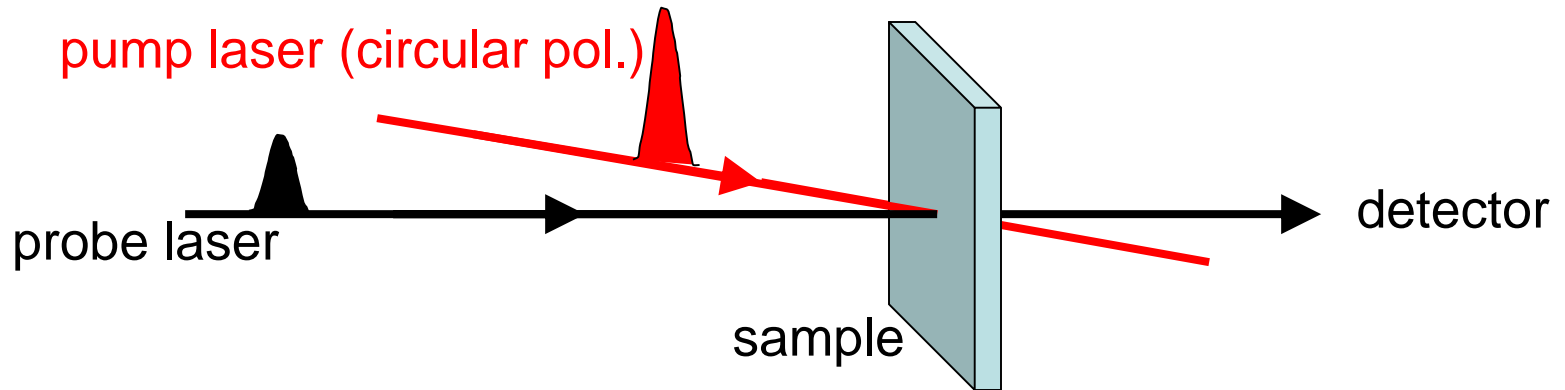


...then measure (dissipative) response



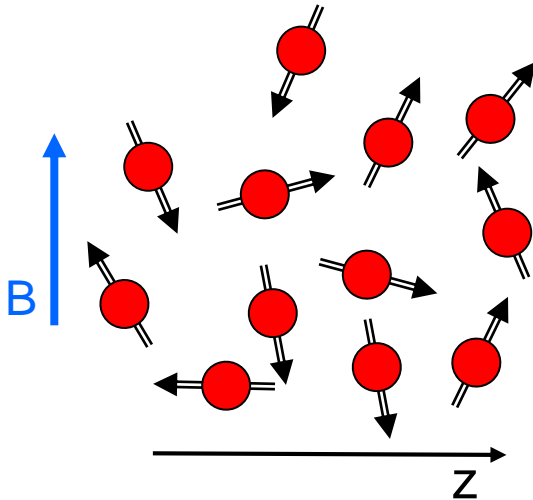
# Magnetic analogy: stochastic 'spin noise'

Normally, spin dynamics revealed with spin-resonance (NMR, ESR), pump-probe optics: techniques are necessarily perturbative

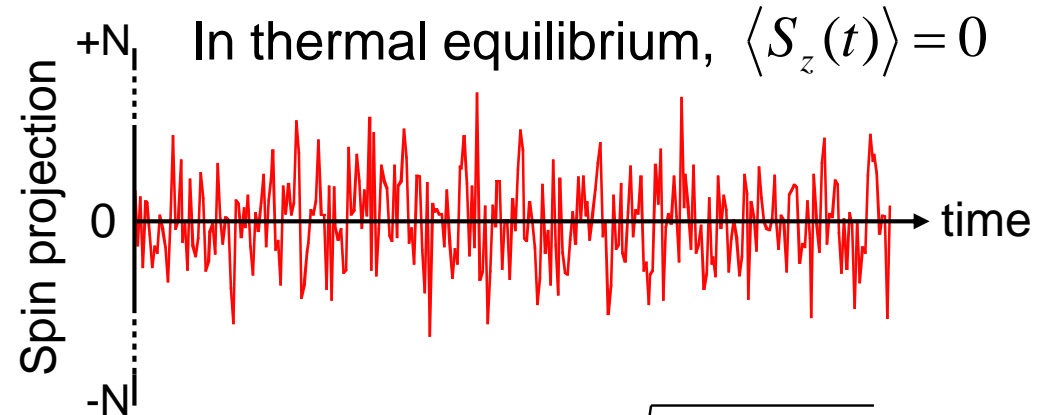


# Dynamics *also* available via stochastic “spin noise”

Consider  $N$  uncorrelated spins in equilibrium...

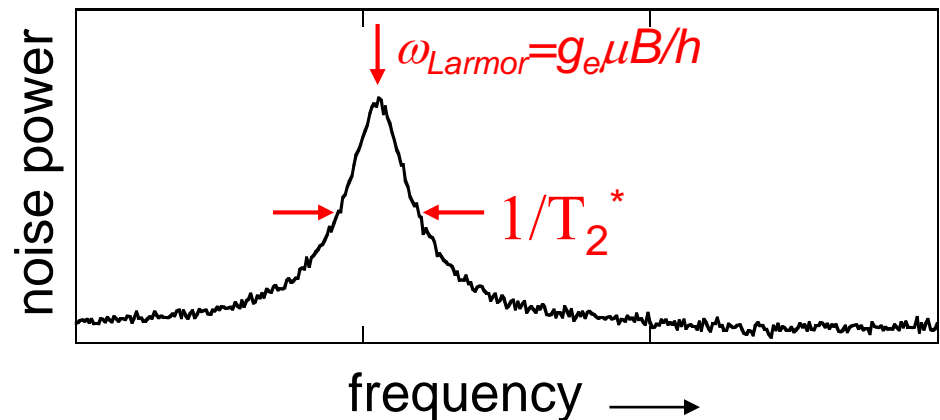


Spectrum of correlations:



But fluctuations exist:  $\sqrt{\langle [S_z(t)]^2 \rangle} \sim \sqrt{N}$

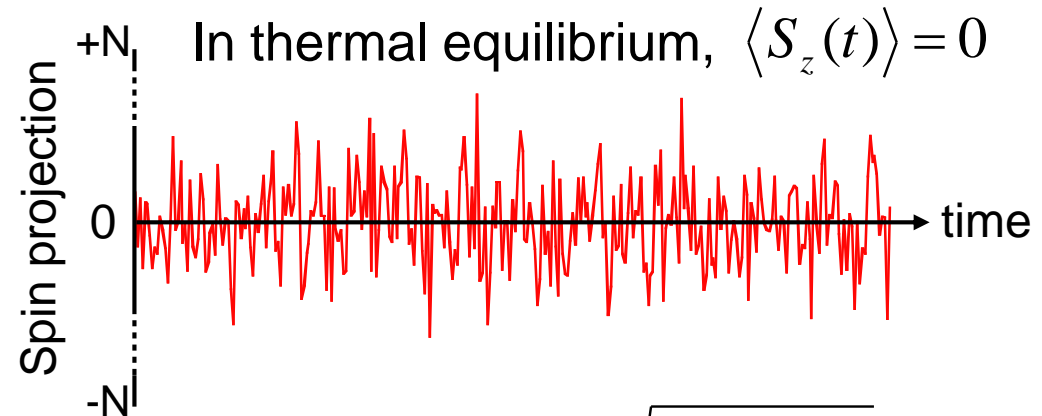
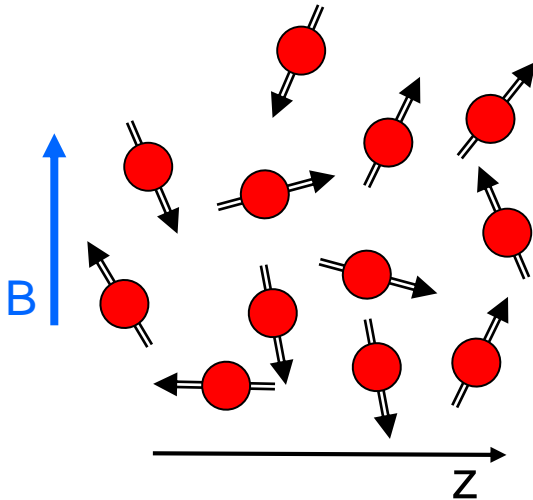
Correlation function:  $\langle S_z(t) S_z(0) \rangle$





# Dynamics *also* available via stochastic “spin noise”

Consider  $N$  uncorrelated spins in equilibrium...



But fluctuations exist:  $\sqrt{\langle [S_z(t)]^2 \rangle} \sim \sqrt{N}$

Correlation function:  $\langle S_z(t) S_z(0) \rangle$

Fluctuation-dissipation theorem:  $\chi''(\omega) \sim \int_{-\infty}^{\infty} \langle S_z(t) S_z(0) \rangle e^{-i\omega t} dt$

*“Linear response of a system to external perturbation (ie, the susceptibility) can be described by the fluctuation properties of the system while in thermal equilibrium”.*

- In principle: spin noise alone completely describes dynamics*



In 1946...

PHYSICAL REVIEW

VOLUME 70, NUMBERS 7 AND 8

OCTOBER 1 AND 15, 1946

## Nuclear Induction

F. BLOCH

*Stanford University, California*

(Received July 19, 1946)

on page 2... Even in the absence of any orientation by an external magnetic field one can expect in a sample with  $N$  nuclei of magnetic moment  $\mu$  to find a resultant moment of the order  $(N)^{1/2}\mu$  because of statistically incomplete cancellation. This moment, however, would naturally be very small



## Nuclear-Spin Noise

Tycho Sleator and Erwin L. Hahn

*Department of Physics, University of California, Berkeley, California 94720*

and

Claude Hilbert and John Clarke

*Department of Physics, University of California, Materials and Molecular Research Division, Lawrence Berkeley Laboratory, Berkeley, California 94720*

(Received 12 August 1985)

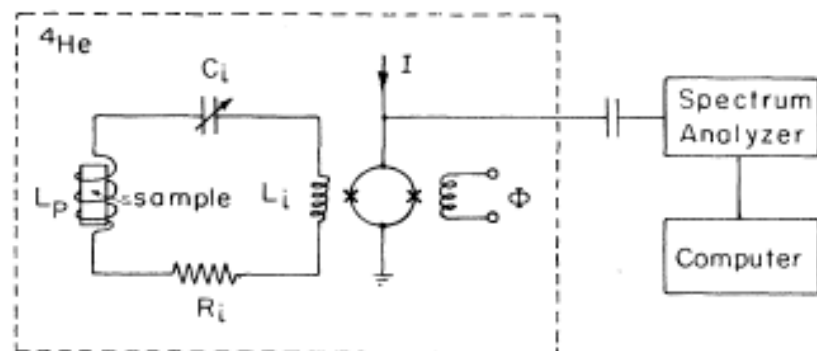


FIG. 1. Experimental configuration. Components in dashed box are immersed in liquid  $^4\text{He}$ .

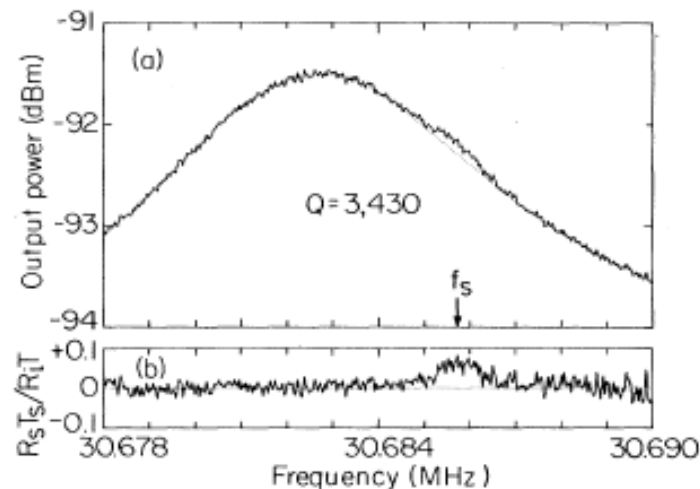


FIG. 3. Spectral density of (a) noise current for a  $\text{NaClO}_3$  sample with saturated spins ( $T_s = \infty$ ), and (b) nuclear-spin noise of  $\text{NaClO}_3$  sample obtained from (a).



# Nuclear spin noise imaging

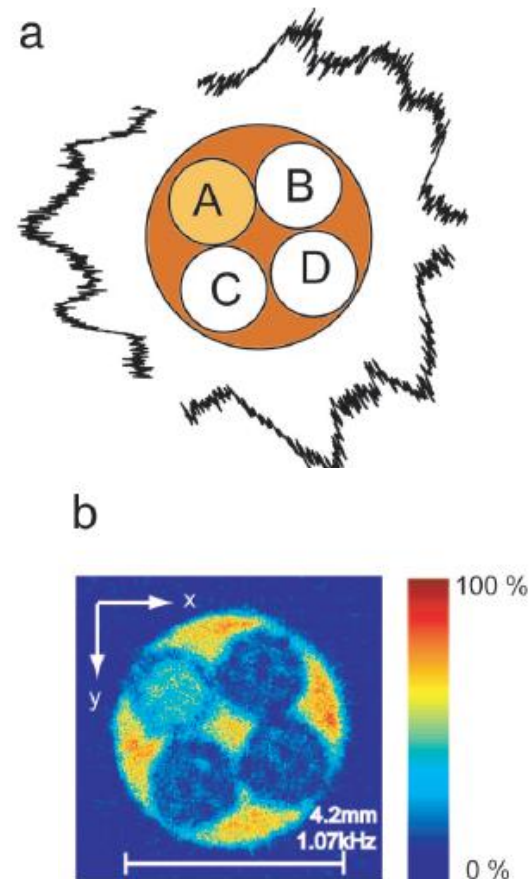
Proc. Nat. Acad. Sci. **103**, 6790 (2006)

Norbert Müller<sup>†</sup> and Alexej Jerschow<sup>‡§</sup>

<sup>†</sup>Institute of Organic Chemistry, Johannes Kepler University, Altenbergerstrasse 69, A-4040 Linz, Austria; and <sup>‡</sup>Department of Chemistry, New York University, 100 Washington Square East, New York, NY 10003

Communicated by E. L. Hahn, University of California, Berkeley, CA, March 9, 2006 (received for review December 7, 2005)

NMR images were obtained from the **proton spin noise signals** of a water-containing phantom, which was placed in the highly tuned, low-noise resonant circuit of a cryogenically cooled NMR probe in the presence of systematically varied magnetic field gradients. The spatially resolved proton spin density was obtained from the raw signal by a modified projection–reconstruction protocol. Although spin noise imaging is inherently less sensitive than conventional magnetic resonance imaging, **it affords an entirely noninvasive visualization of the interior of opaque objects or subjects. Thus, tomography becomes possible even when neither x-ray nor radio frequency radiation can be applied for technical or safety reasons.**



# Nanoscale magnetic resonance imaging

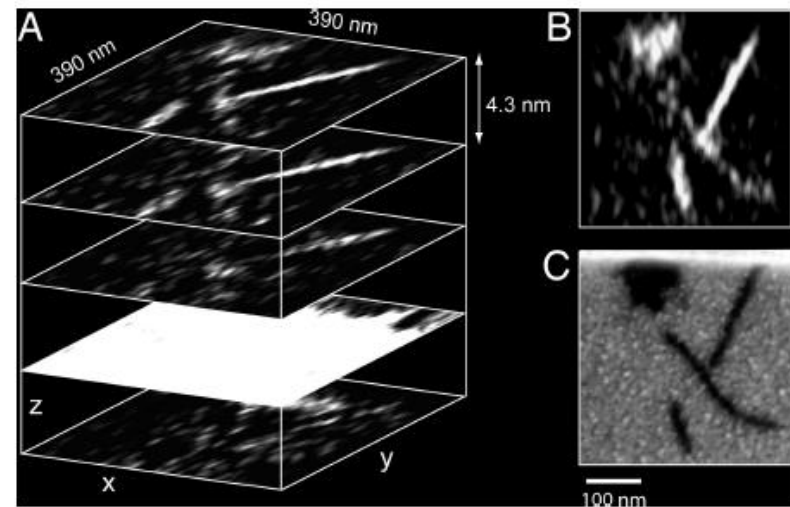
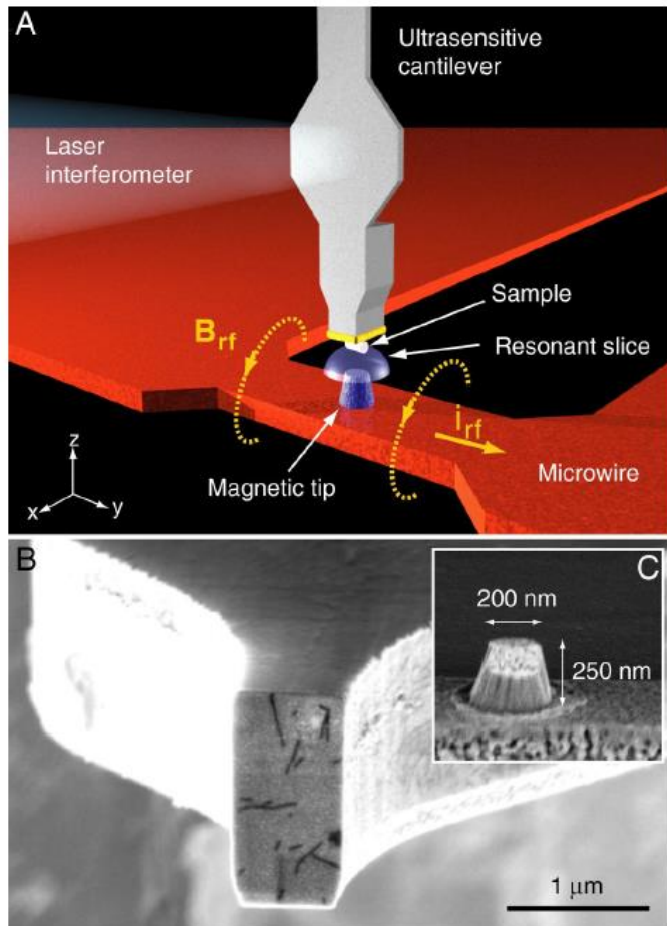
PNAS 106, 1313 (2009)

C. L. Degen<sup>a</sup>, M. Poggio<sup>a,b</sup>, H. J. Mamin<sup>a</sup>, C. T. Rettner<sup>a</sup>, and D. Rugar<sup>a,1</sup>

<sup>a</sup>IBM Research Division, Almaden Research Center, 650 Harry Road, San Jose, CA 95120; and <sup>b</sup>Center for Probing the Nanoscale, Stanford University, 476 Lomita Mall, Stanford, CA 94305

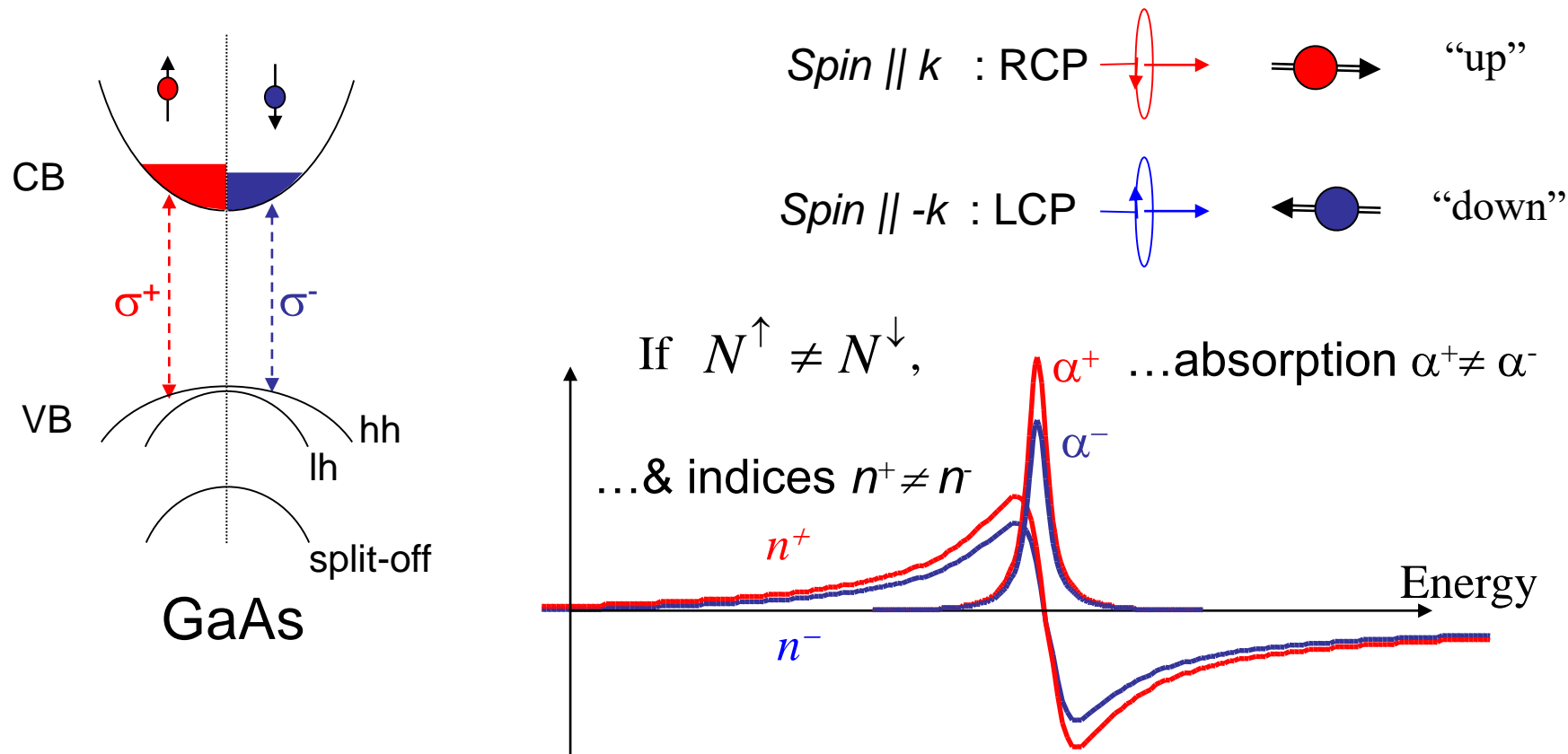
Communicated by Stuart S. P. Parkin, IBM Almaden Research Center, San Jose, CA, December 1, 2008 (received for review August 21, 2008)

The spin signal originates from the naturally occurring  $\sqrt{N}$  statistical polarization of the spin ensemble (“spin noise”), where  $N$  is the number of  $^1\text{H}$  spins in the measurement volume (19, 23, 31–33). Using the statistical polarization is advantageous because its root-mean-square amplitude exceeds the mean Boltzmann polarization for nanoscale volumes of spins (23).



# Passive detection of spin/valley noise using optical Faraday rotation

- Possible when  $\sigma^+/\sigma^-$  optical selection rules exist due to spin-orbit coupling  
eg, spin up/down in III-V semiconductors... or K/K' valleys in TMD monolayers

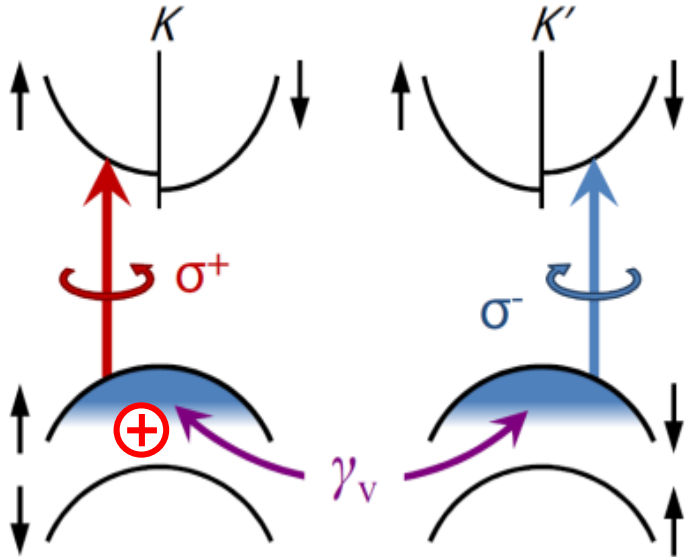


Faraday rotation:  $\theta_F(t) \propto n^+ - n^- \propto N^\uparrow - N^\downarrow \propto M_z(t)$

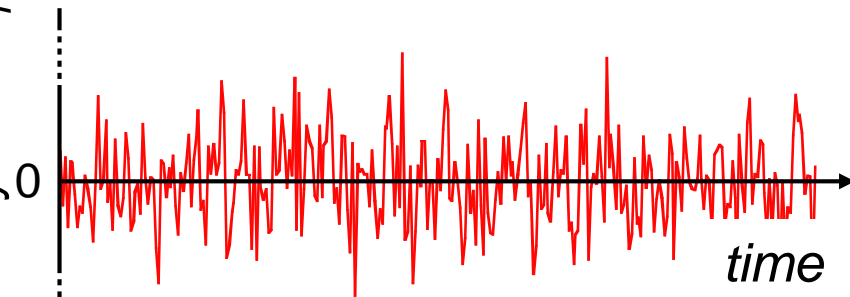
Probe laser can be tuned far from absorption, but still measure spin via  $n^+ - n^-$   
In this regard, it is "non-perturbing" probe

# “Valley Noise Spectroscopy” in TMD monolayers

Consider Fermi sea of holes  
in thermal equilibrium...



Valley polarization  
(Faraday rot.  $\delta\theta_F$ )

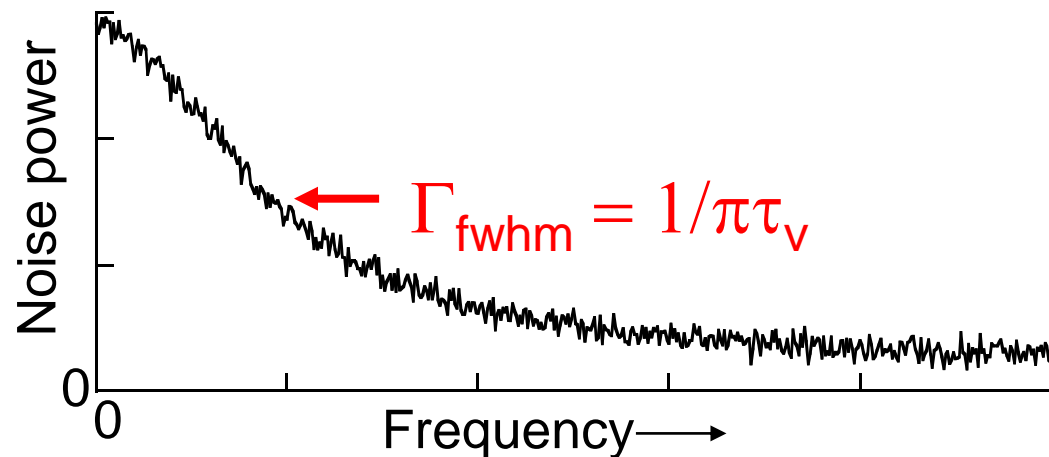


On average:  $\langle \delta\theta_F(t) \rangle = 0$

But fluctuations exist:  $\langle [\delta\theta_F(t)]^2 \rangle \neq 0$   
Valley correlation function:  $\langle \delta\theta_F(t) \delta\theta_F(0) \rangle$

*Spectrum of correlations:*  
“Valley Noise”

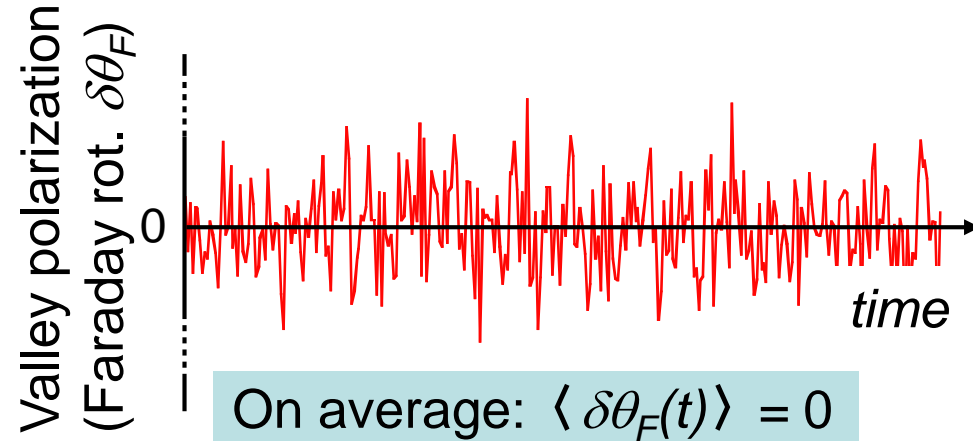
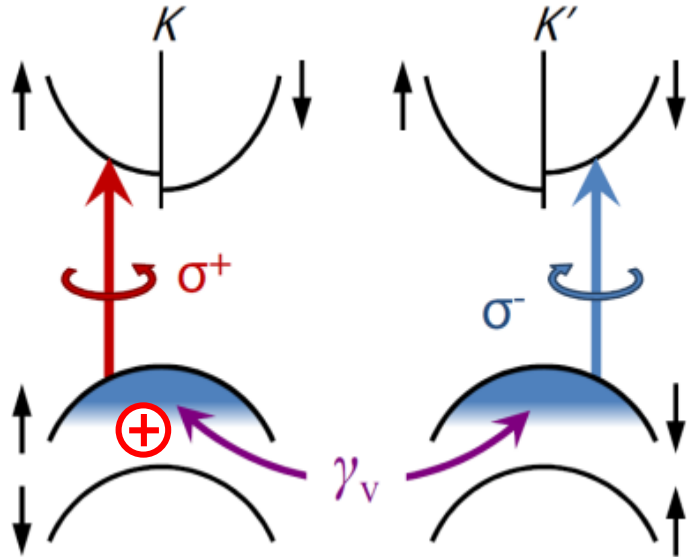
- *Width* gives timescales
- *Shape* gives mechanism  
*etc...*





# “Valley Noise Spectroscopy”

Consider Fermi sea of holes  
in thermal equilibrium...



But fluctuations exist:  $\langle [\delta\theta_F(t)]^2 \rangle \neq 0$   
Valley correlation function:  $\langle \delta\theta_F(t) \delta\theta_F(0) \rangle$

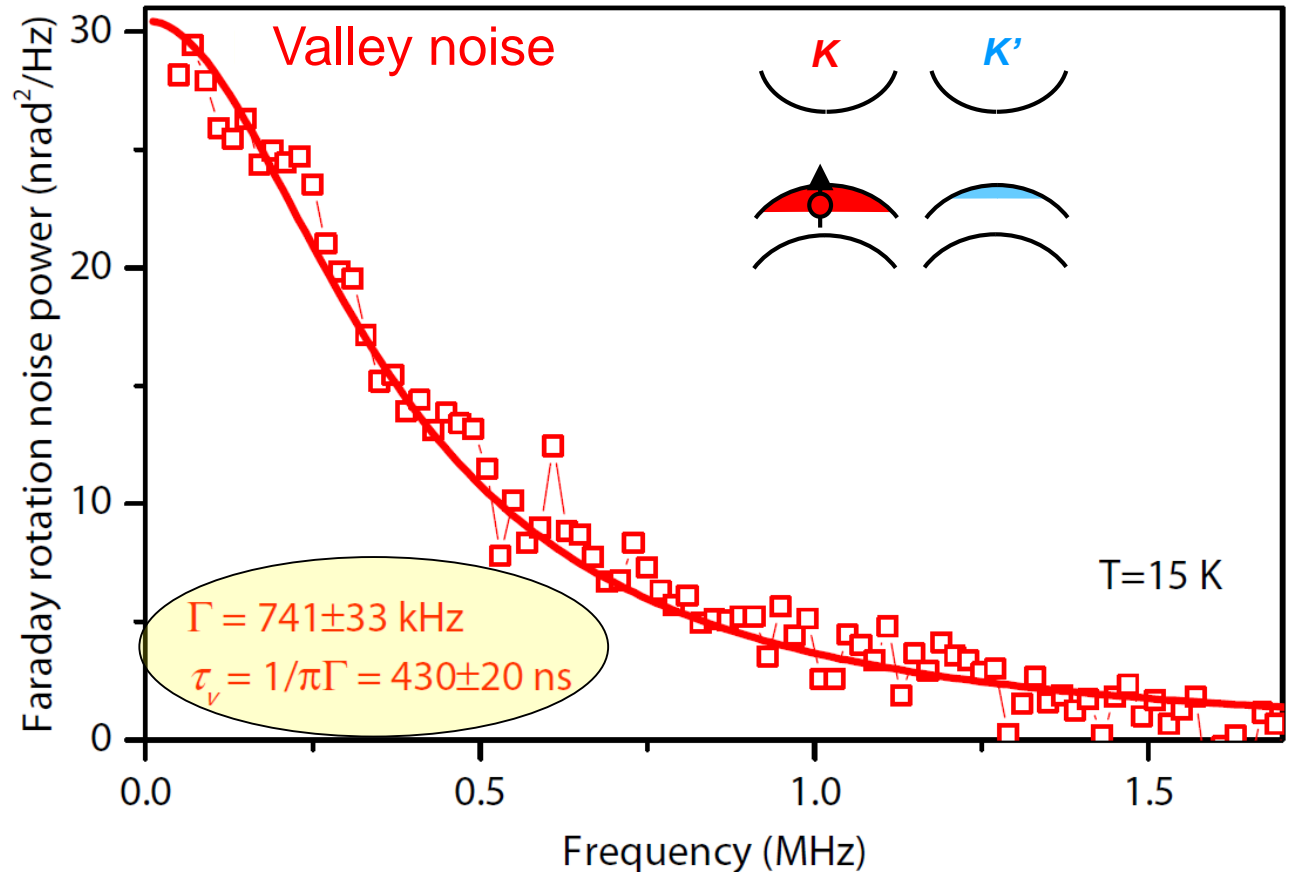
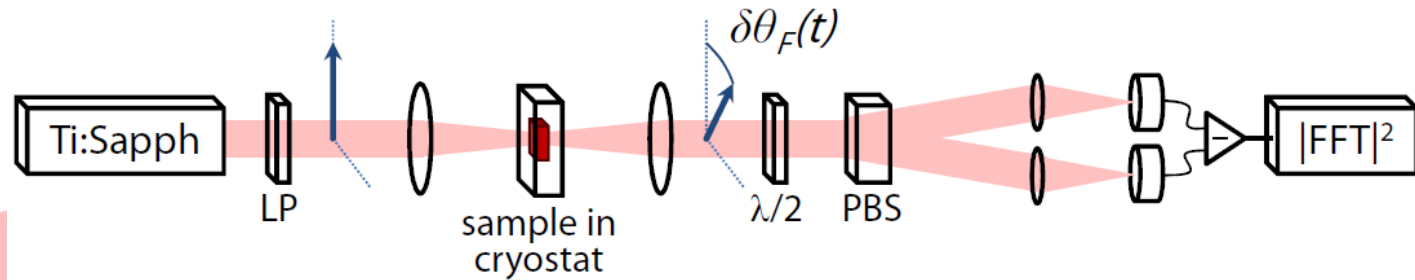
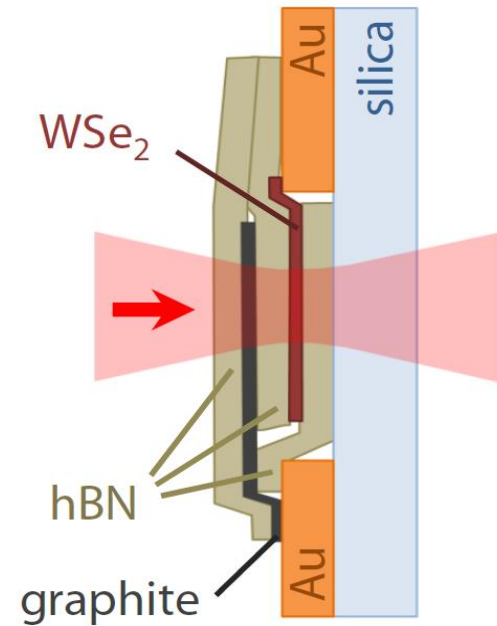
**Fluctuation-Dissipation Theorem:**  $\chi''(\omega) = \text{FFT} [ \langle \delta\theta_F(t) \delta\theta_F(0) \rangle ]$

*“Linear response of a system to external perturbation (ie, the susceptibility) can be described by the fluctuation properties of the system while in thermal equilibrium”.*

• *In principle: valley noise alone describes valley dynamics*

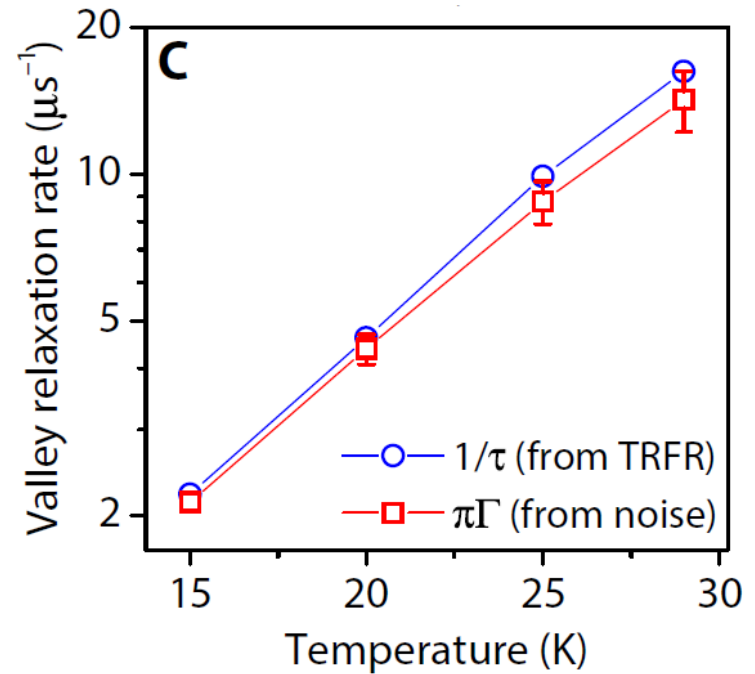
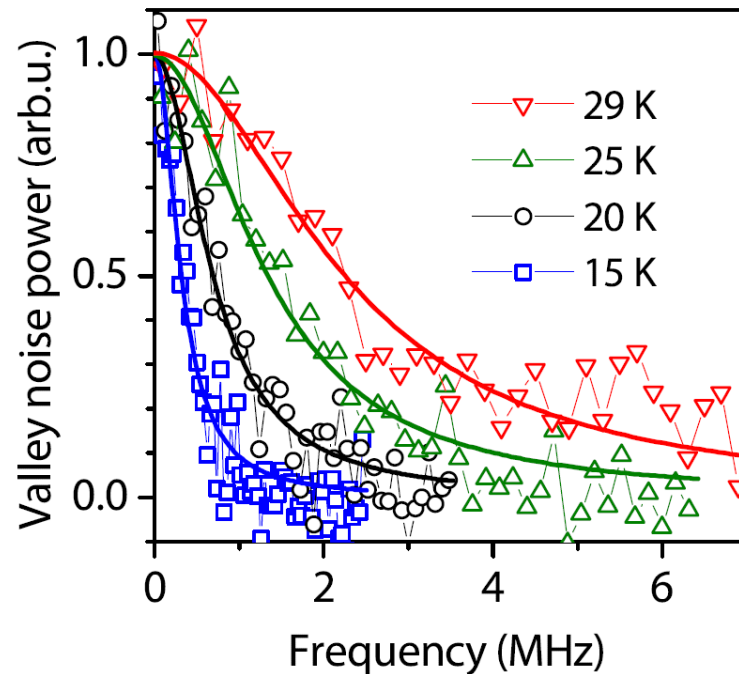
*\*\*No perturbation, drive, or excitation necessary\*\**

# “Listening” to valley noise of holes in monolayer WSe<sub>2</sub>



Nathan Wilson  
(U Washington)

# Temperature-dependent valley relaxation of holes



## Theory:

Ochoa, Fal'ko, PRB (2014)

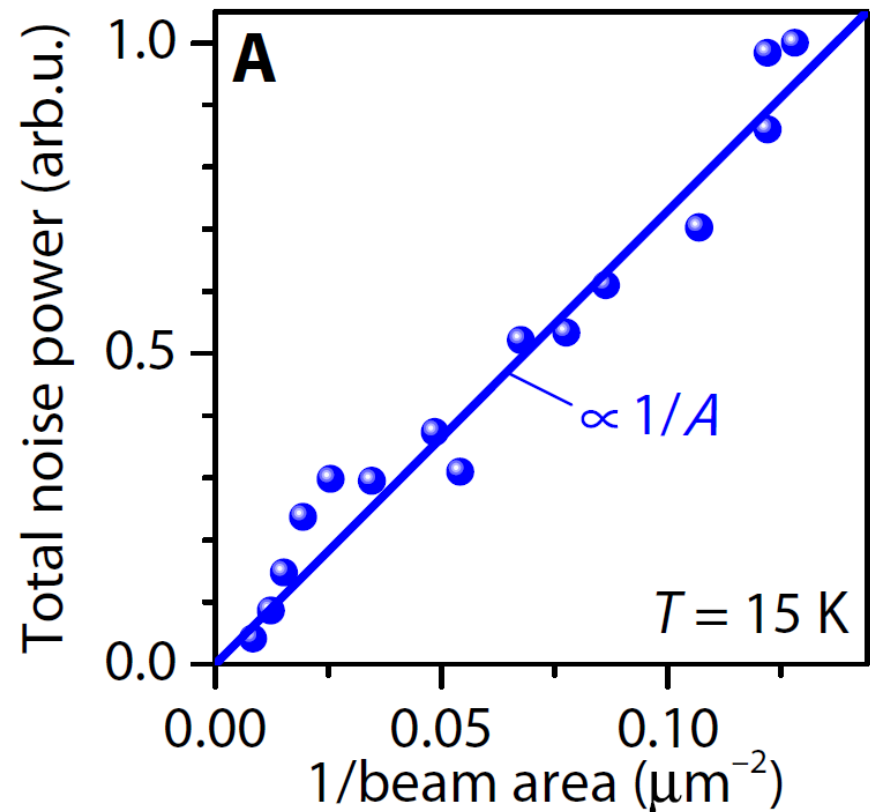
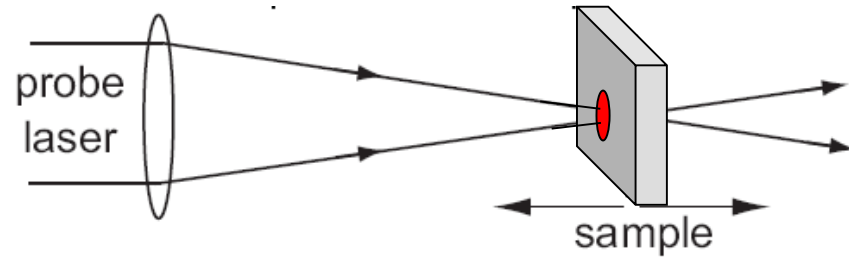
Yu & Wu, PRB (2014)

Song & Dery, PRL (2013)

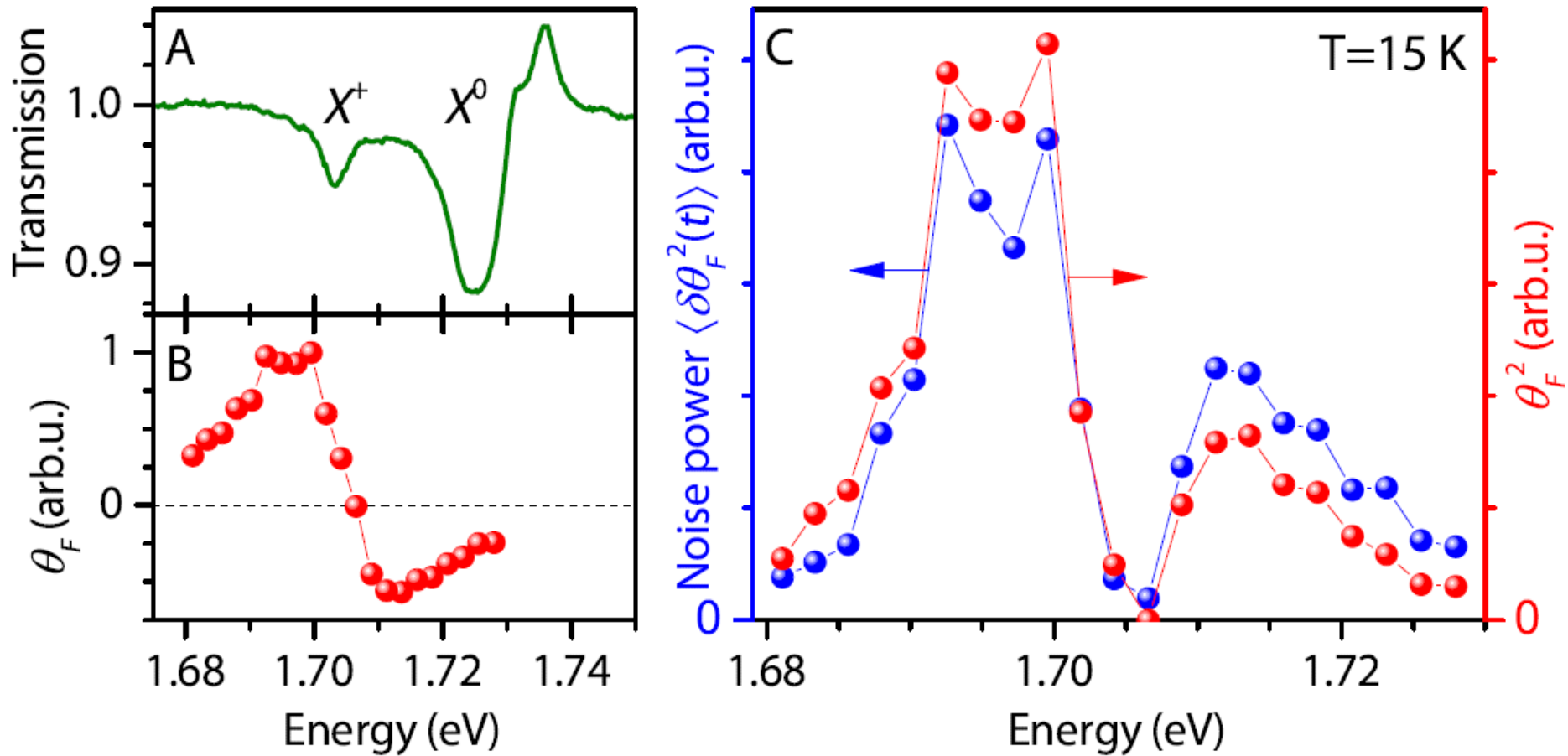
Kormanyos, 2D Mater (2015)

# Inverse scaling with probed area – *fewer* holes give *more* noise

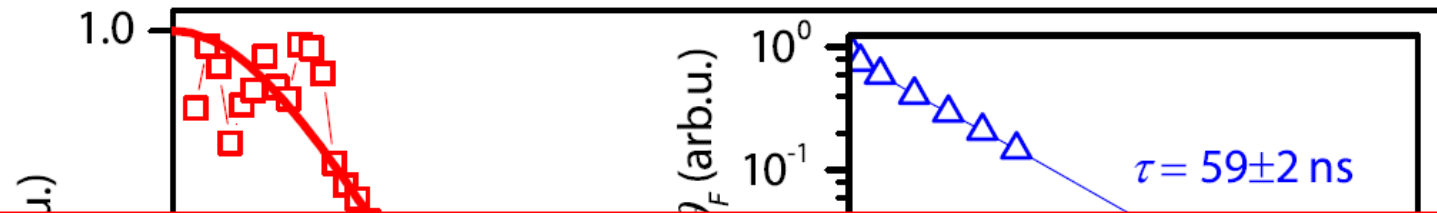
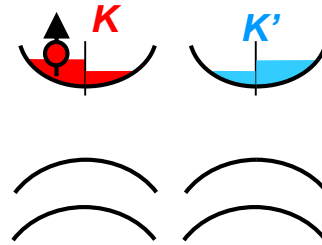
Noise signal is a *larger* fraction of saturated signal when probing *fewer* holes.



# Spectral dependence of valley noise

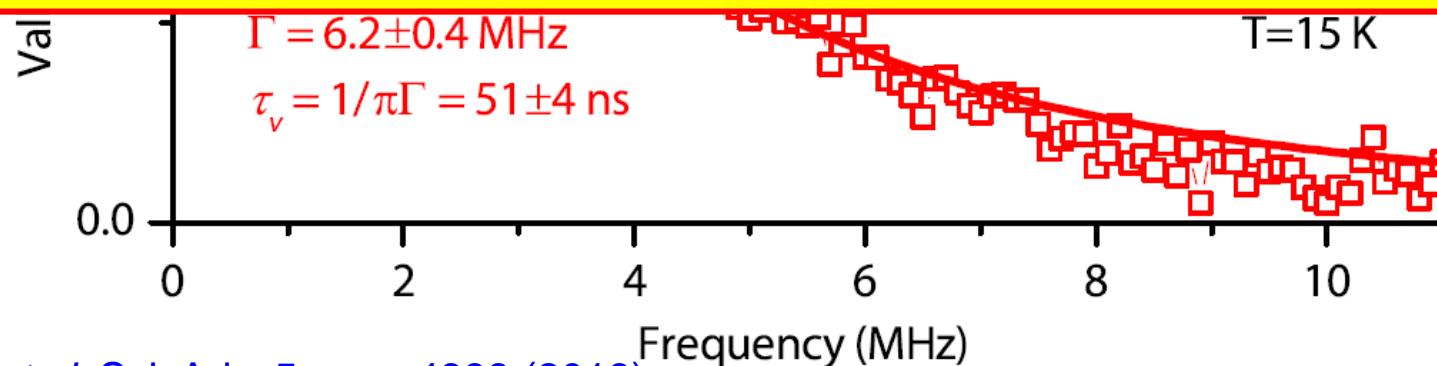


# Electron valley noise in *n*-type monolayer WSe<sub>2</sub>



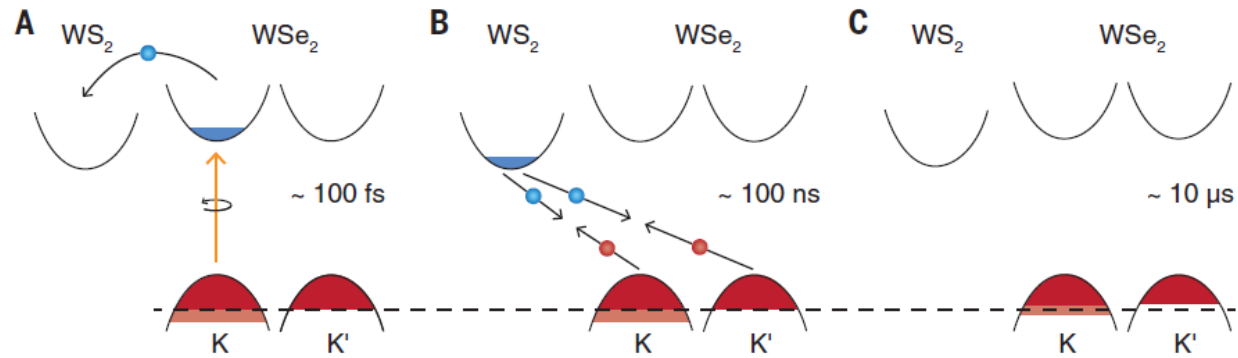
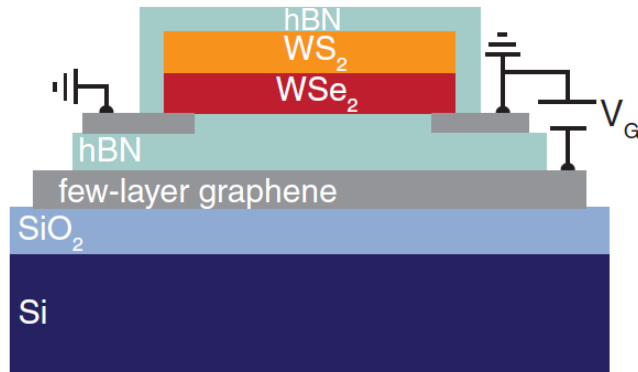
## Main message:

Passive noise signals reveal truly intrinsic valley dynamics  
Validates earlier studies based on conventional pump-probe  
 $\sim 1$  microsecond for holes (pretty long!)  
 $\sim 100$  ns for electrons (not too bad)

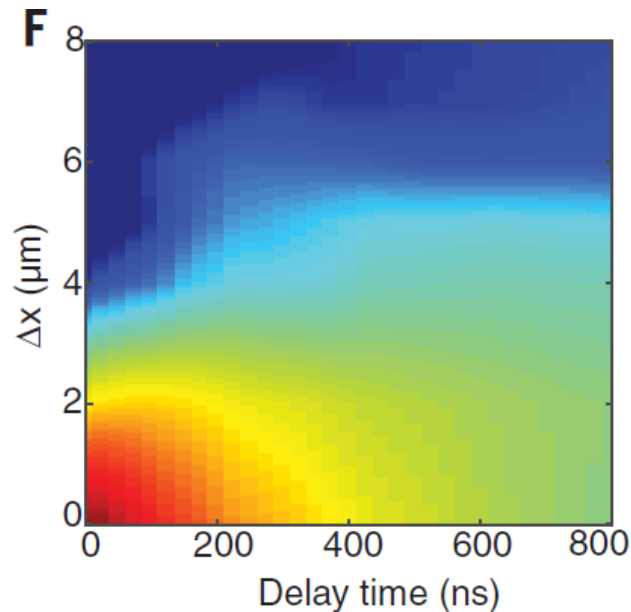
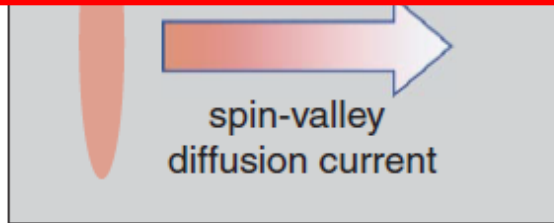




# Imaging of pure spin-valley diffusion current in $\text{WS}_2$ - $\text{WSe}_2$ heterostructures Jin *et al.*, *Science* **360**, 893–896 (2018)

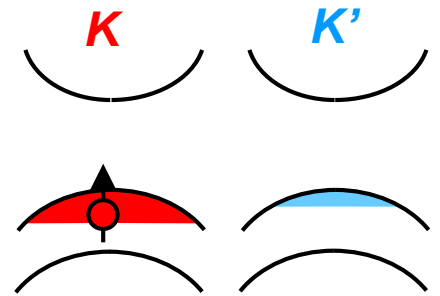
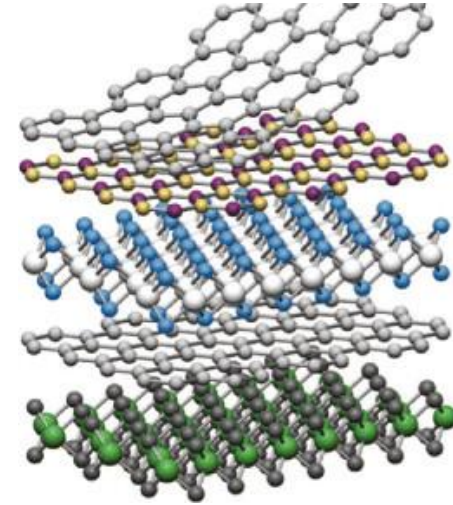


- Tens of microseconds
- Tens of microns transport
- (*but still no  $K \leftrightarrow K'$  switching*)



# Summary

- **Valley dynamics in monolayer TMDs**
  - *Really short for excitons ( $\sim 1$ ps)*
  - *Reasonably long for resident electrons and holes (but still only at low temperature)*
- **Thermodynamic “valley noise”**
  - *Nonperturbative access to intrinsic dynamics*
  - *Perhaps useful approach for quantum measurement*
  - *Validates recent pump-probe studies of carriers*



M. Goryca *et al*, Science Advances 5, eaau4899 (2018)  
P. Dey *et al.*, PRL **119**, 137401 (2017)

## Thank you!